

# Navigation

Gregor Schöner

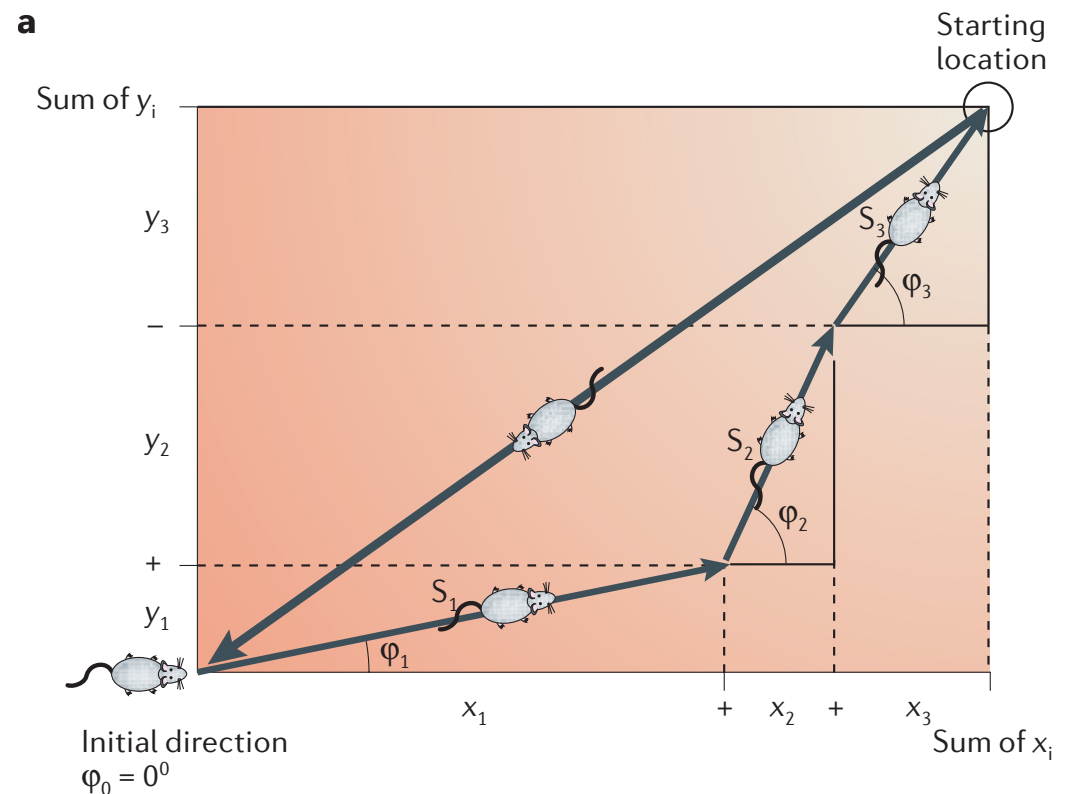
June 2024

# Problem

- we talked about how to plan motion toward targets avoiding obstacles
- in many cases, information about targets may be available through a **map** that represents where relevant locations are in the world
- to use a map, a robot/organism needs to know “where it is” on the map: ego-location estimation
- that estimate must be updated as a robot/organism moves...

# Dead-reckoning/path integration

- if the agent knows its current velocity=heading direction + speed (and keeps track of time), it can estimate its change of position by integration



[McNaughton et al., *Nature reviews neuroscience* 2006]

# Dead-reckoning/path integration

- a long history in technology... dating back to literal “navigation”: sailing ships...
- estimating heading direction based on a compass
- estimating speed by counting “knots”... which entails an estimate of time
- updating position in a map



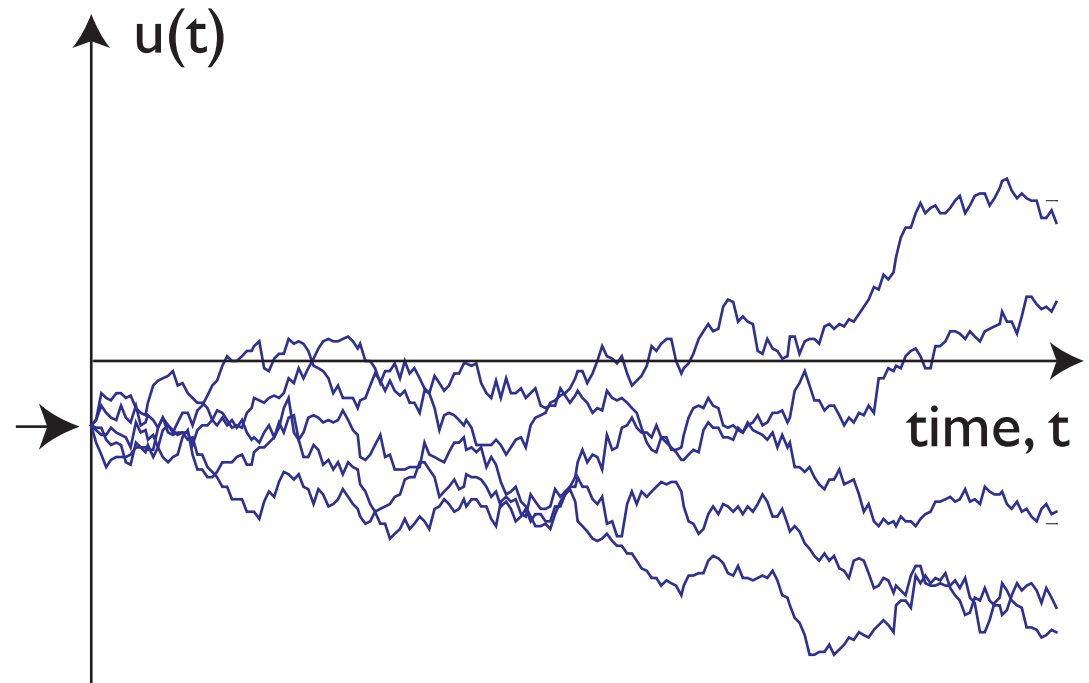
# Dead-reckoning/path integration

- modern technology increases the precision
  - e.g. inertial guidance by measuring acceleration
  - precise measurement of time
  - with good control, the control signals can also be used to predict the new state ...
  - optimal estimation integrates prediction and measurement...

# Dead-reckoning/path integration

## ■ fundamental problem

- the integration leads to an accumulation of uncertainty...
- the principle of Brownian motion...



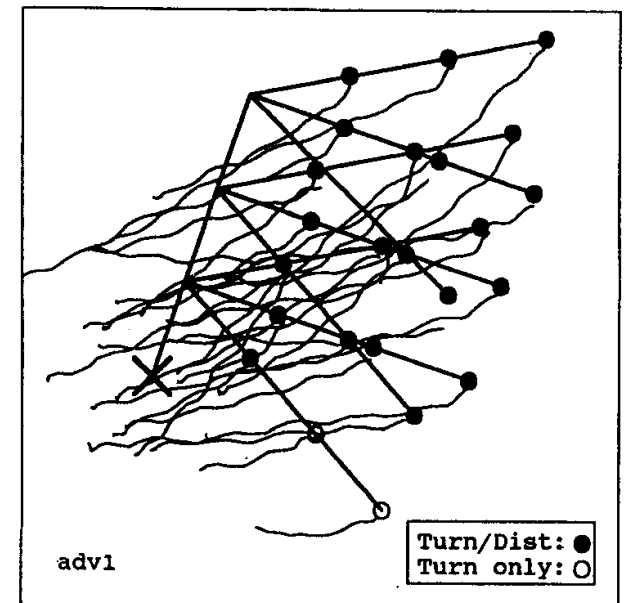
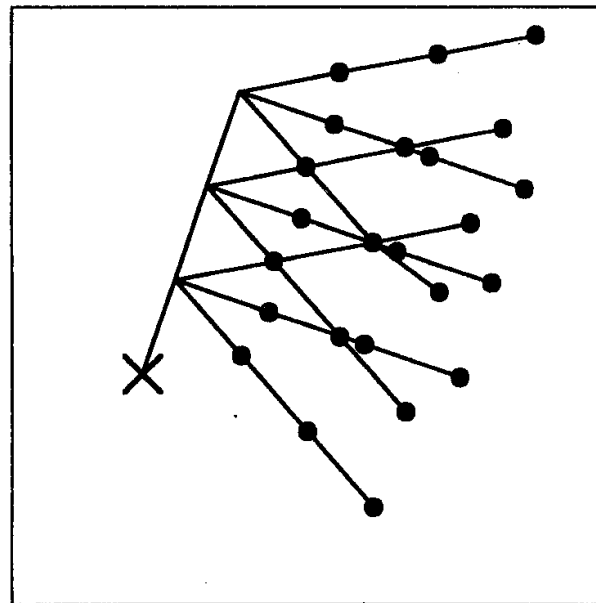
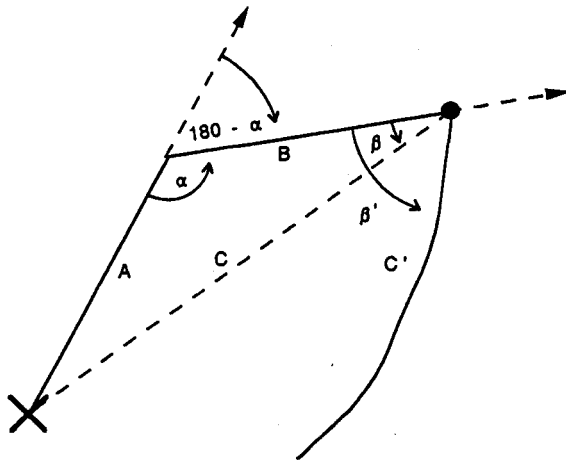
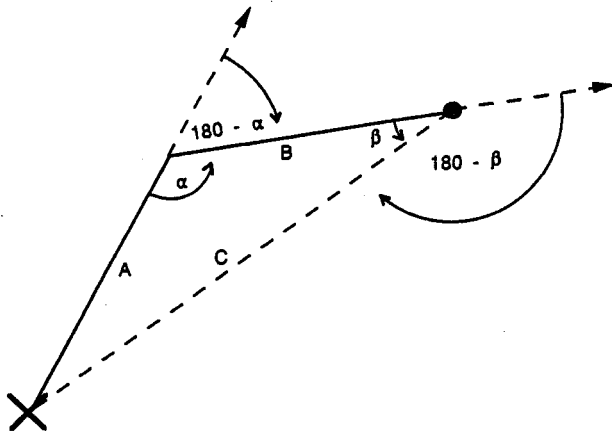
# Dead-reckoning/path integration

- a need for “recalibration” or re-setting of the estimate.. based on “recognizing” the true location on the map...
- historical solution:
  - landmark recognition...
  - triangulation
- modern variants based on special beacons, GPS etc

# Dead-reckoning/path integration

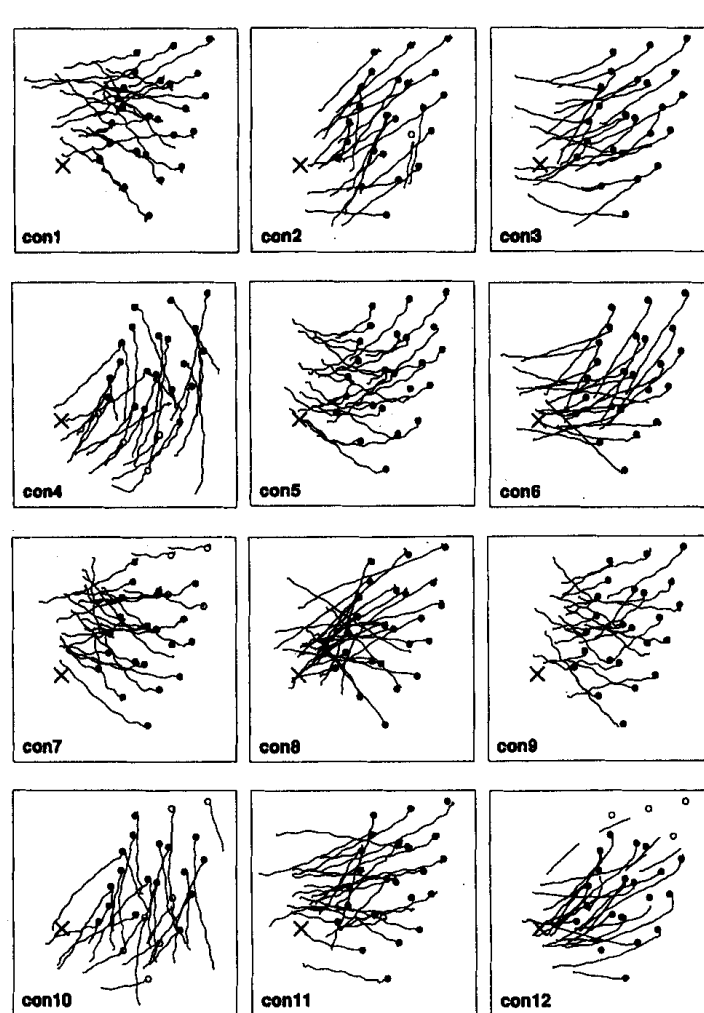
- animals including humans use path integration

guided along solid lines until dot  
return to start location X  
without vision

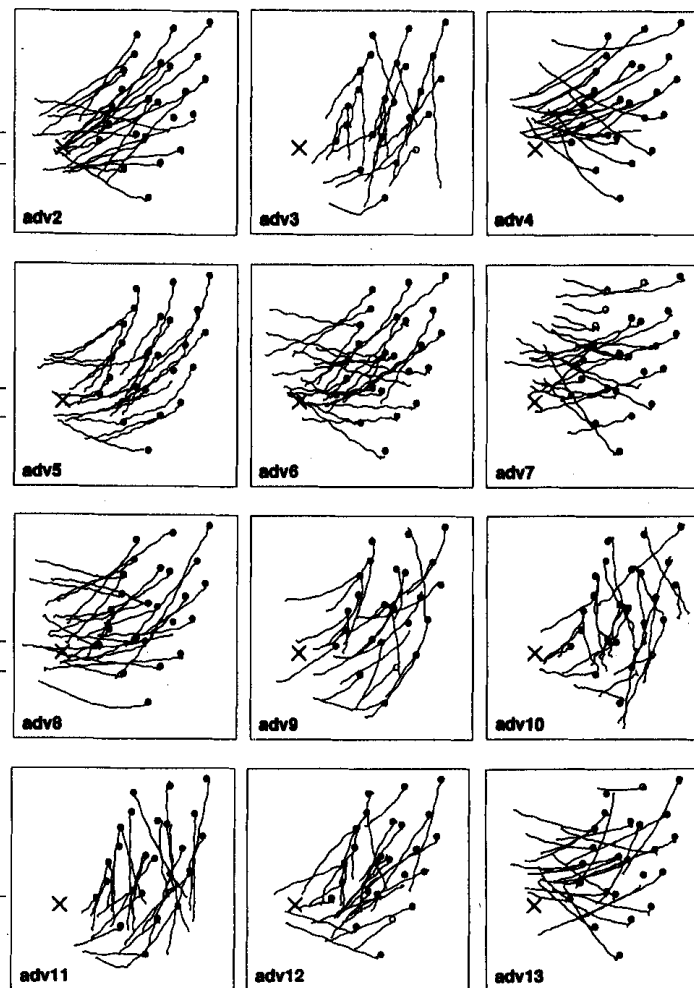


adventitiously blind

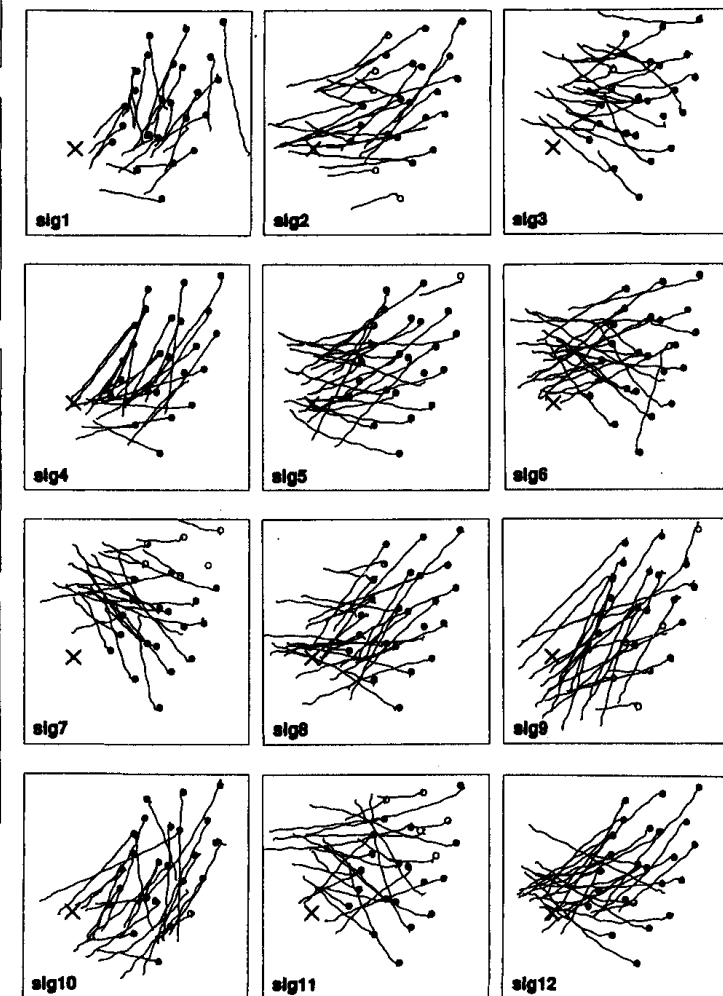
[Loomis, Klatzky, 1993]



blind from birth



blind from accident



seeing

*Errors on the Triangle-Completion Task by Group*

Error	Turn error (degrees)			Distance error (cm)		
	Con	Adv	Sighted	Con	Adv	Sighted
Absolute	24	22	24	137	107	168
Signed	-16	3	-4	-83	-61	-161

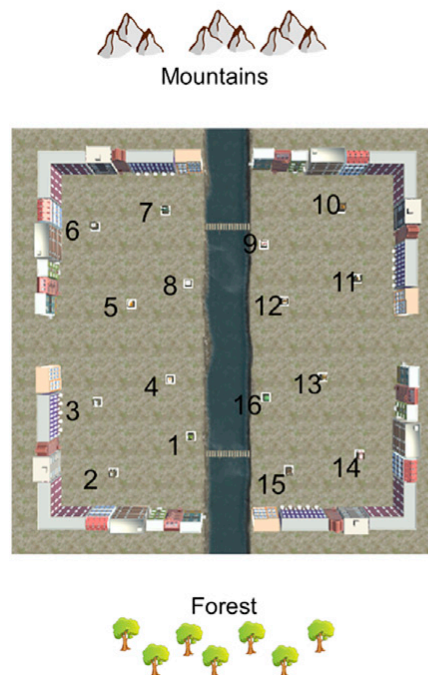
*Note.* Con = congenitally blind; Adv = adventitiously blind.

