## Higher-dimensional dynamics fields enable new cognitive function

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#### Dimensionality of fields

- all this was done primarily in fields defined over a single dimension...
- multi-dimensional fields are not per se fundamentally different....
- in particular, they have the same kind of dynamics as one-dimensional fields

#### example: retinal space

#### obviously two-dimensional



□ 0.4°



#### example: visual feature map

#### orientation-retinal location



#### example: visual feature maps

#### the neural field representation a single feature (e.g. orientation) as well as retinal location is at least three-dimensional

cannot be mapped onto cortical surfaces without cuts ...



## Dynamic fields of higher dimensionality

- I, 2, 3, 4... dimensions: peak/ blob states ...
- dynamics scale with dimensions









#### Nodes...

represent discrete categories by virtue of their coupling to feature fields/feedforward NN

typically embedded in populations of nodes that are inhibitorily coupled enabling selection among categories



#### Nodes...

may also play a specific role to organizes fields within architectures..

=> we'll address this when talking about sequences

Boost Node



## What do higher dimensional fields represent?

### Combining different feature dimensions

neurons tuned to multiple dimensions

e.g. receptive field + direction tuning

=> combines visual space and orientation

"anatomical" binding



[Hubel, Wiesel, 1962]

### Combining different feature dimensions

example: a joint representation of color and visual space "binds" these two dimensions



#### Extract bound features

- project to lowerdimensional fields
- by summing along the marginalized dimensions
- (or by taking the softmax)



#### Assemble bound representations

#### project lower-dimension field onto higherdimensional field as "ridge input"



#### Assemble bound representations



### Assemble bound representations

- binding problem: multiple ridges along lower-dimensional space lead to a correspondence problem
- => assemble one bound object at a time...
- => sequentiality bottleneck!



## Search

- ridge input along one dimension extracts
  from bound
  representation matching
  objects
- other dimensions of those objects can then be extracted

e.g. visual search



#### Visual search



[Grieben et al. Attention, Perception & Psychophysics 2020; CogSci 2021]









#### Visual search



[Grieben et al. Attention, Perception & Psychophysics 2020]

## Binding

"anatomical" binding does not scale

binding through space

Iocalist vs. distributed representations

learning

## Scaling feature dimensions

=>

- 2 spatial dimensions
- depth 🛋
- orientation
- color
- texture
- movement direction
- size

etc...

- e.g. 8 dimensions
- 100 neurons per dimension
  - $10^{2*8} = 10^{16}!$
  - more than there are in the entire brain!
  - => only small sets of feature dimensions can be bound "anatomically"

#### Localist vs. distributed

- scaling problem arises in localist representations
- distributed representations scale better



- but: localist representations enable stable states and thus cognitive function: detection, selection, working memory, (and sequence generation)
- that is why DFT sticks to the costly localist picture

#### Localist vs. distributed

 Hopfield networks have attractors for distributed representations, but these (and the synaptic weights) are specific to each memorized pattern



so the Hopfield networks lack flexibility that enables cognition...

## Binding through space

- many 3 to 4 dimensional feature fields
- all of which share the one dimension: visual space (~all neurons have receptive fields)
- bind through space à la Feature Integration Theory (Treisman)



[Grieben et al. Attention, Perception & Psychophysics 2020]

## Binding through space



[Grieben et al. Attention, Perception & Psychophysics 2020]





[Schneegans et al., Ch 8 of DFT Primer, 2016]



[Schneegans et al., Ch 5 of DFT Primer, 2016]



# Binding through space => sequential bottleneck

- binding through space must occur one time at a time..... to avoid binding problem
- => the sequential processing bottleneck may originate from this



# Coordinate transforms and binding through space

coordinate transforms: 2 by 2 spatial dimensions

perform the coordinate transform in space only!

no need to transport the feature values, which can be filled in by binding through space



[Schneegans, Schöner, 2012]

#### Generalization to other binding agents

than space...

a binding agent must be a shared neural dimension...

can be discrete/categorical in nature

e.g. can be an ordinal dimension, an "index", a "label"

=> special lecture by Daniel Sabinasz on grounded cognition

#### Coordinate transforms

are fundamental element to sensory-motor cognition

[but critical also to mental operations!]

example: reaching is guided by bodycentered, not by retinal visual representation



#### Coordinate transforms

are fundamental element to sensory-motor cognition

[but critical also to mental operations!]

example: movement
parameters are extracted by
representing movement
target in coordinates
centered in the initial
position of the hand



#### Coordinate transforms

are fundamental element to sensory-motor cognition

[but critical also to mental operations!]

worked example: from retinal to head-centered/ body-centered frame



- transformation depends on the gaze angle = steering dimension
- need a bound neural representation of
  - retinal space
  - 📕 gaze angle
- obtained from ridge/slice input to bind these
- project to body space













Retina => body space



Spatial remapping during saccades



[Schneegans, Schöner Biological Cybernetics 2012]

## Accounts for predictive updating

[neural data: Duhamel, Colby, Goldberg, 1992, LIP]



[model: Schneegans, Schöner Biological Cybernetics 2012]





#### Scaling



[Schneegans, Schöner, 2012]

## Summary: higher dimensions

representing different kinds of dimensions within a higher-dimensional field offers new (cognitive) functions

📕 binding

search

coordinate transforms