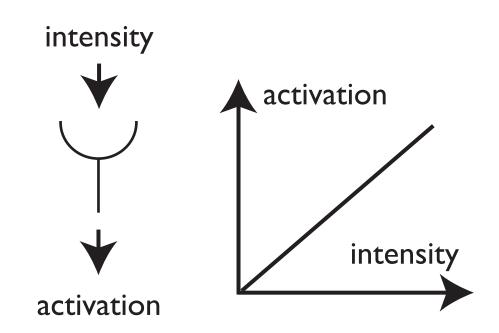
## Neural Dynamics

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## Sensors

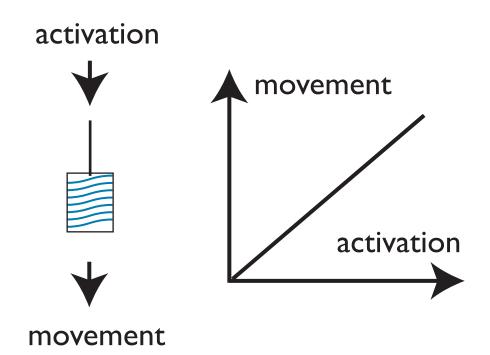
- transform a physical intensity into a neural activation
- intensity: light, sound, displacement
- neural activation: membrane potential, spike rate



## Motors

#### transform activation into physical action

… muscles

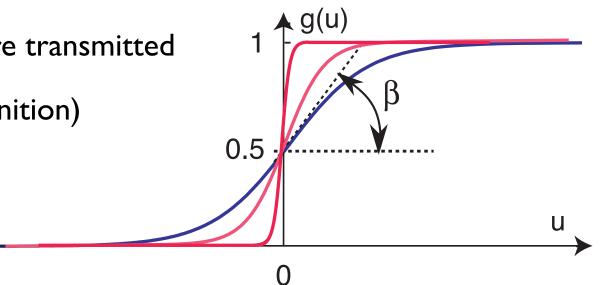


## What is "activation"?

- activation is an abstraction of the state of neurons, defined relative to sigmoidal threshold function
  - Iow levels of activation are not transmitted (to other neural systems, to motor systems)

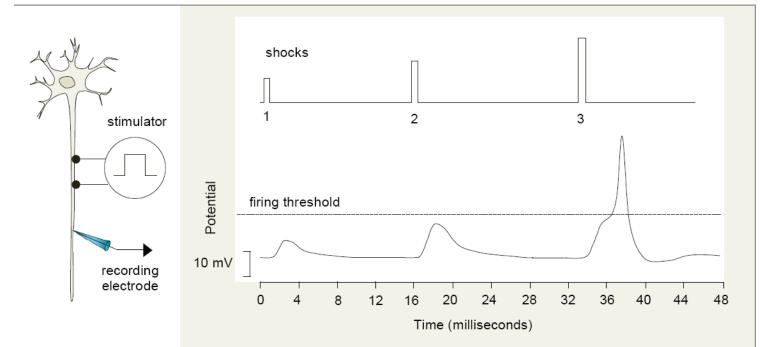
high levels of activation are transmitted

threshold at zero (by definition)



# Origin of the activation concept in neurophysics

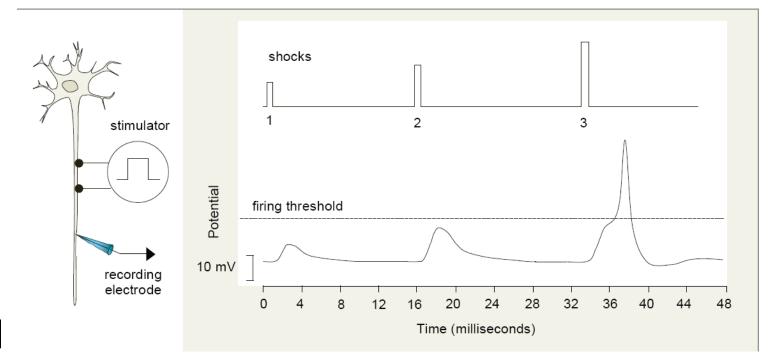
activation, u, as a real number that reflects the (population) membrane potential