# Landmark recognition

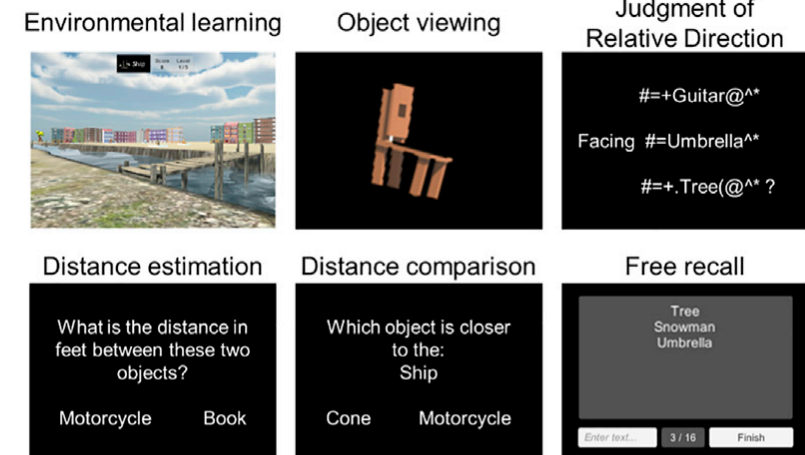
- landmarks are not necessarily objects...
- empirical evidence that views serve to estimate ego-position and pose

- evidence for use of views from animal behavior and neural data

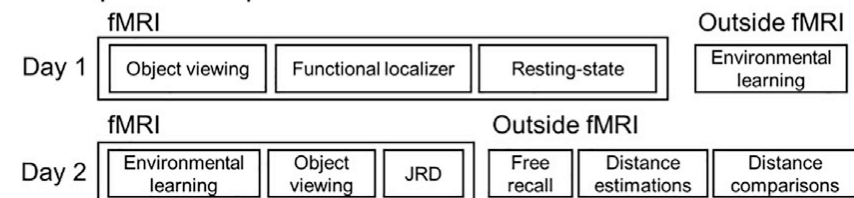
**A** Experimental environment



**B** Experimental tasks

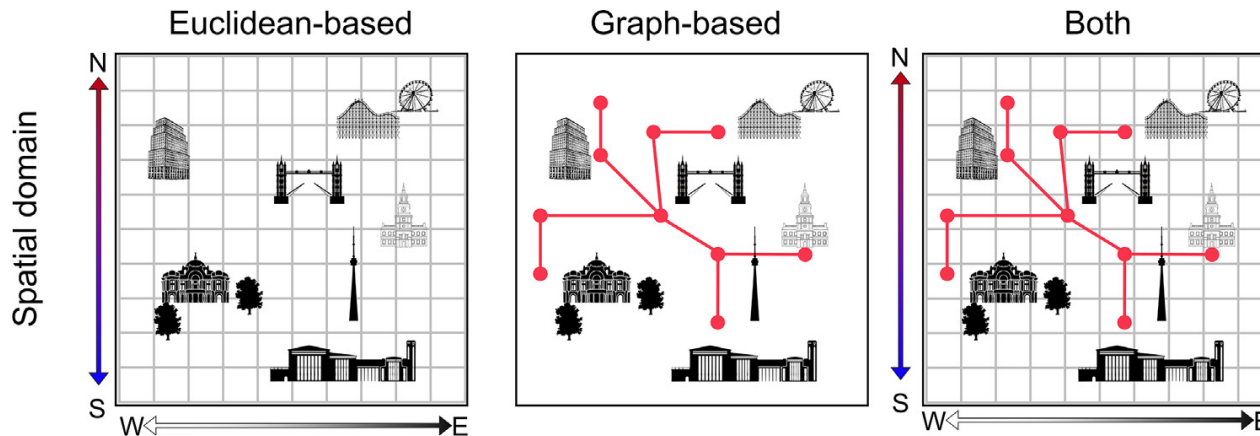


**C** Experimental procedure

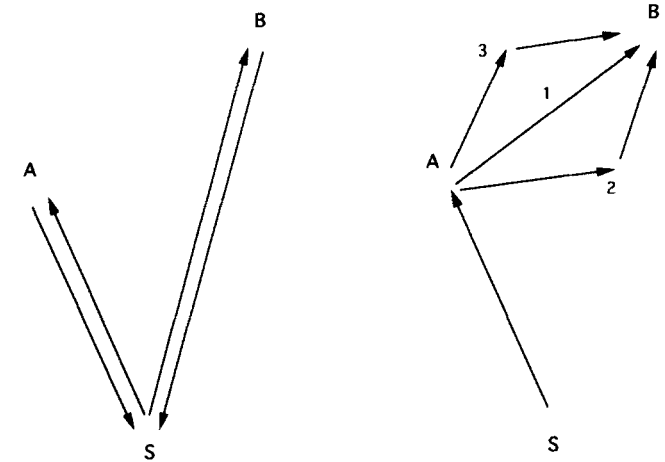


# Maps

- when can we say that an animal uses a map?
- rather than use stimulus-response chaining
- => when it can take short-cuts



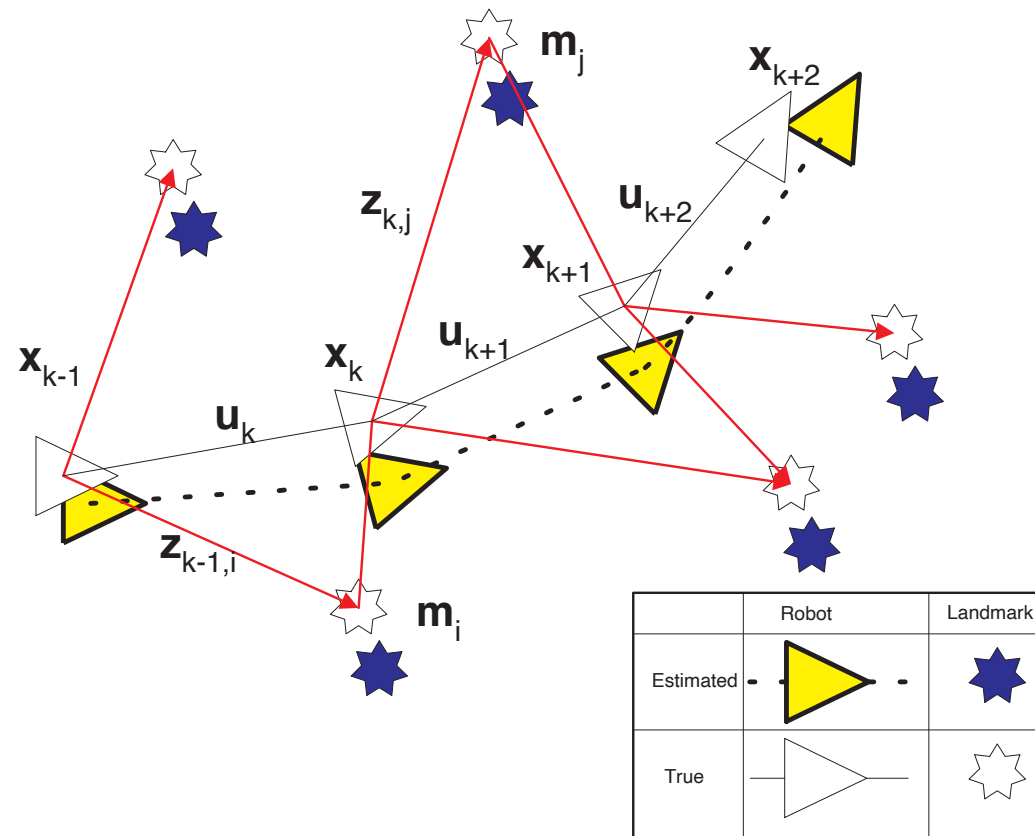
[Peer et al, 2020]



[Poucet, 1993]

# SLAM

## ■ Simultaneous Localization and Mapping



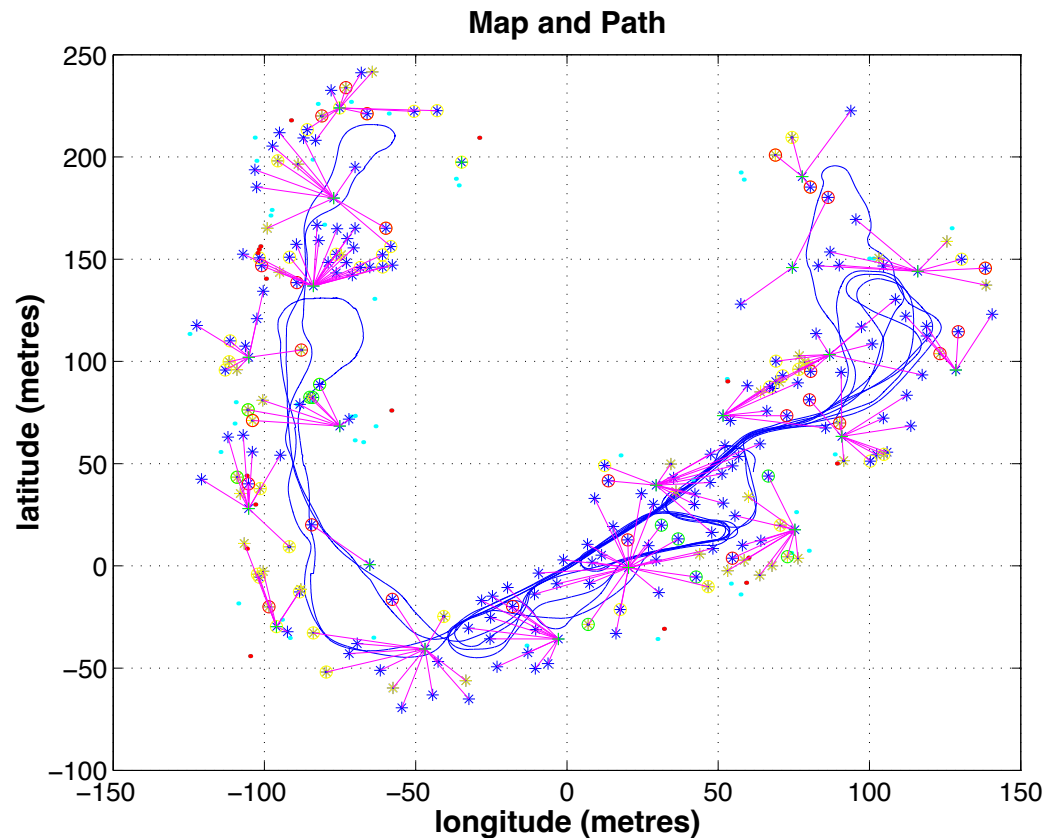
[Durrant-Whyte, Bailly, 2006]



# SLAM

- problem of learning/optimizing path integration...  
and using this to associated landmark information  
with locations

- problem of  
loop closure



# (Neural) dynamics of navigation

- dynamics for ego-position estimation
- dynamical approach to learning the map: network of locations (home bases) at which the agent knows where it is relative to others
- dynamics of path planning



Robotics and Autonomous Systems 20 (1997) 133–156

Robotics and  
Autonomous  
Systems

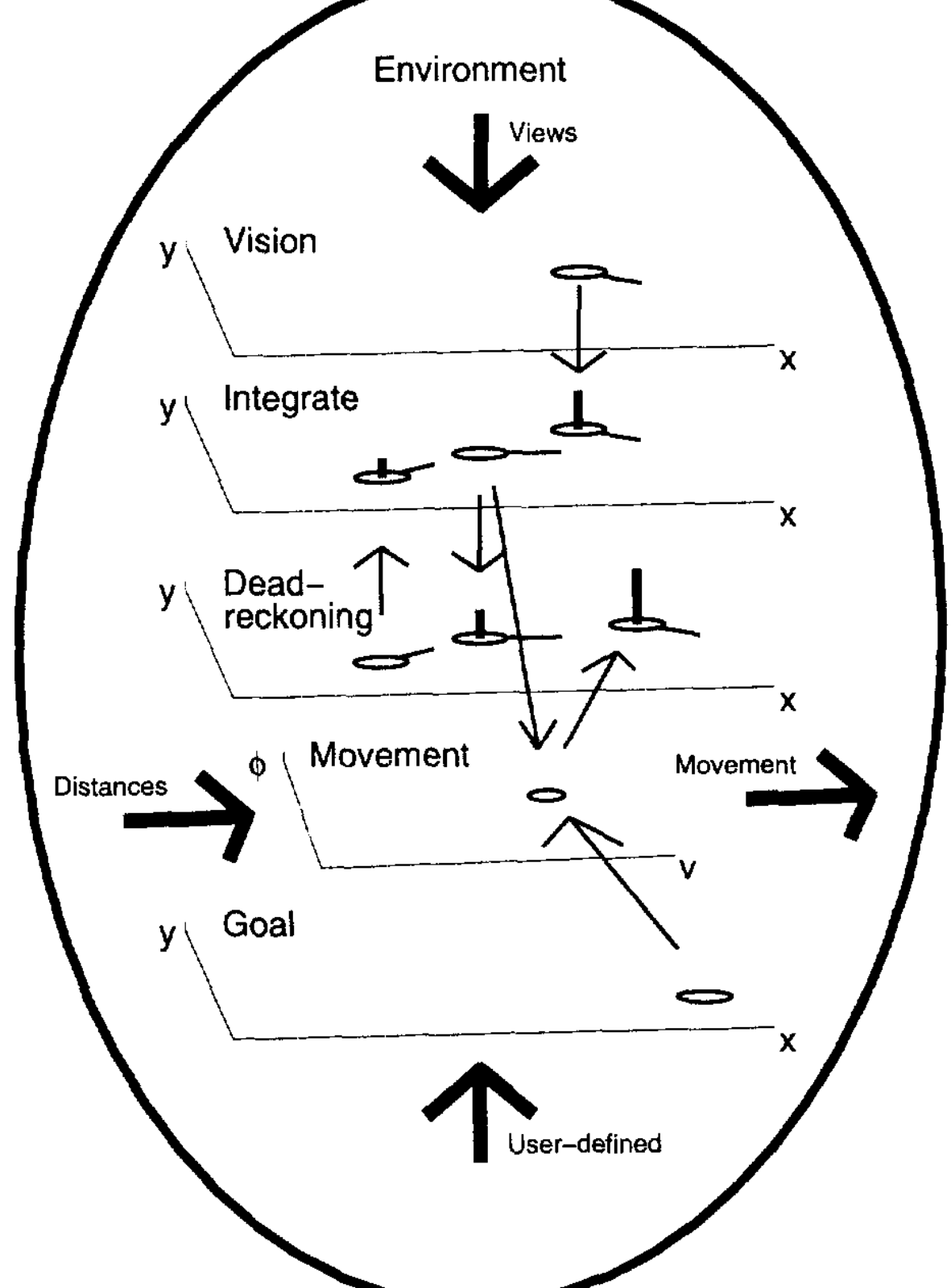
Self-calibration based on invariant view recognition:  
Dynamic approach to navigation

Axel Steinhage<sup>a,\*</sup>, Gregor Schöner<sup>b</sup>

<sup>a</sup> Institut für Neuroinformatik, Ruhr-Universität Bochum 44780 Bochum, Germany

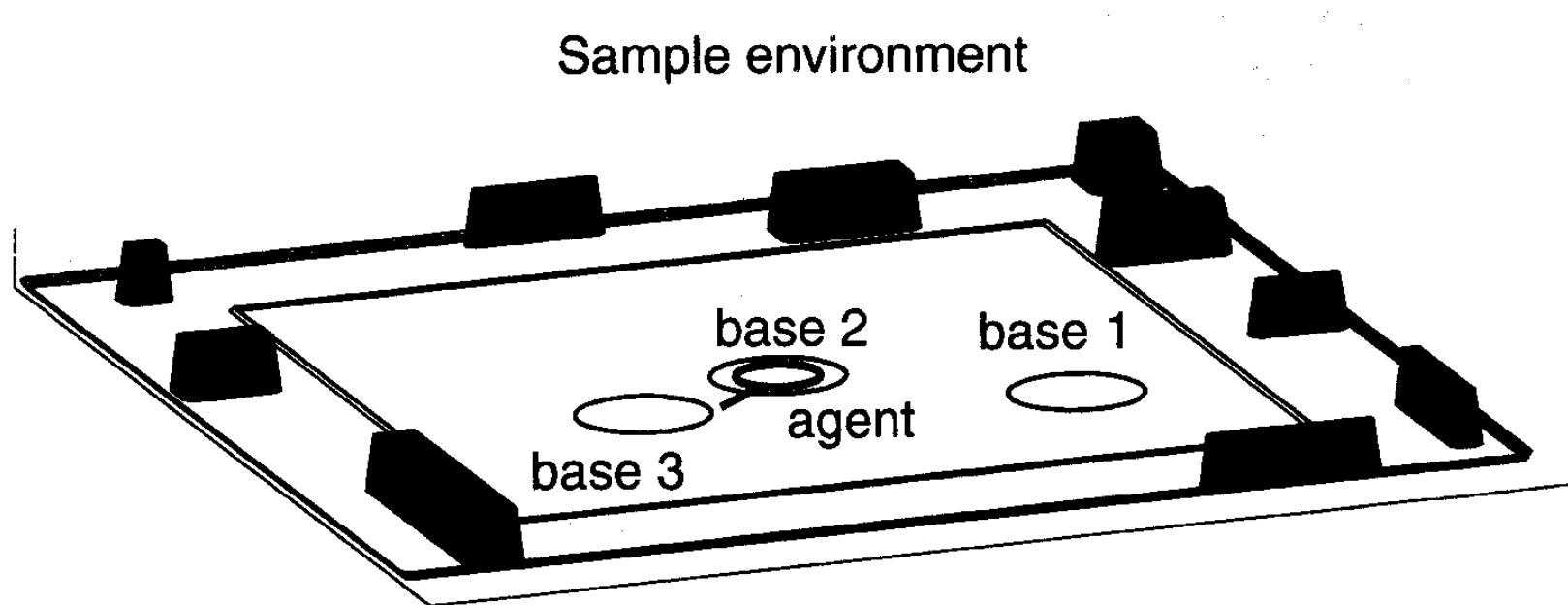
<sup>b</sup> Centre de Recherche en Neurosciences, Cognitives, CNRS 13402 Marseille, Cédex 20, France

# Neural and behavioral architecture



# Visual place navigation

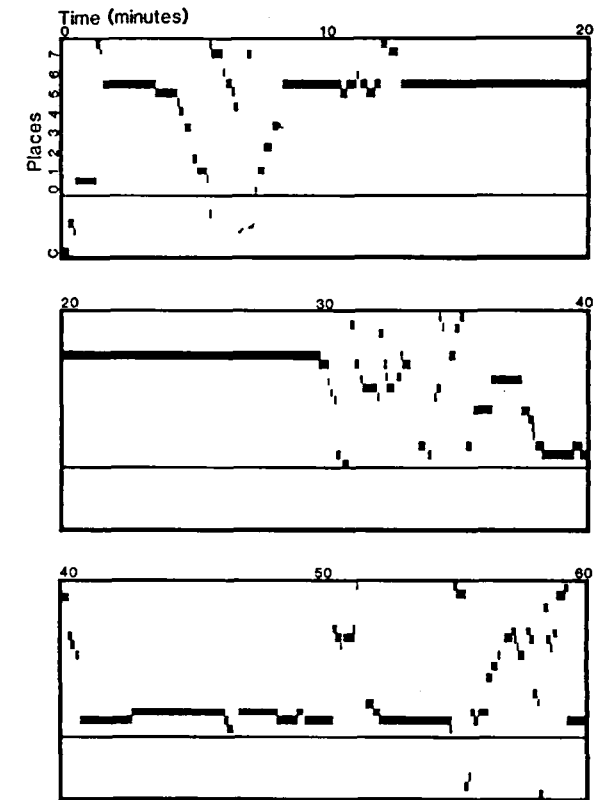
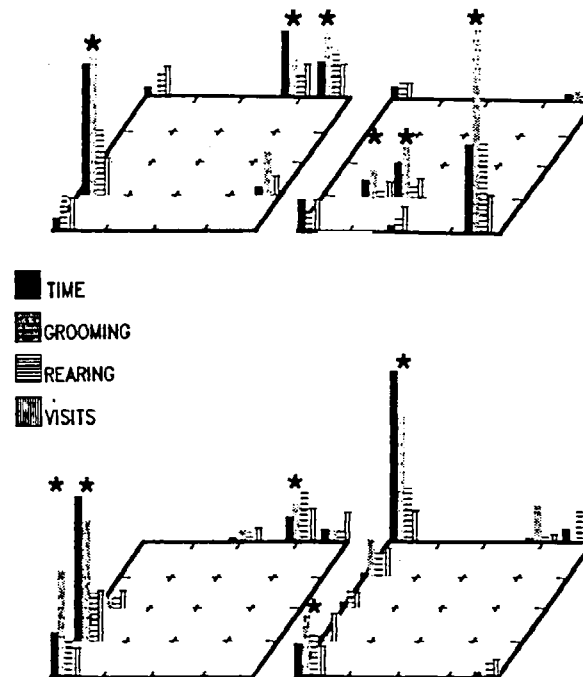
- a visual surround (unsegmented) acquired in clusters around particular locations (home bases)
- views are stored together with current position estimate (translation/rotation)



# Evidence for home bases

- animals in given terrain build home bases by rearing in locations where they spend most of their time

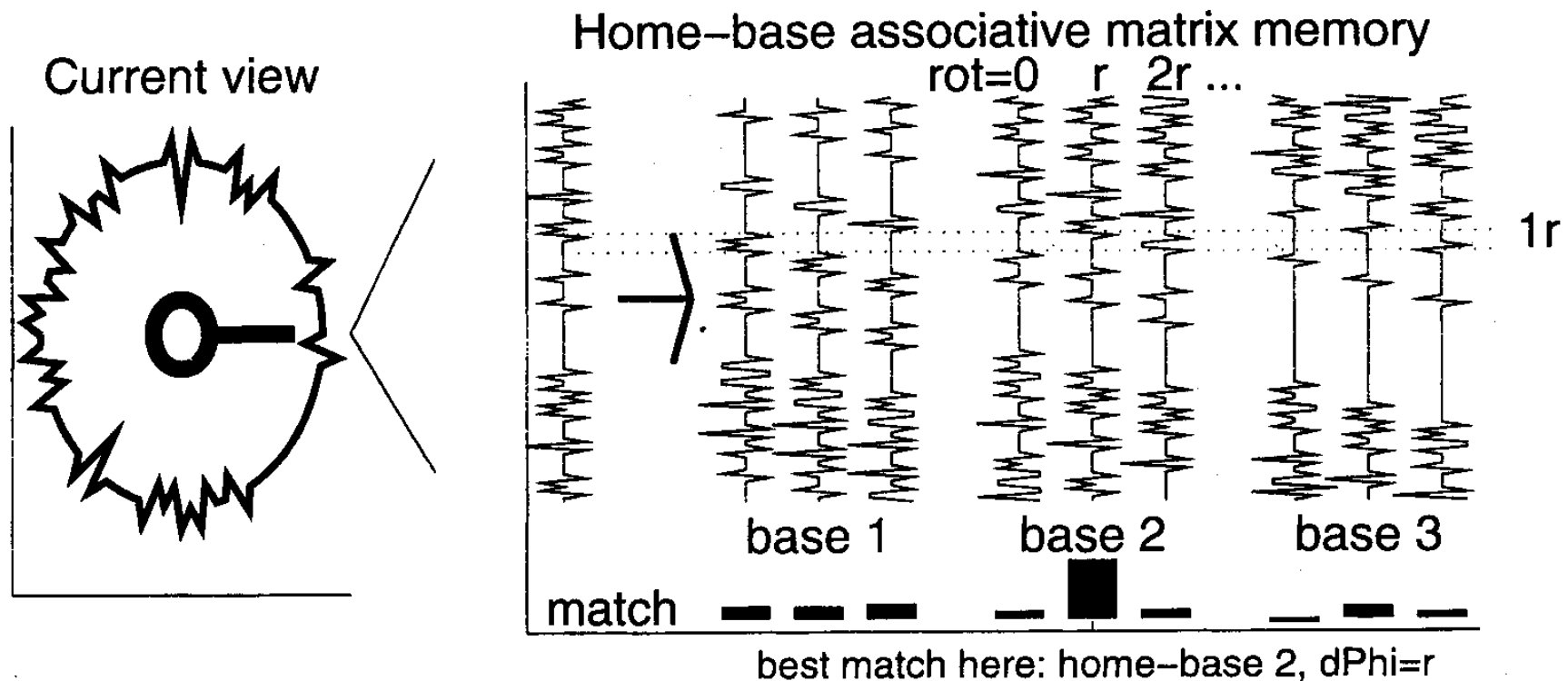
7	7'	0	0'	1
6'	7'	0'	1'	1'
6	6'	C	2'	2
5'	5'	4'	3'	2'
5	4'	4	3'	3



[Eilam, Golani, 1989]

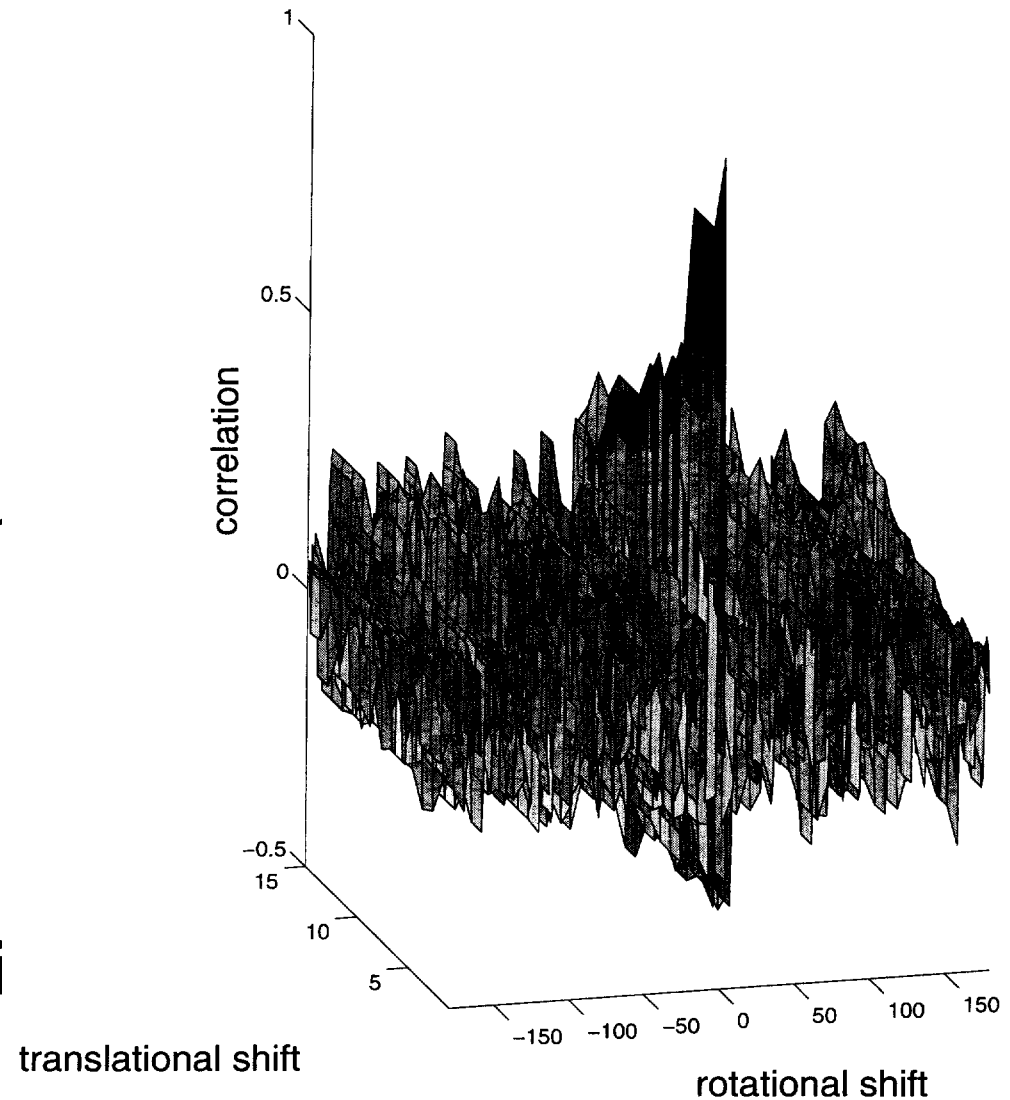
# Visual place navigation

- Each view in home base is matched to current view.... with all possible rotations actively generated from memorized view



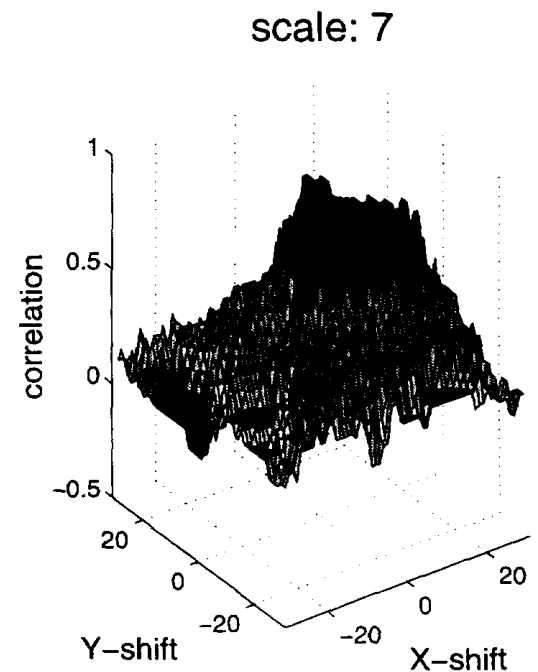
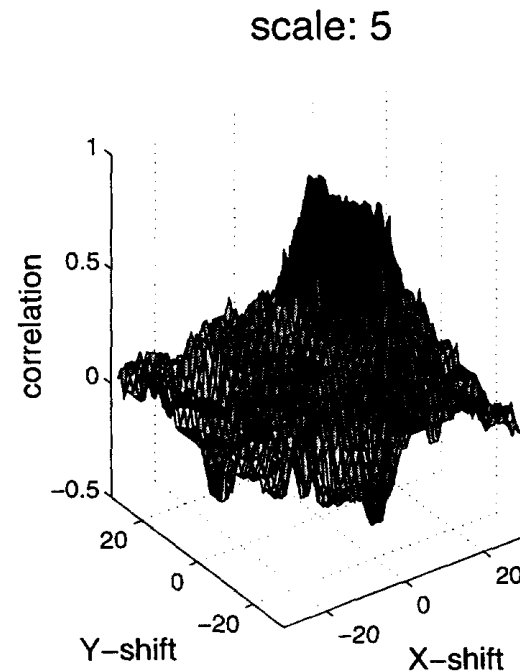
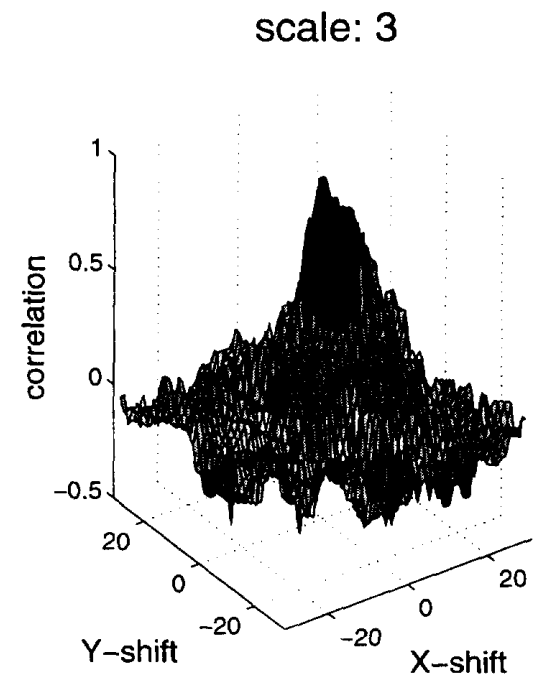
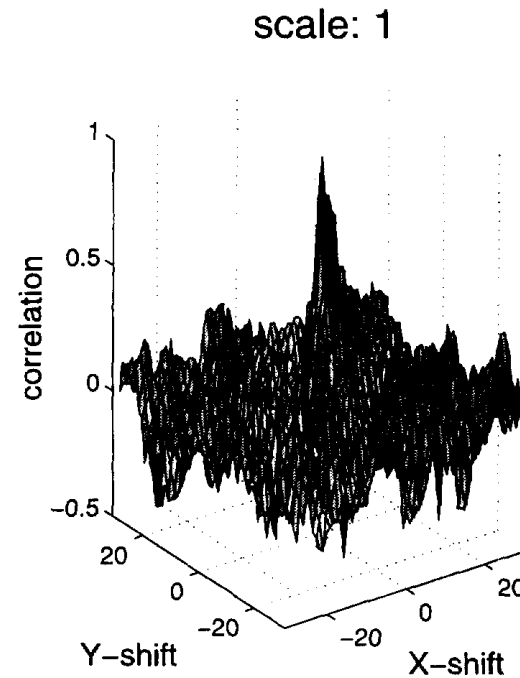
# Visual place navigation