[from: Tresilian, 2012]

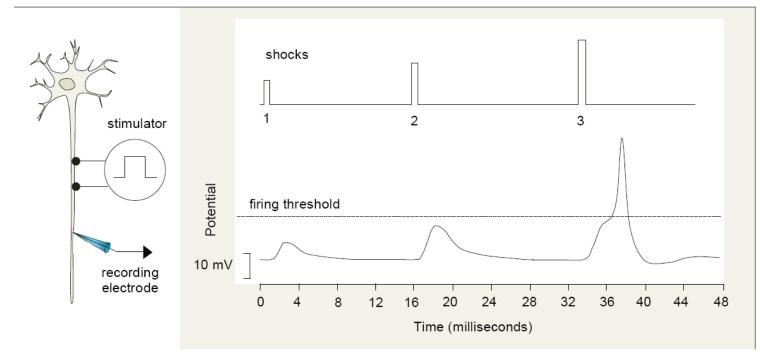
 $\blacksquare$  u(t) evolves as a dynamical system, characterized by a time scale,  $\tau \approx 10 \mathrm{ms}$ 

 $\tau \dot{u}(t) = -u(t) + h + \operatorname{input}(t)$ 



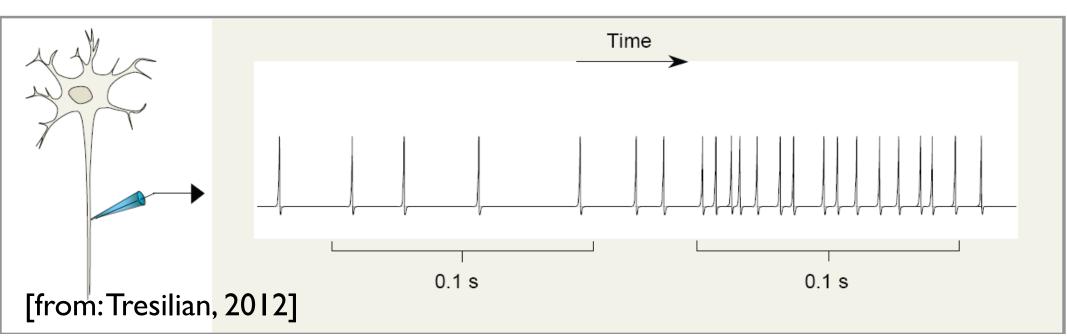
[from: Tresilian, 2012]

- spiking when membrane potential exceeds threshold....
- spike train is transmitted to downstream neurons

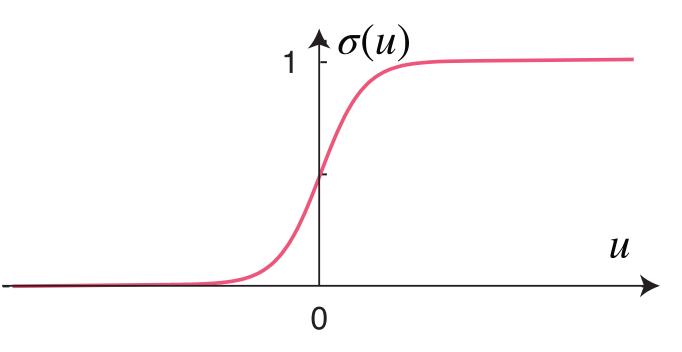


[from: Tresilian, 2012]

activation captures different firing rates in a small population...