- Correlation function across rotation angle peaks sharply at true angular orientation of agent, even if translation is not precise...
- so that estimation of orientation is possible while agent is in receptive field of place cell



# Visual place navigation

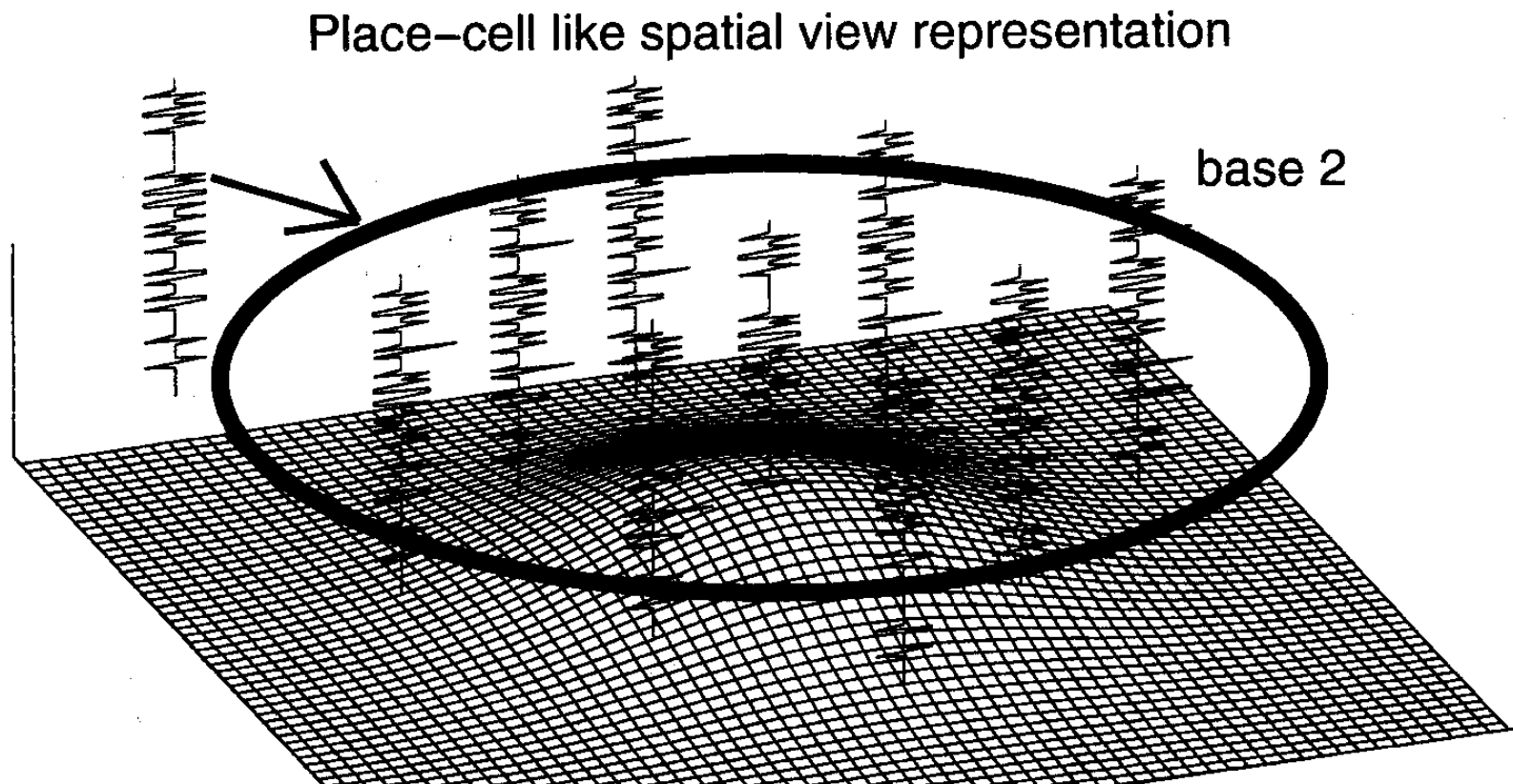
- Correlation with actively shifted memory views decays spatially in way that reflects how distal the view is.... place field..



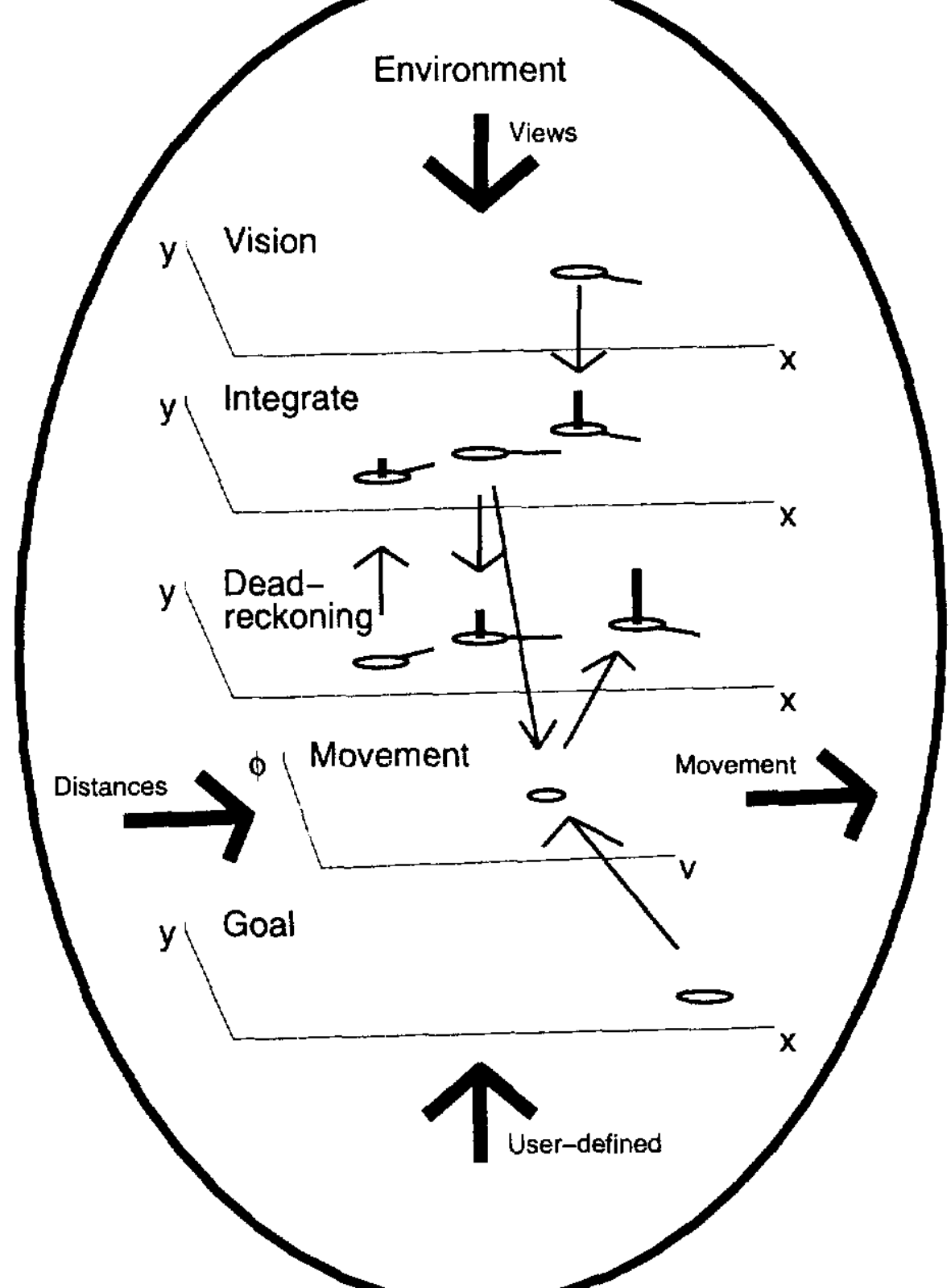


# Visual place navigation

- The level of correlation across multiple views within a home base generates a place view representation of translation  $\Rightarrow$  position estimate

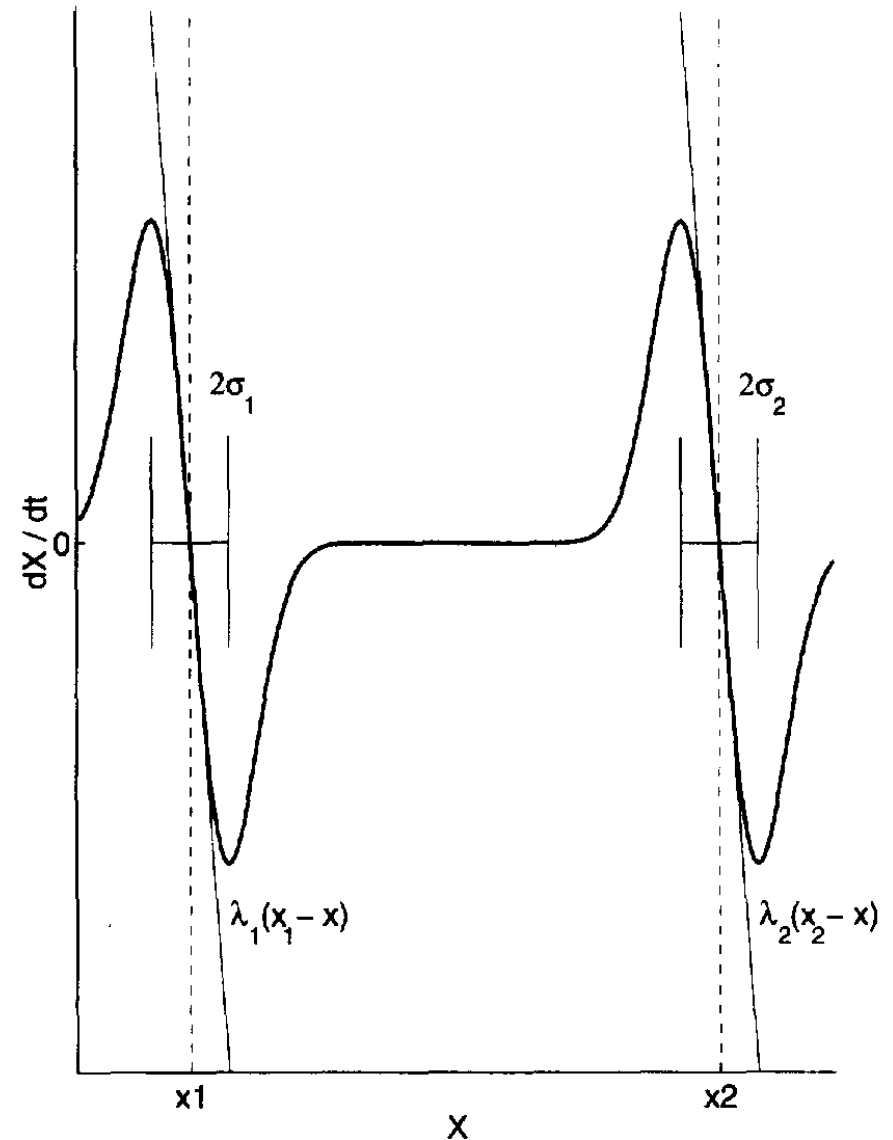


# Neural and behavioral architecture



# Integration by an attractor dynamics

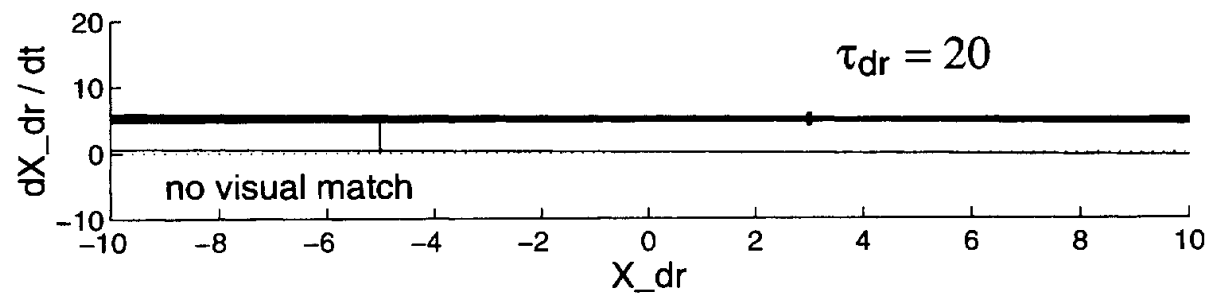
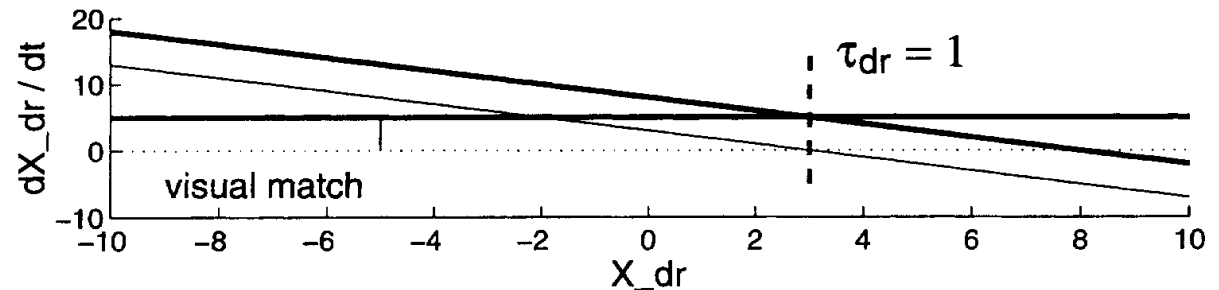
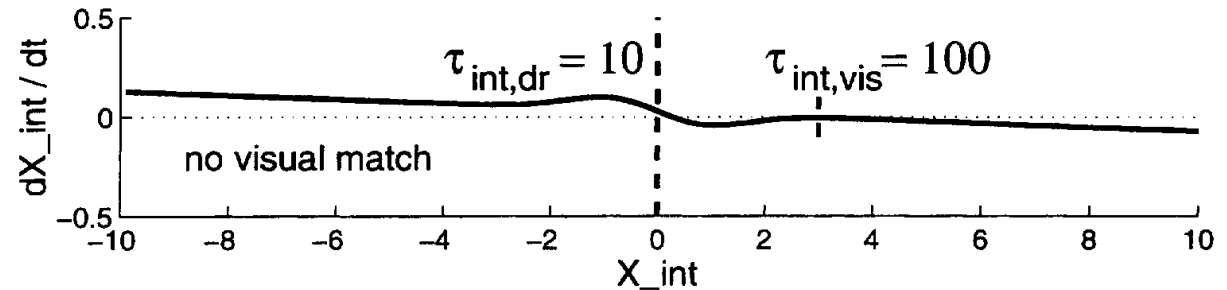
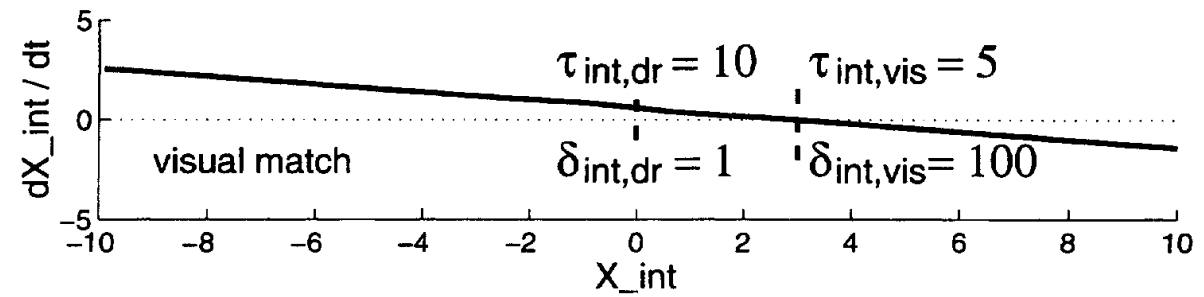
- every sensory estimate contributes a “force-let” to a dynamical system whose attractor is the estimate of ego-position ...
- for vision: space to rate code... removes the problem of normalization



# Recalibration from instability

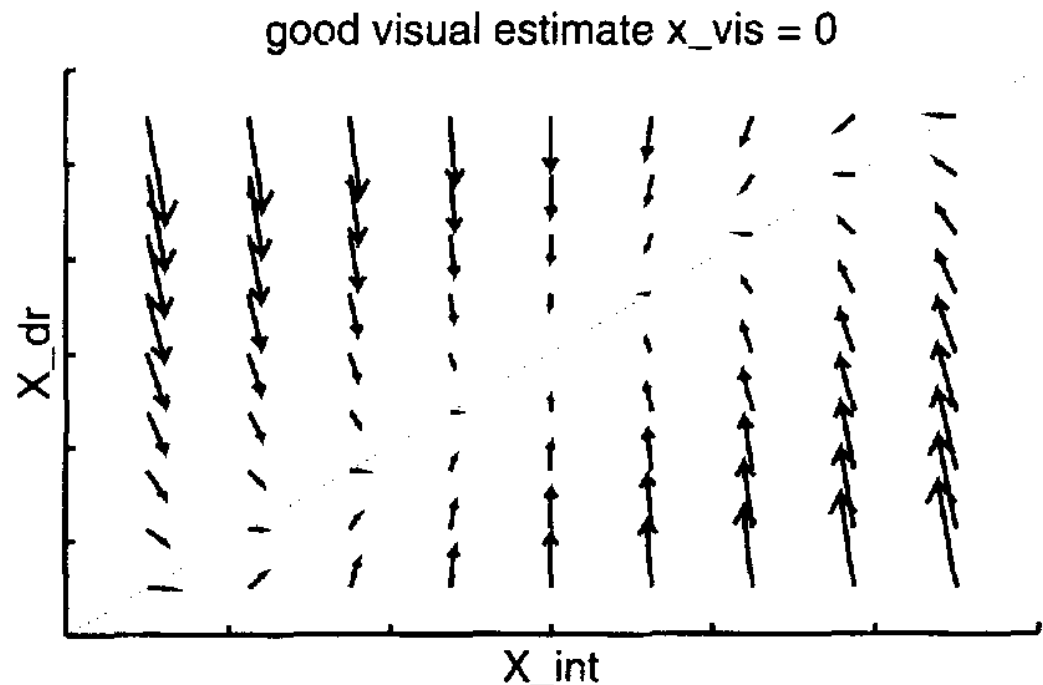
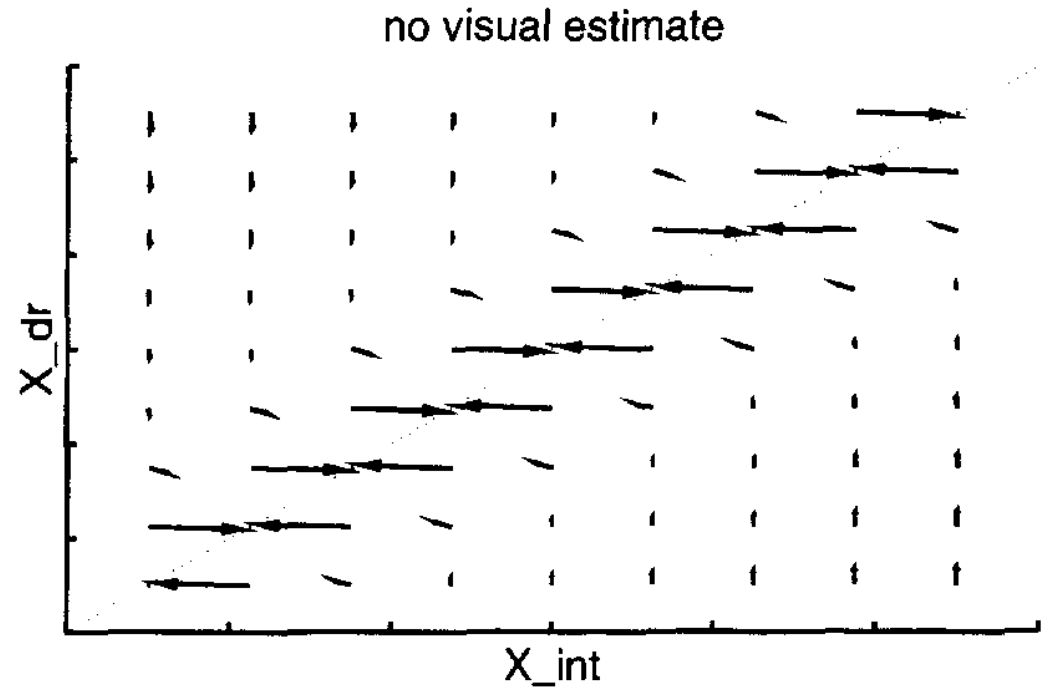
■ with visual match, a strong attractor force-let induces instability in which the estimate gets reset to the visually specified estimate

■ which resets the dead-reckoned estimate as well

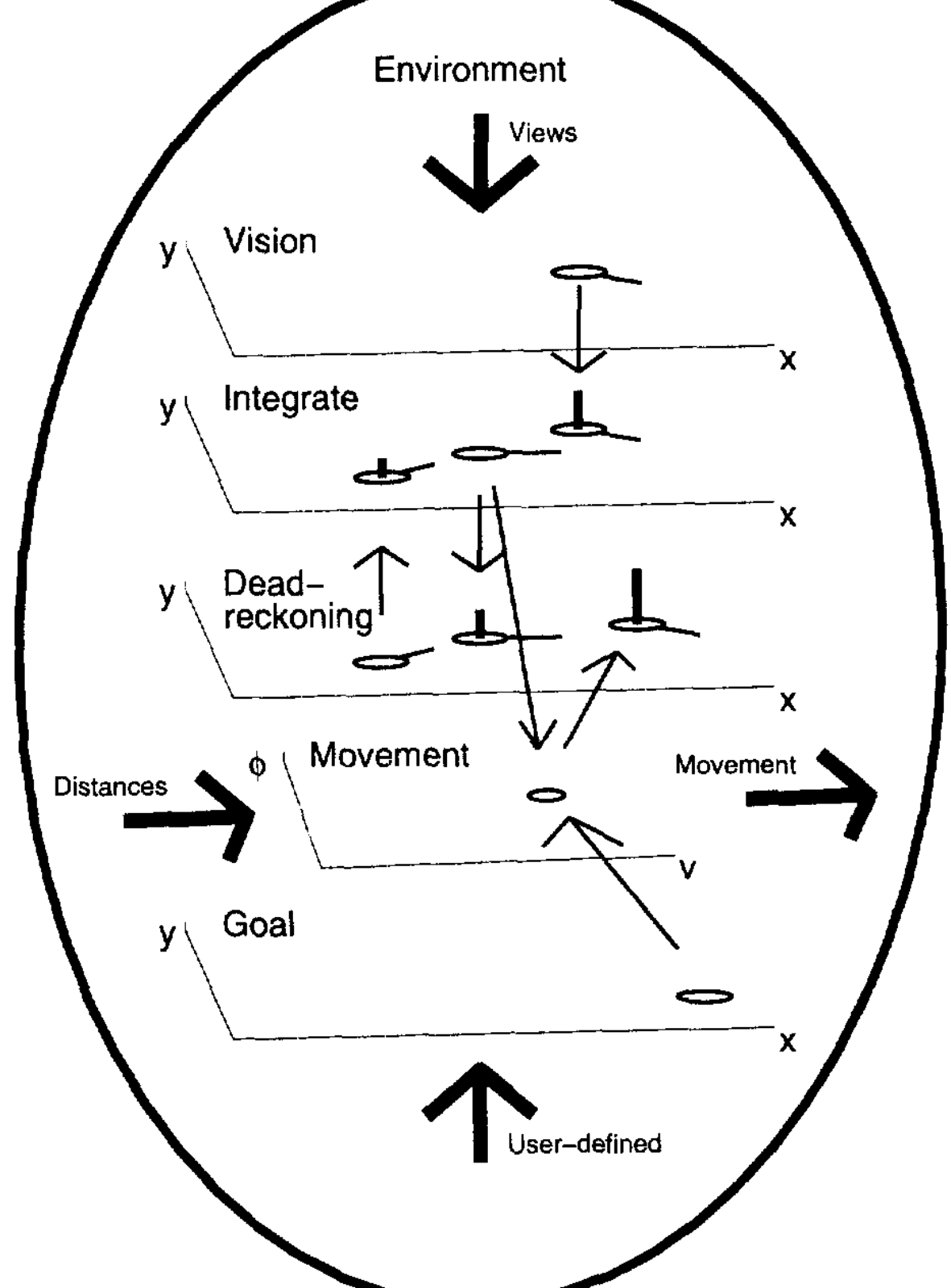


# Recalibration from instability

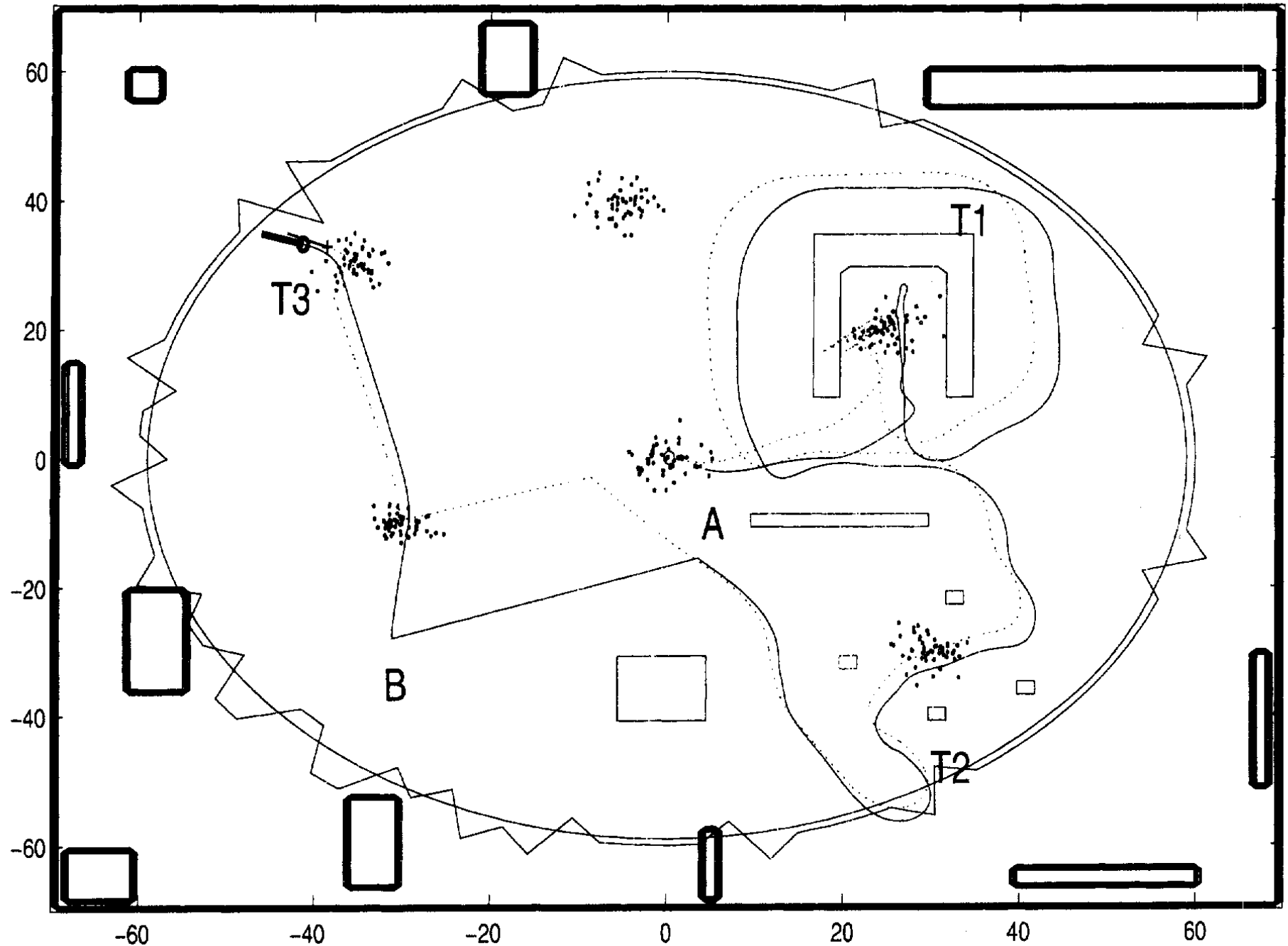
- with visual match, a strong attractor force-let induces instability in which the estimate gets reset to the visually specified estimate
- which resets the dead-reckoned estimate as well



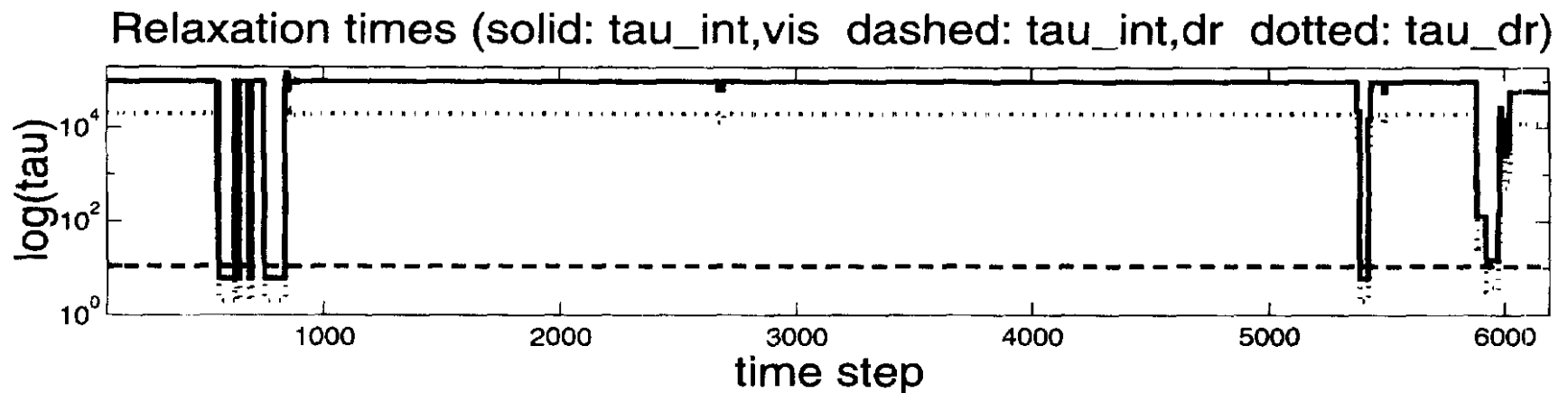
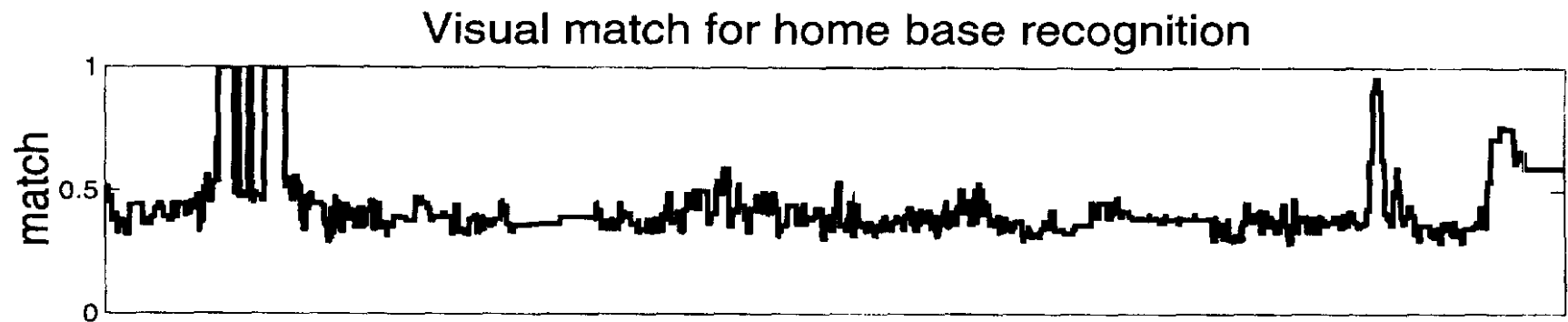
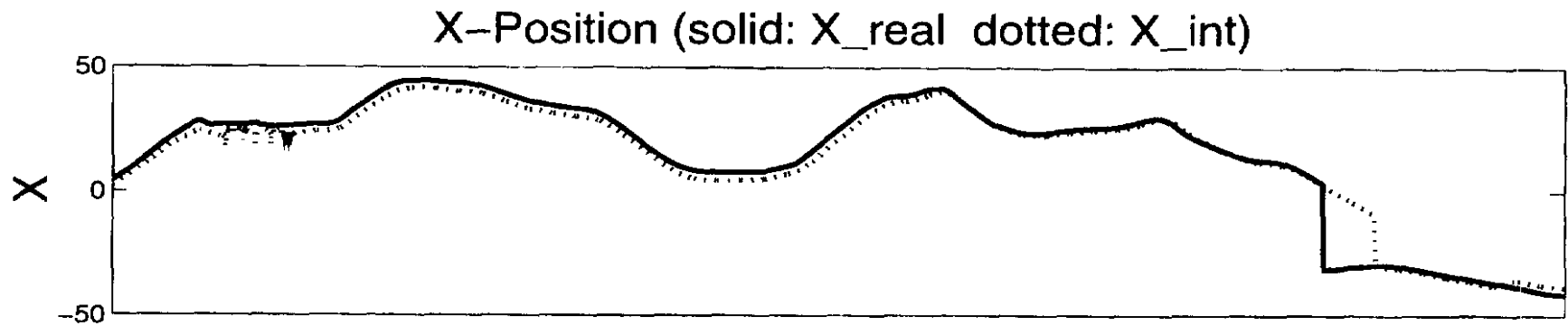
# Neural and behavioral architecture