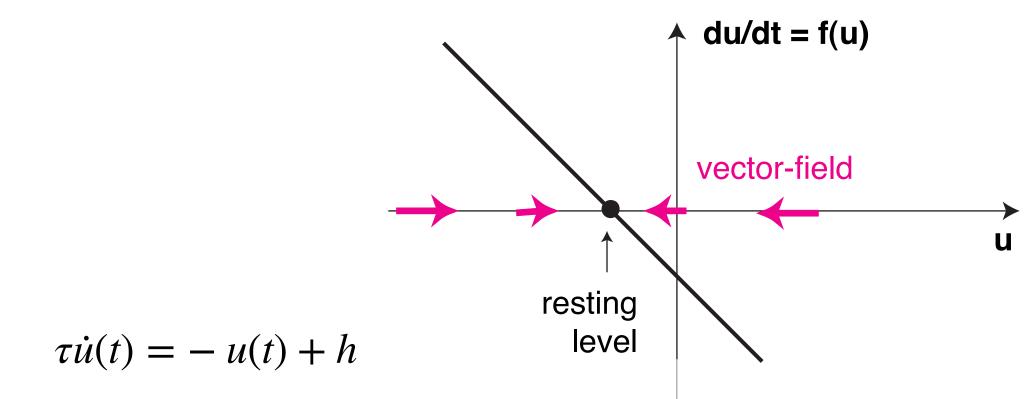
in neural dynamics, the spiking mechanism and associated firing rate is replaced by a statistical (population) description: threshold function



## Neural dynamics

dynamical system: the present predicts the future

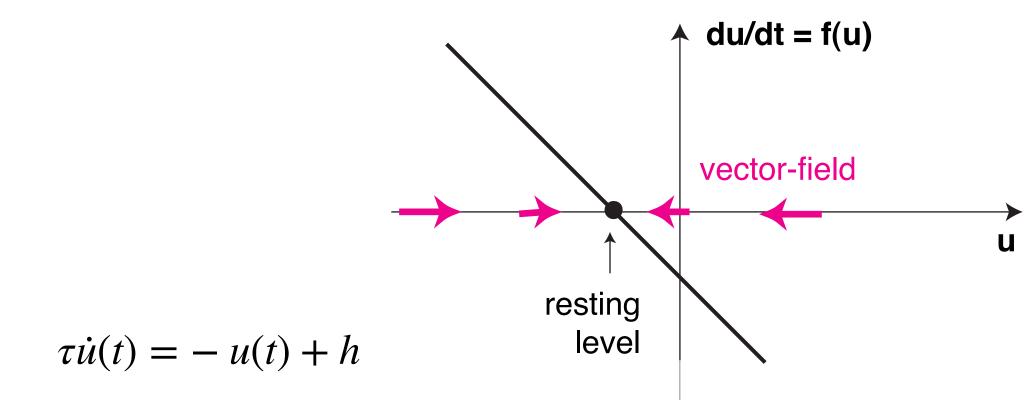
given a initial level of activation, u(0), the activation, u(t), at times t>0 is uniquely determined



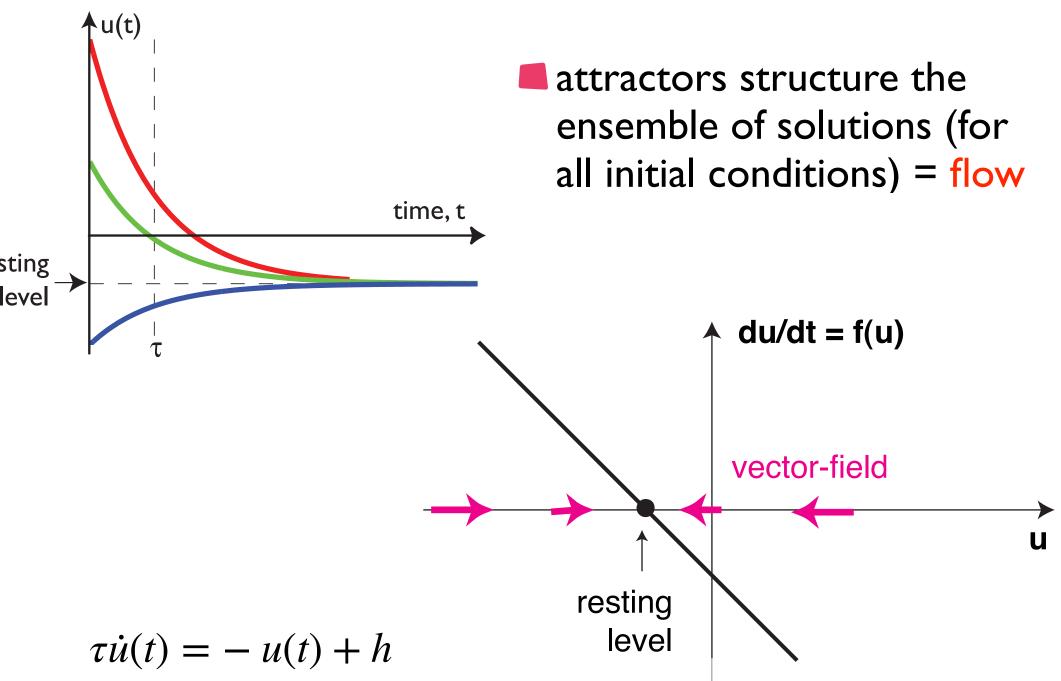
## Neural dynamics

**fixed point** = constant solution (stationary state)

stable fixed point = attractor: nearby solutions converge to the fixed point



## Neural dynamics



## Neuronal dynamics

in neural dynamics, inputs are contributions to the rate of change

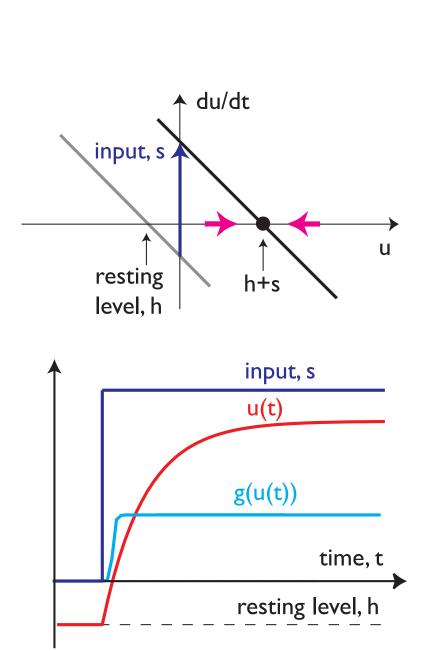
positive: excitatory

negative: inhibitory

=> shifts the attractor

=> activation tracks this shift due to stability

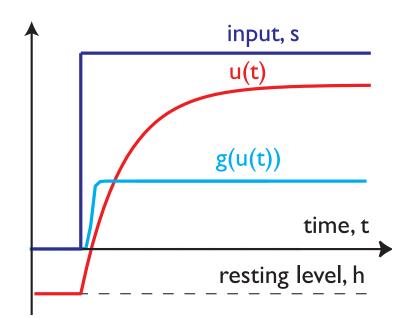
$$\tau \dot{u}(t) = -u(t) + h + s(t)$$



## Neuronal dynamics

- what is transmitted is  $\sigma(u(t))$
- (labelled g(t) in the book and in some figures)
- neural dynamics as a lowpass filter of time varying input
- = input-driven solution