# Integrating it all: dynamics all the



# a reset event



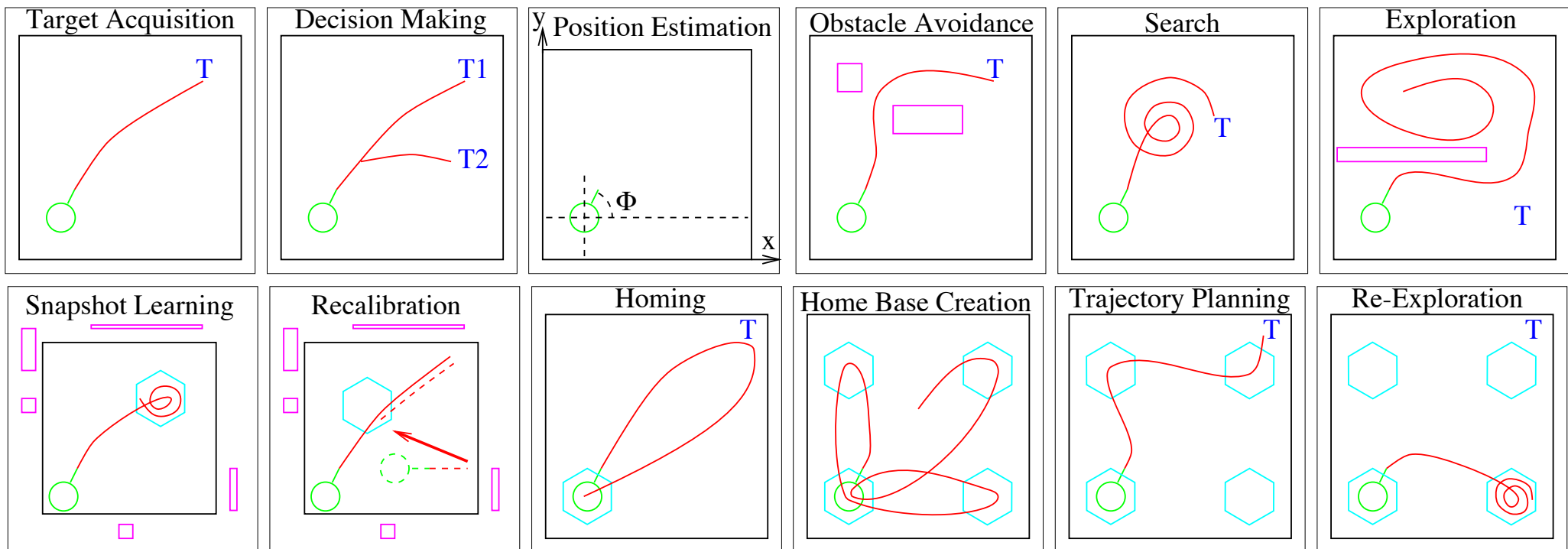


# Further development:

- complex behavioral organization
- robotic implementation

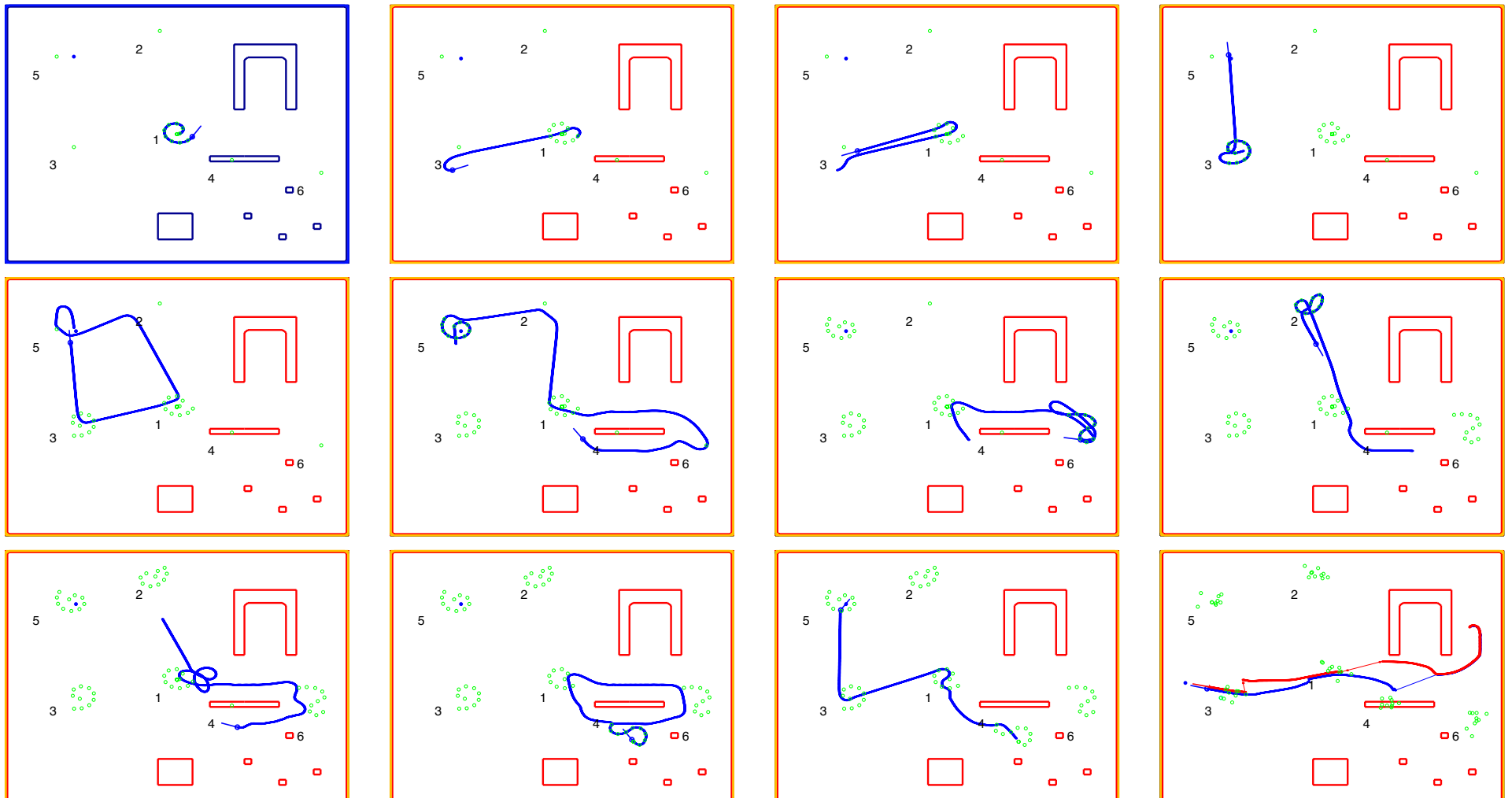
# Autonomous behavioral organization

■ neural dynamics organizes sequence of behaviors...



# Autonomous behavioral organization

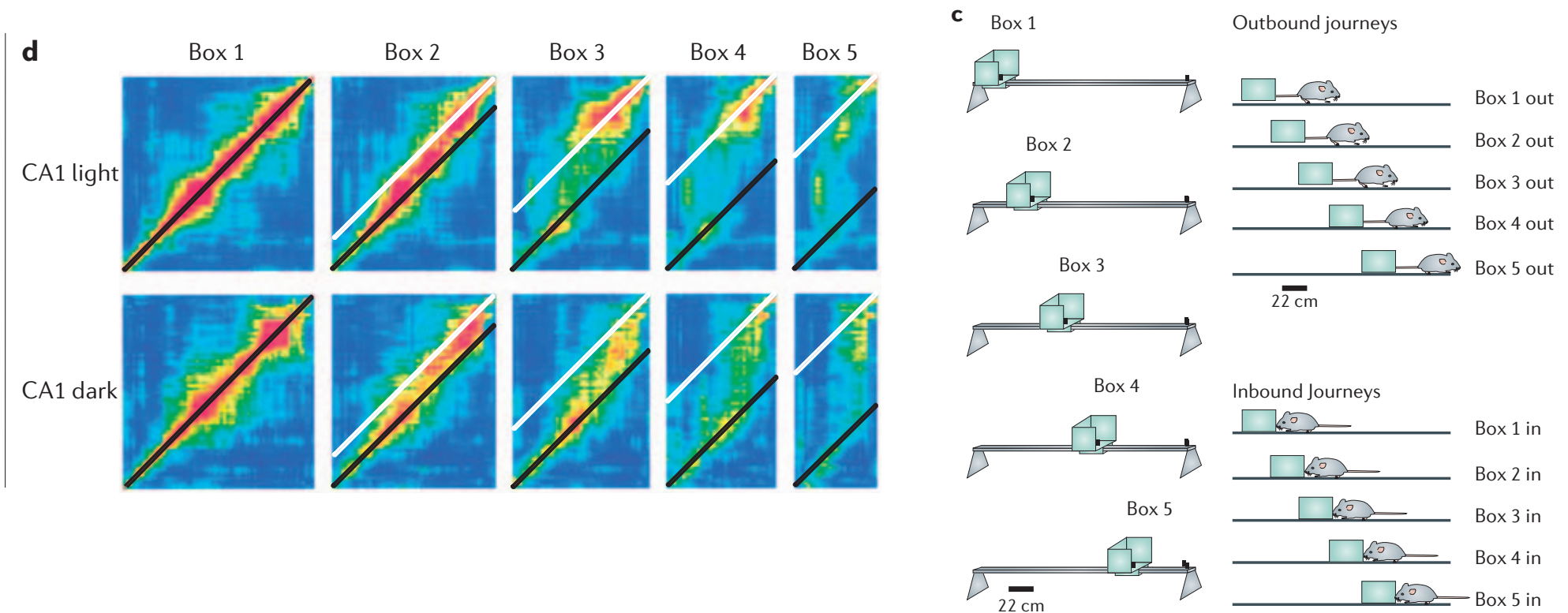
■ neural dynamics organizes sequence of behaviors...



# How neurally realistic is this?

# Neural mechanisms of navigation

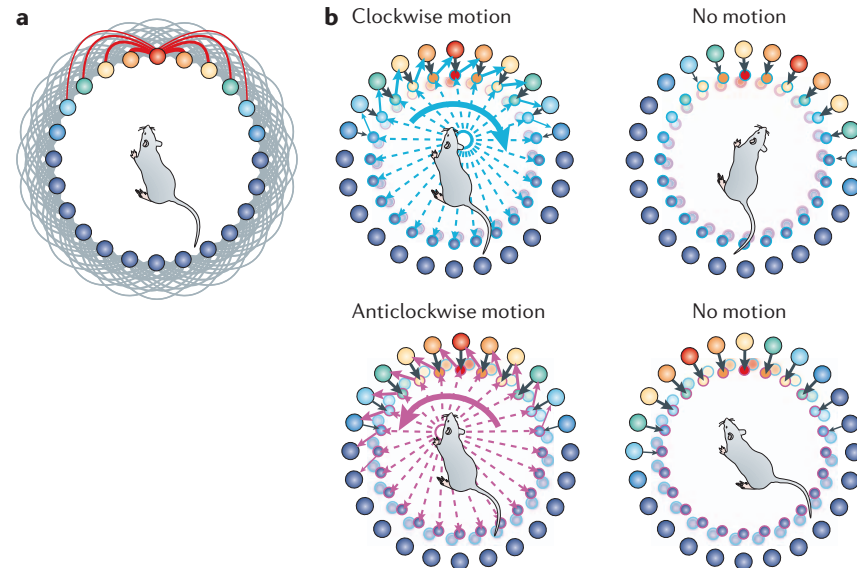
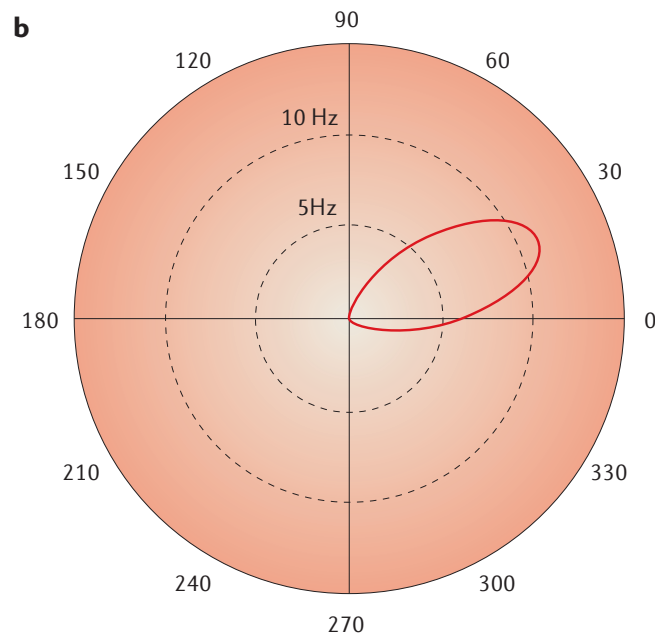
## ■ neural representation of path integration



[McNaughton et al., *Nature reviews neuroscience* 2006]

# Heading direction

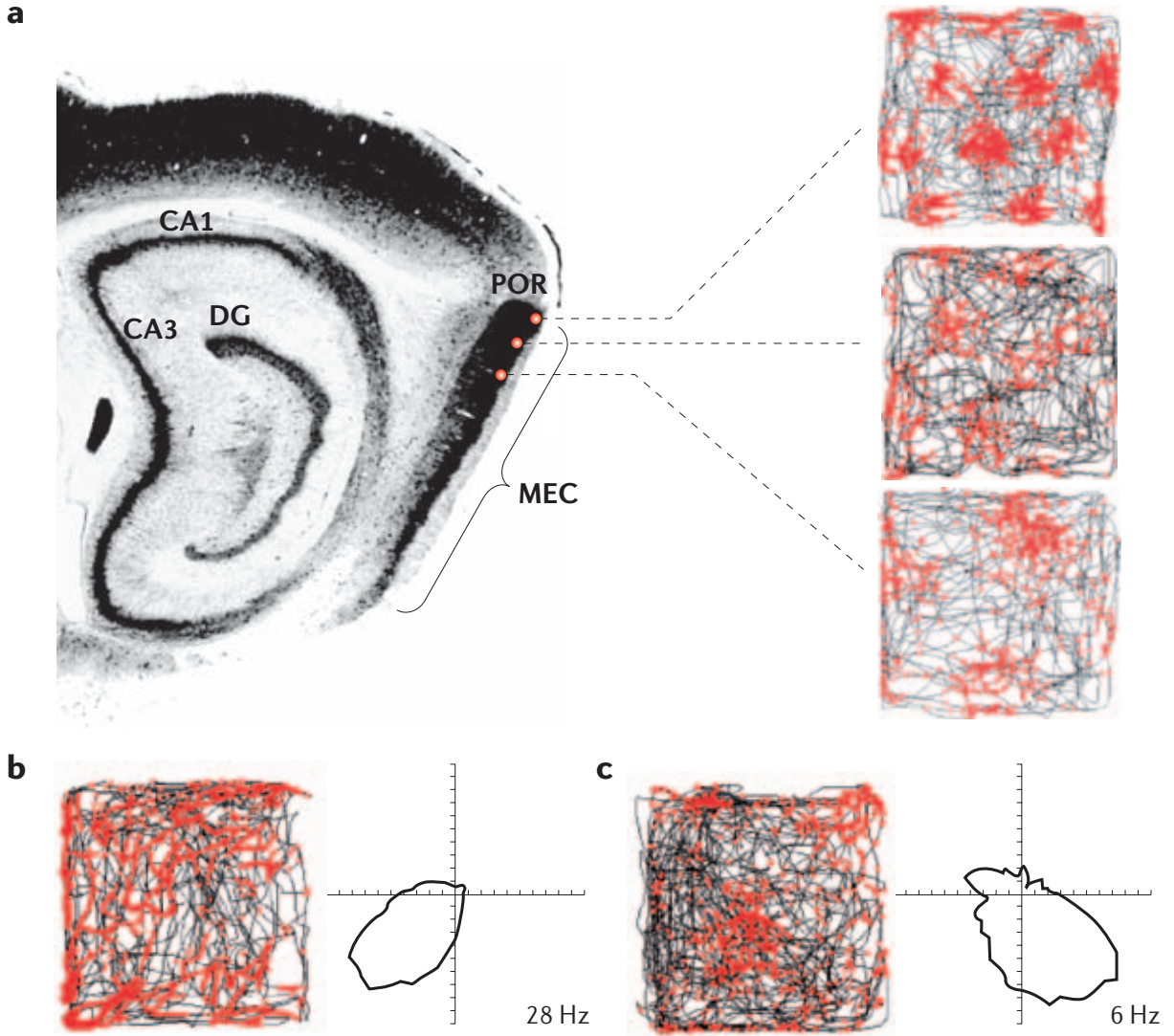
- Neural evidence for head-orientation cells... that function as heading direction representation
- Neural attractor dynamics (neural field) for heading direction



[McNaughton et al., *Nature reviews neuroscience* 2006]