$$\tau \dot{u}(t) = -u(t) + h + s(t)$$

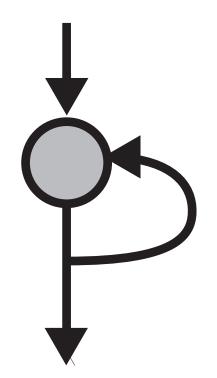


## => simulation

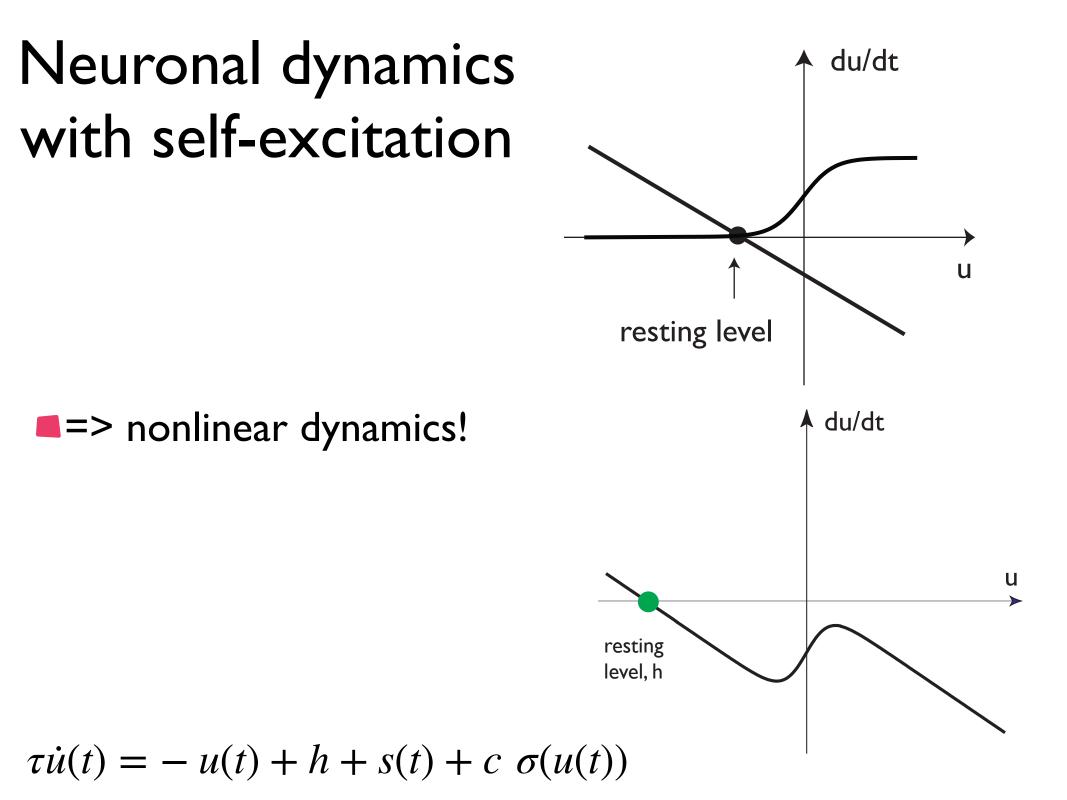
## Neuronal dynamics with self-excitation

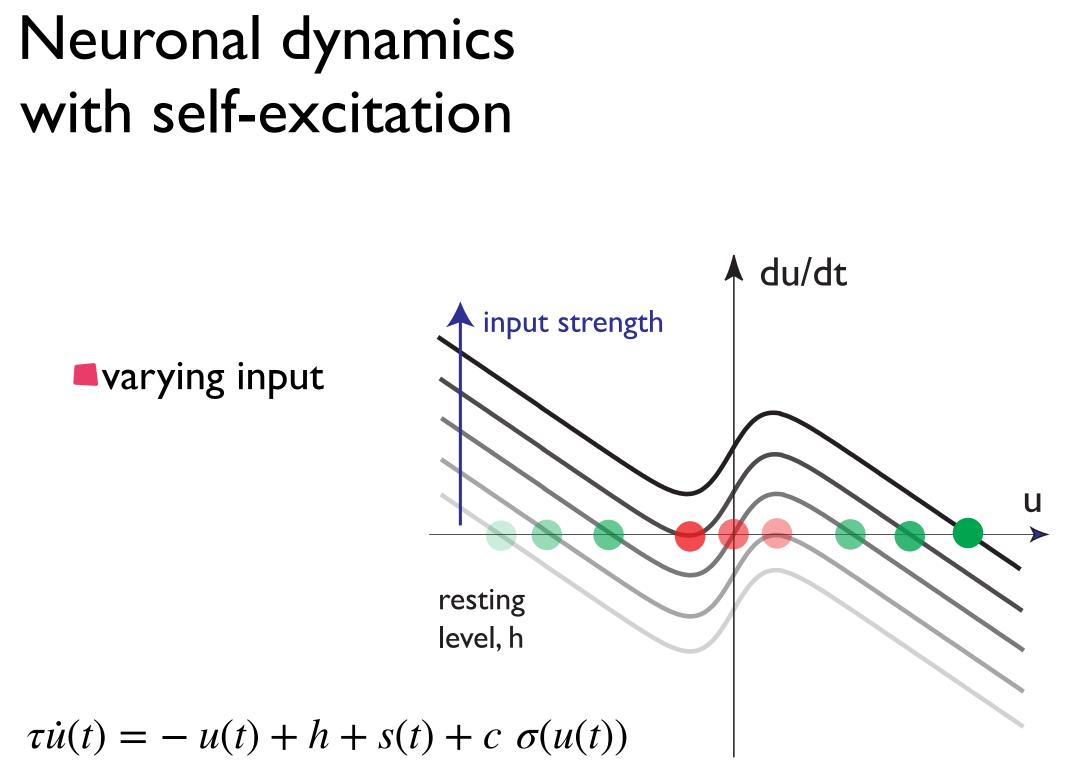
single activation variable with selfexcitation