# Place and grid cells

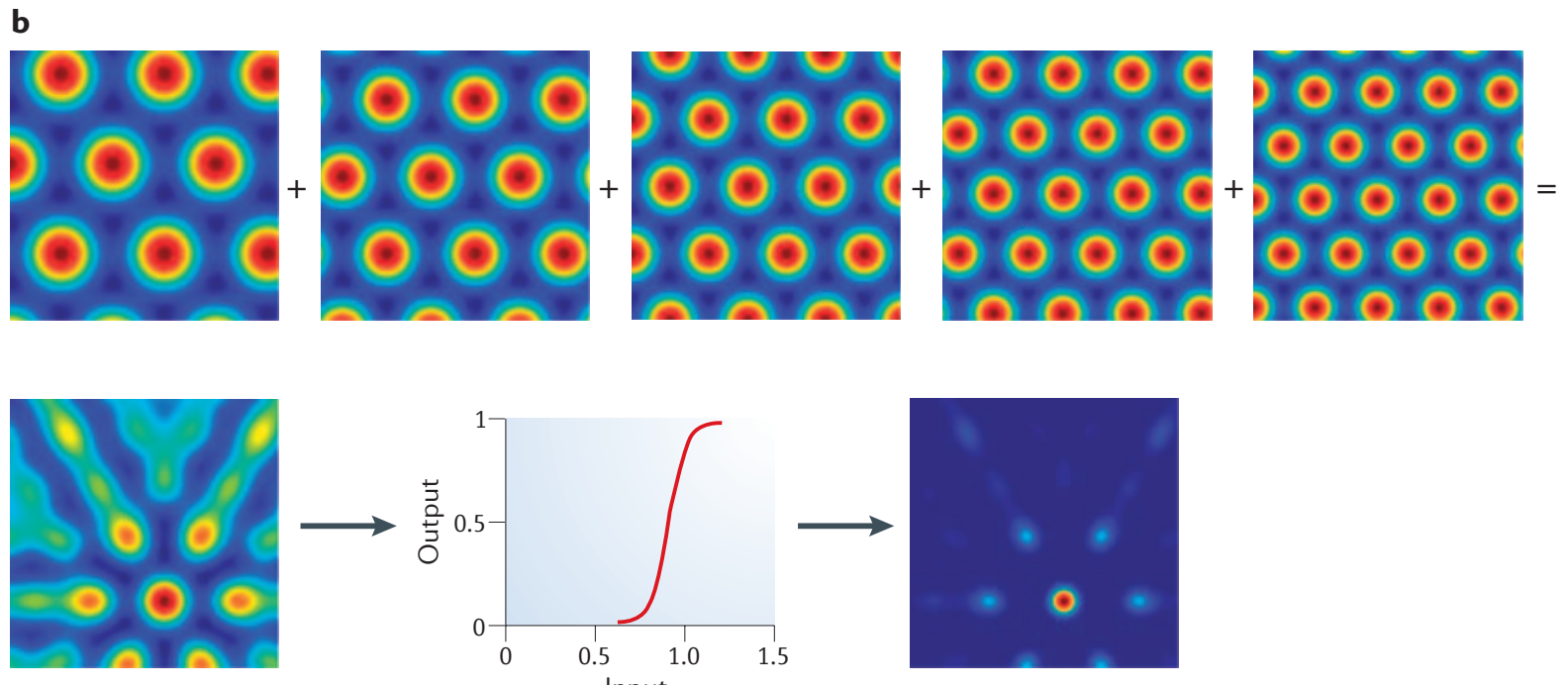
- neural representation of location in Hippocampus and Entorhinal Cortex



[McNaughton et al.,  
*Nature reviews  
neuroscience* 2006]

# Place and grid cells

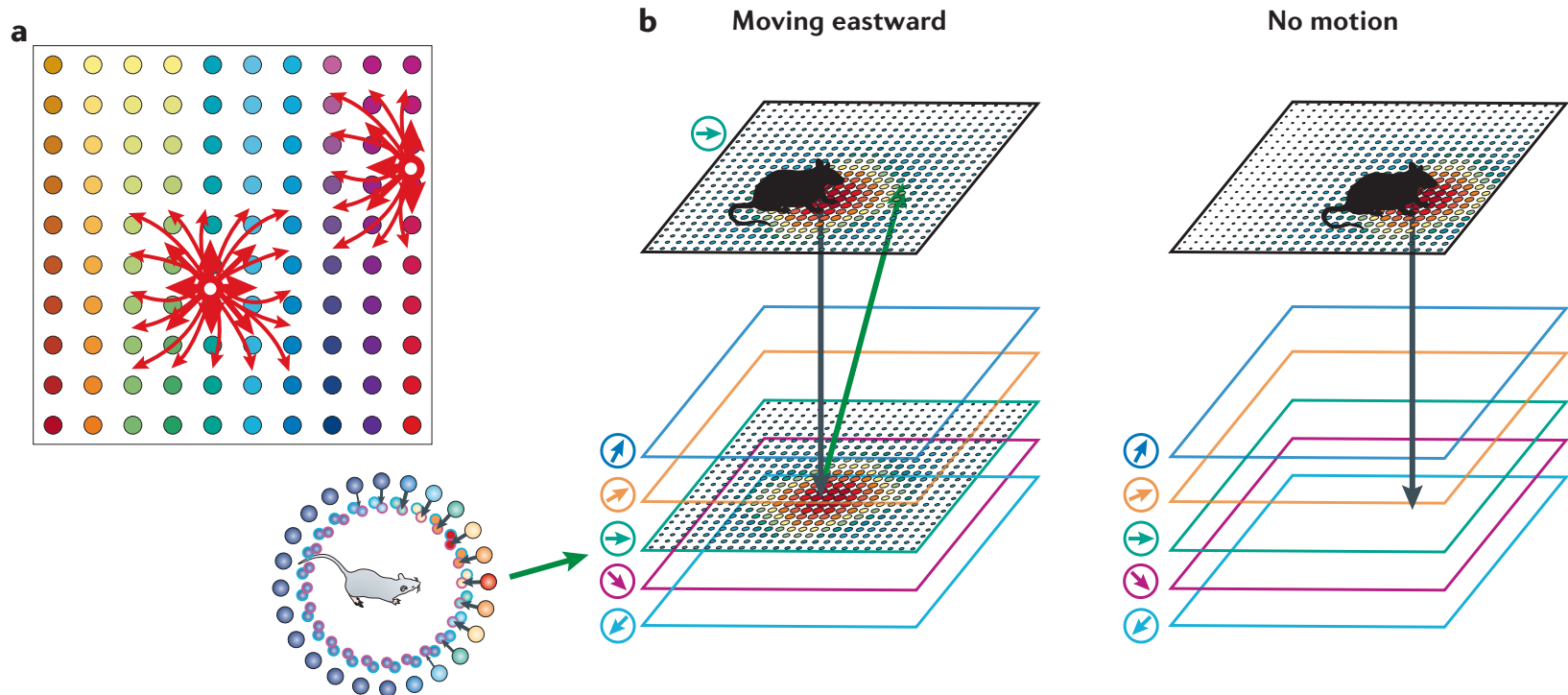
- support building a place representation by a neural field



[McNaughton et al.,  
*Nature reviews*  
*neuroscience* 2006]

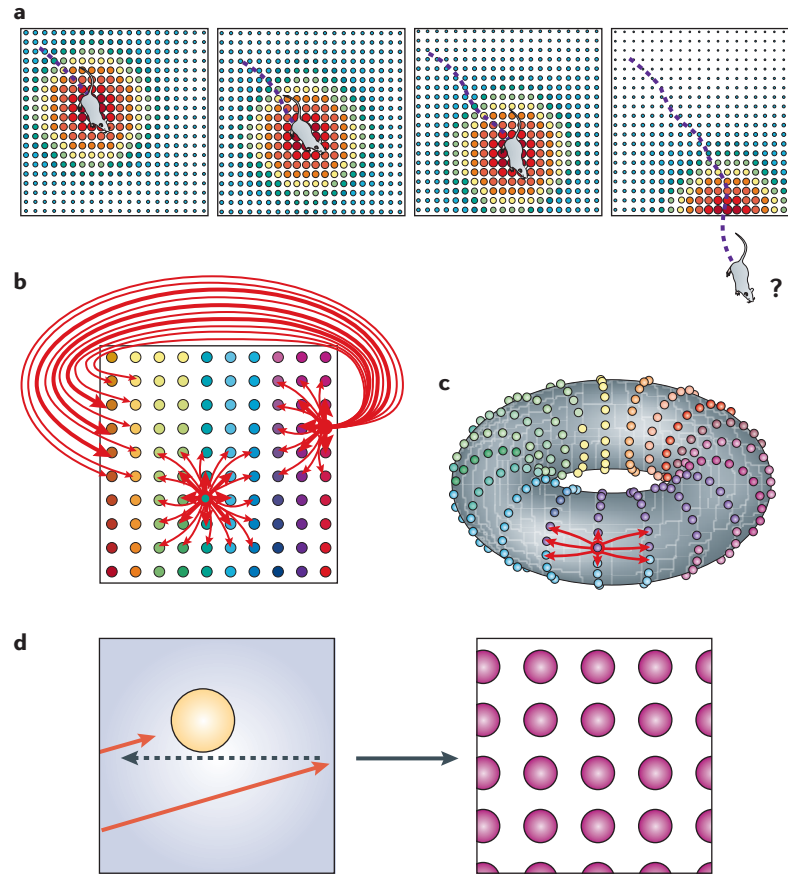


# Neural dynamics of path integration



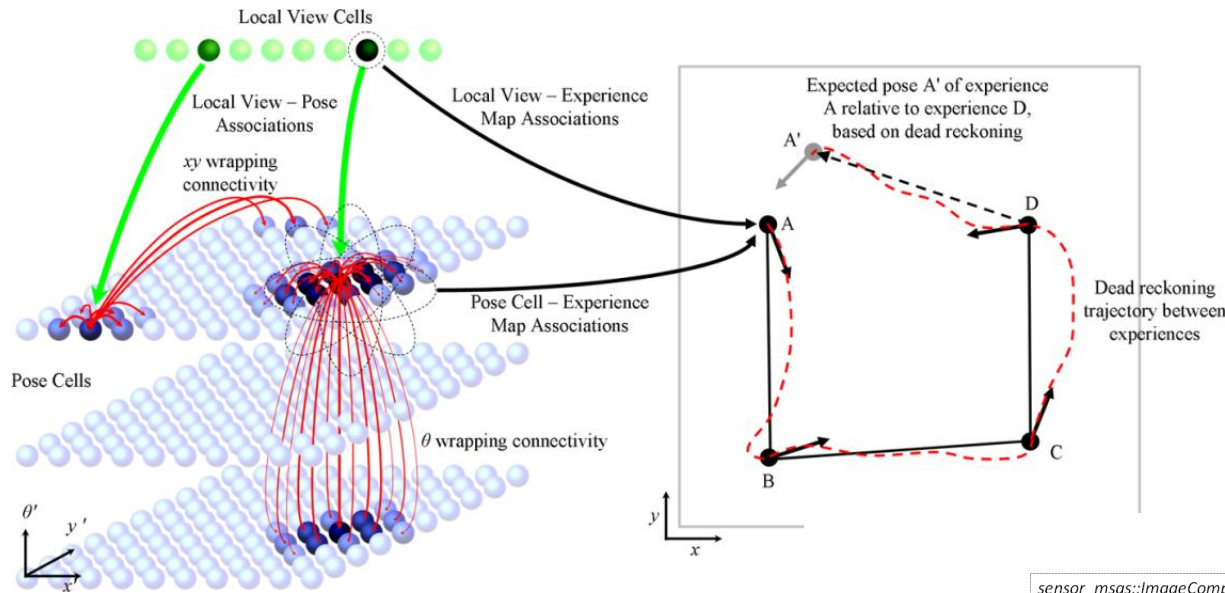
[McNaughton et al., *Nature reviews neuroscience* 2006]

# Neural dynamics of path integration

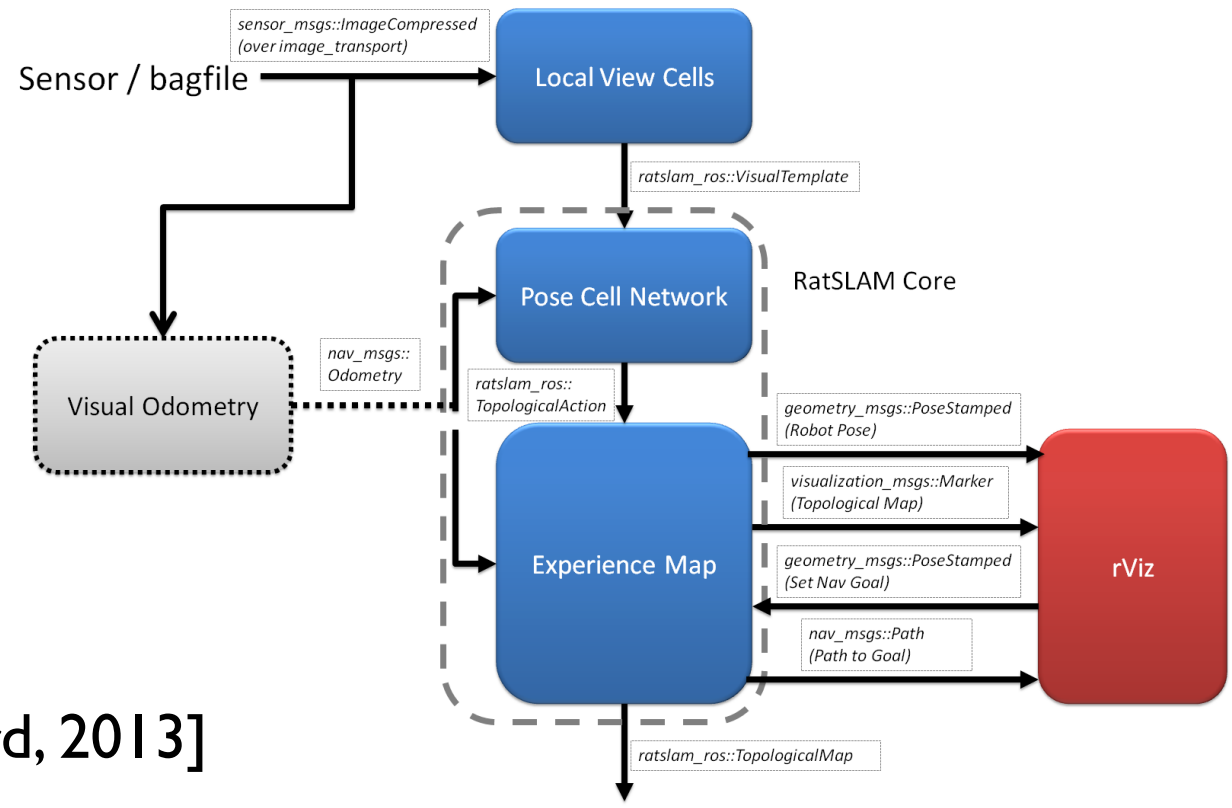


[McNaughton et al., *Nature reviews neuroscience* 2006]

# Neurally inspired technical solution

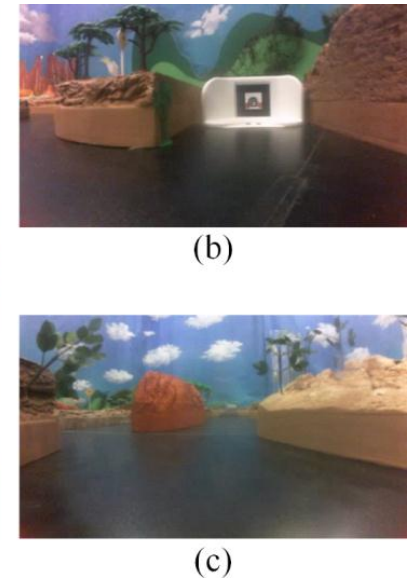
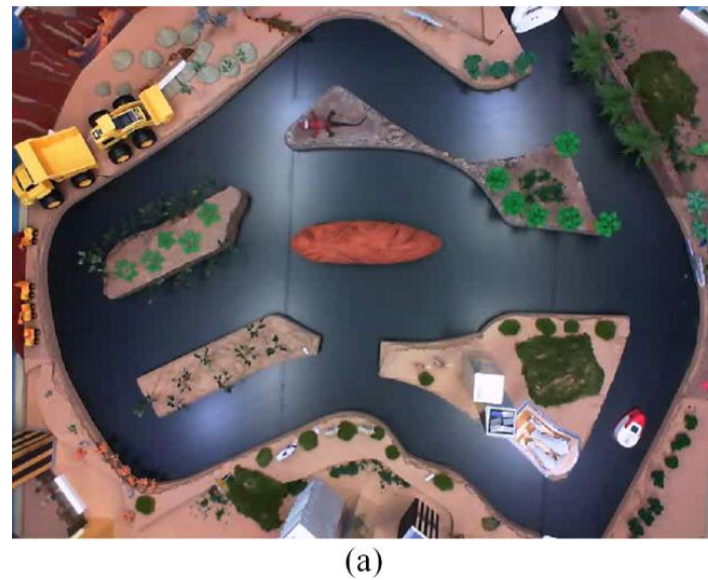
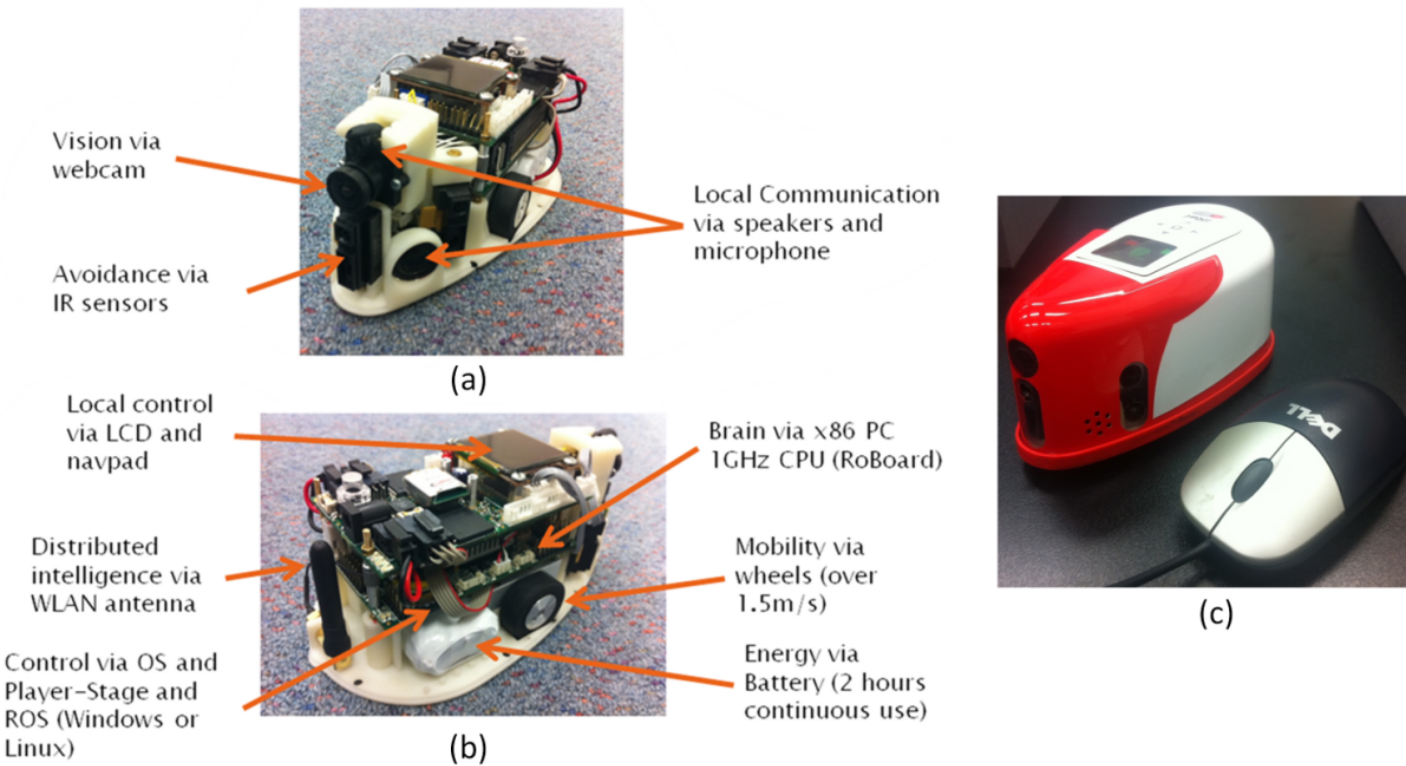


 **RAT-Slam**

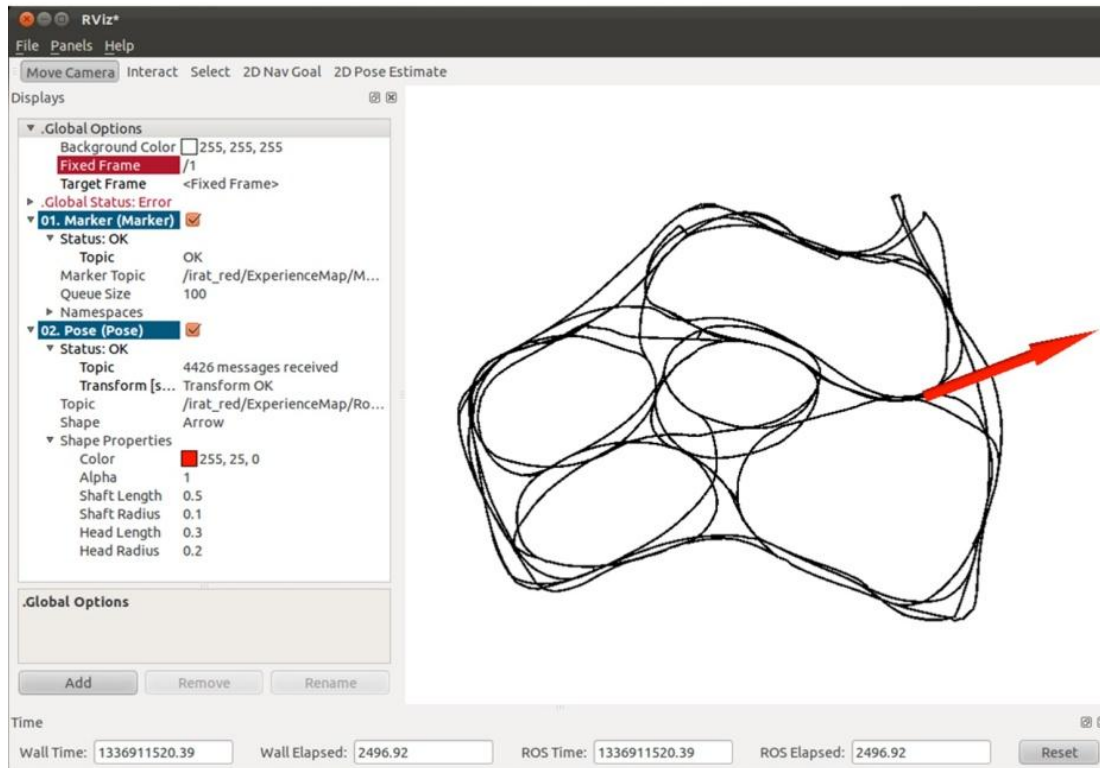


[Ball, Wyeth, Cork, Milford, 2013]

# RAT-Slam







# RAT-Slam



(a)



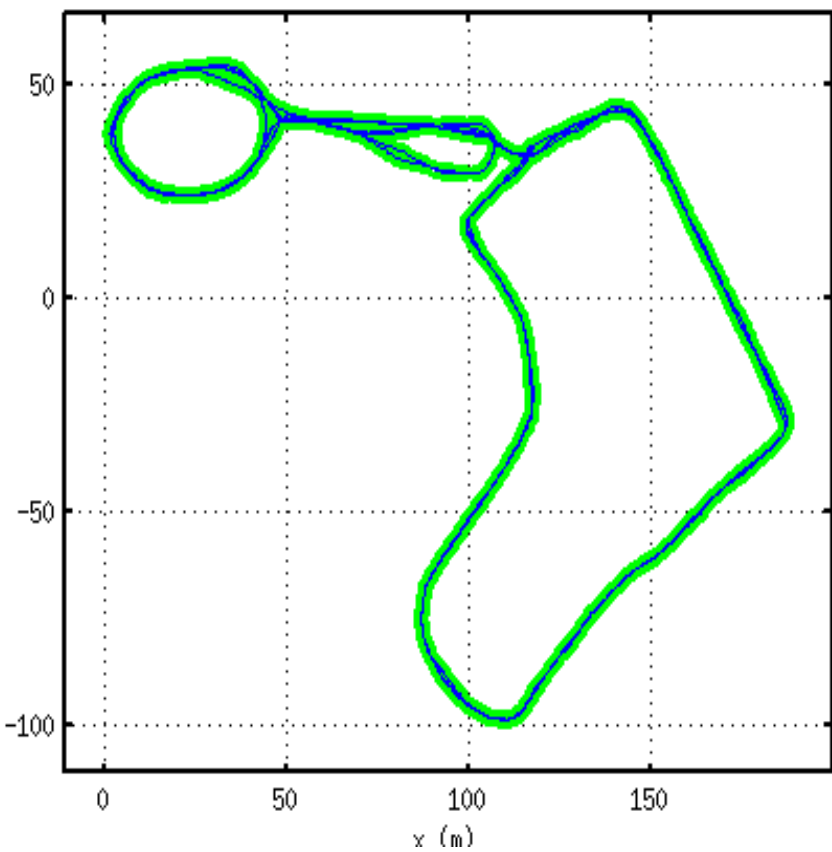
(b)



(c)

[Ball, Wyeth, Cork, Milford, 2013]

# RAT-Slam



(b)



[Ball, Wyeth, Cork, Milford, 2013]

# Event-based place recognition

■ spiking neural vision system...

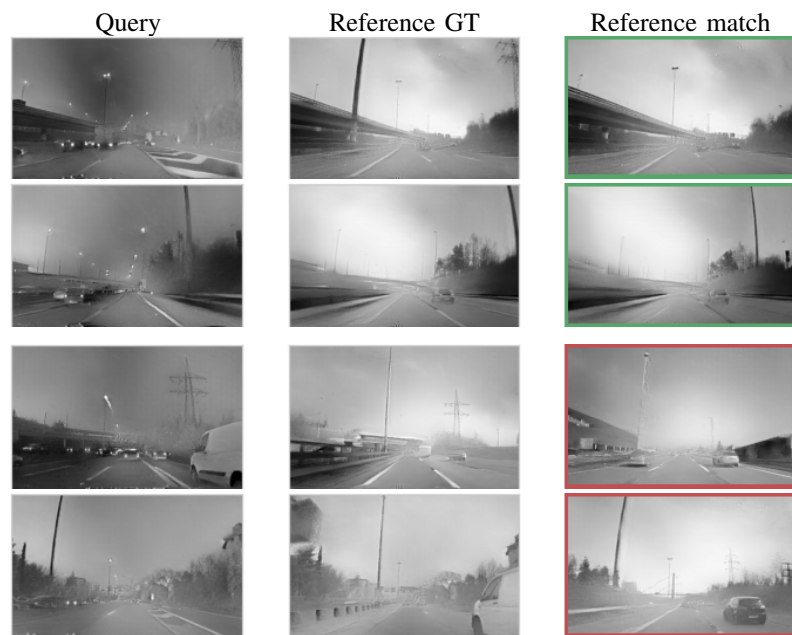
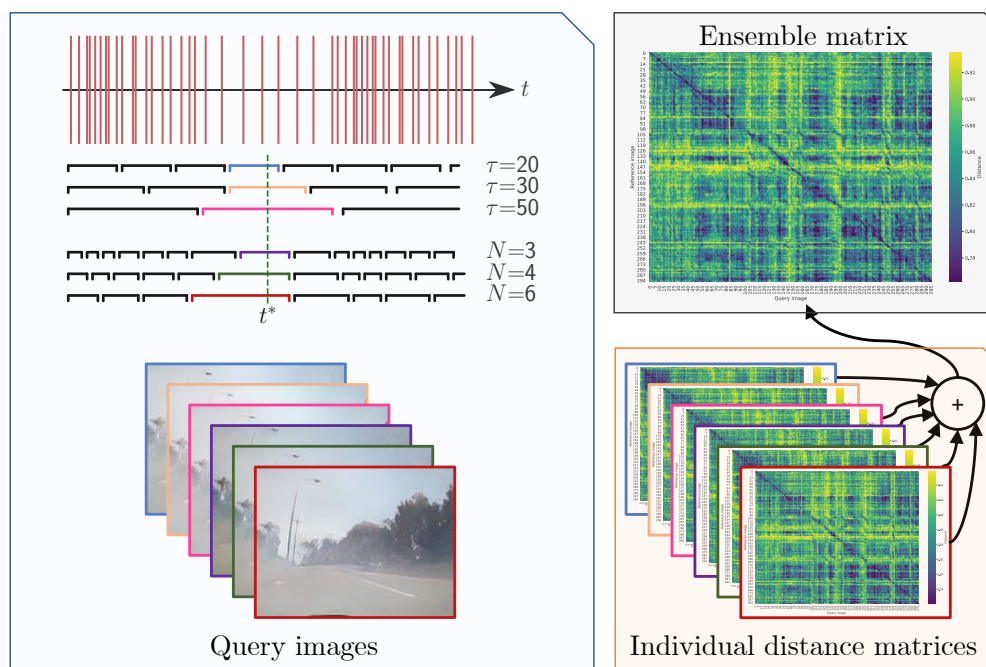
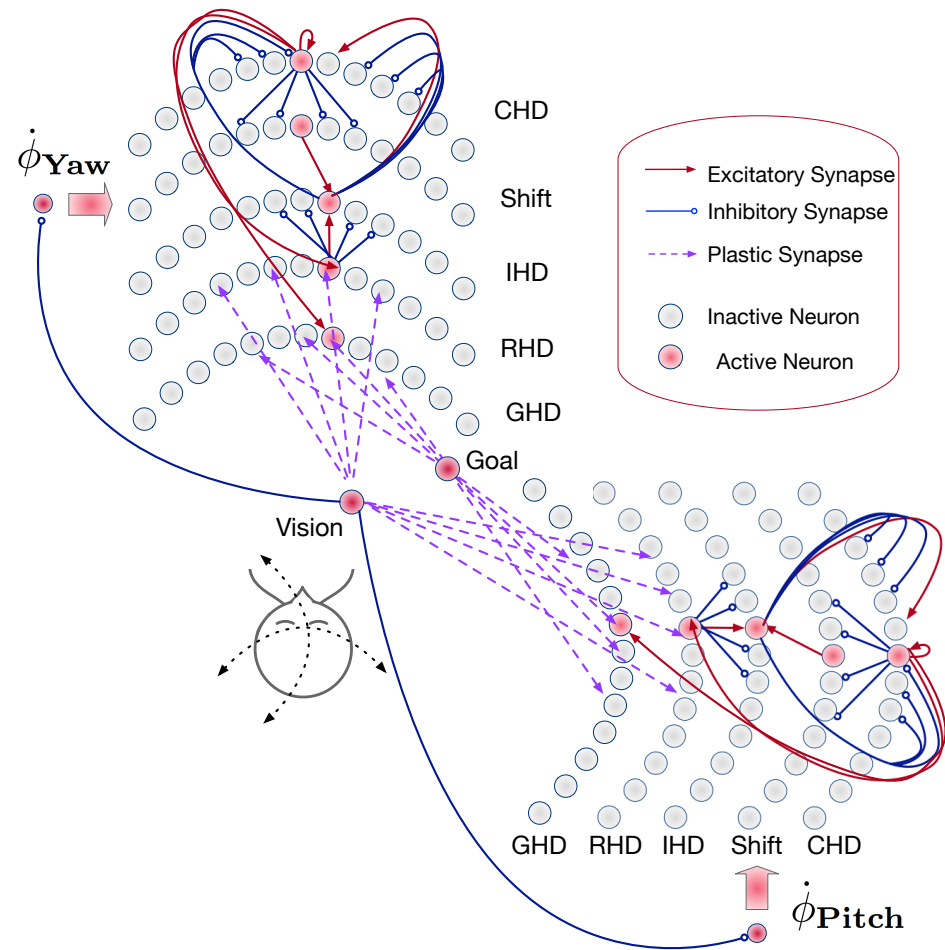


Fig. 8: Example matches of the ensemble and ground-truth (GT) matches on the DDD-17 dataset. Top two rows: success cases where the majority of individual methods failed. Bottom two rows: failure cases.

[Fischer Milford, 2020]

# Neuromorphic head-direction estimate

■ using DFT

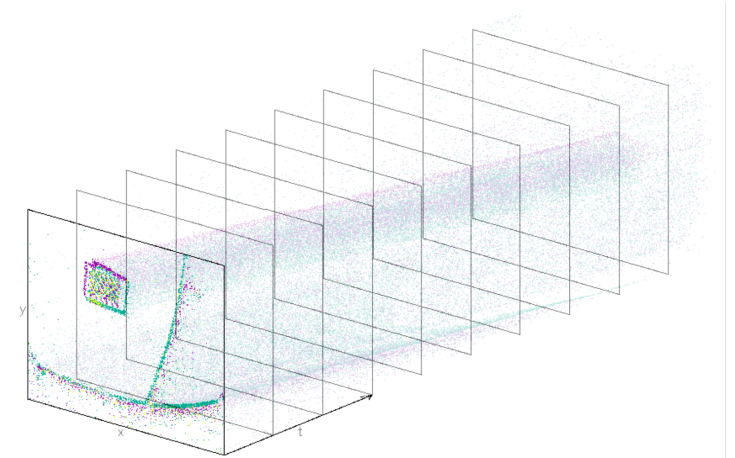
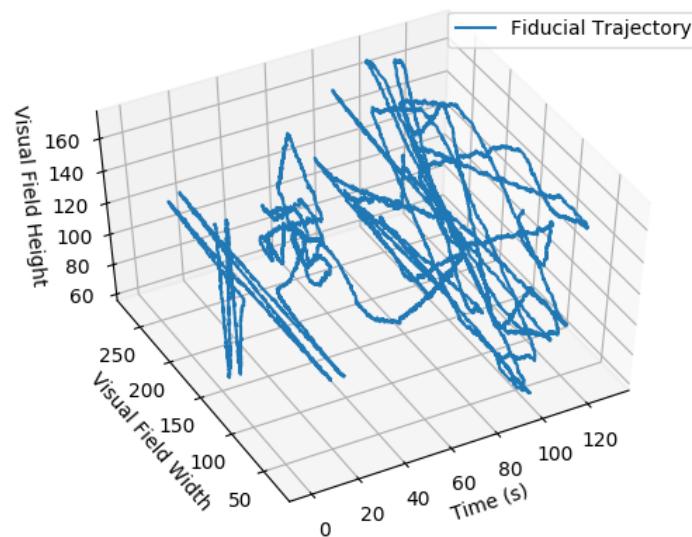
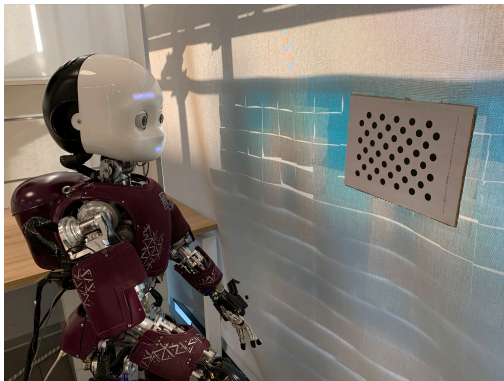


[Kreiser et al. Sandamirskaya, Frontiers 2019]



# Neuromorphic head-direction estimate

■ using DFT



[Kreiser et al. Sandamirskaya, Frontiers 2019]

# Conclusions

- the navigation problem entails both knowing where you are and how to go places
- navigation can be performed by behavioral and neural dynamics
- recalibration of location based on recognition ... can be view-based
- integration by (neural) dynamics ... in which space-time continuous processes... lead to discrete transitions at instabilities