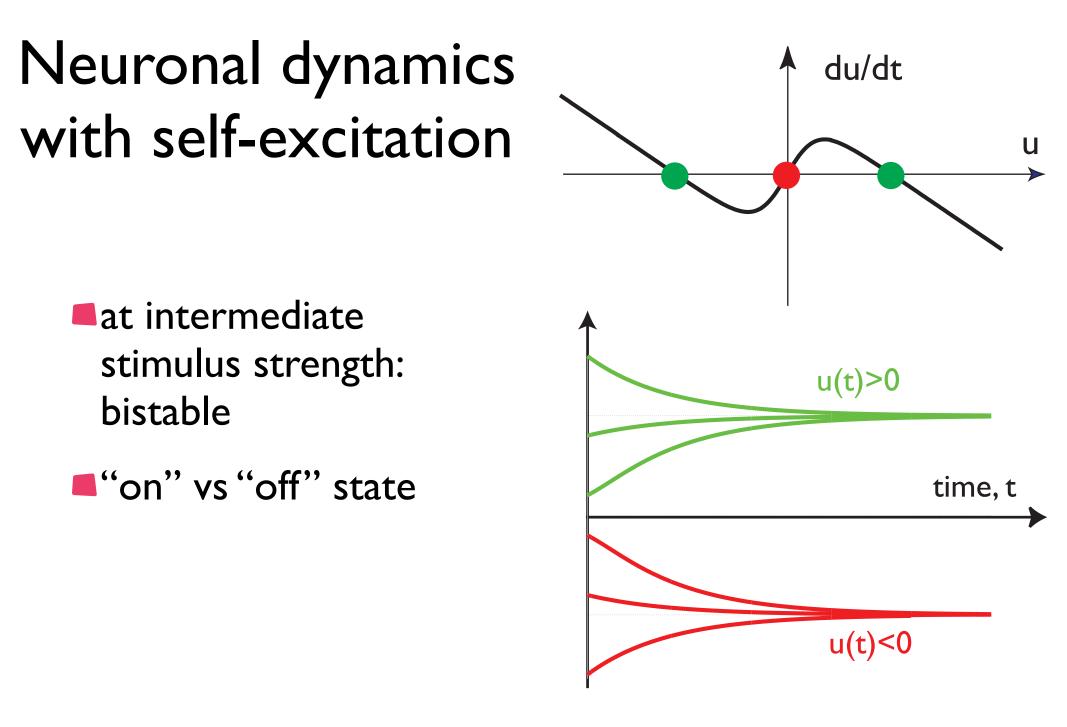
representing a small population with excitatory coupling



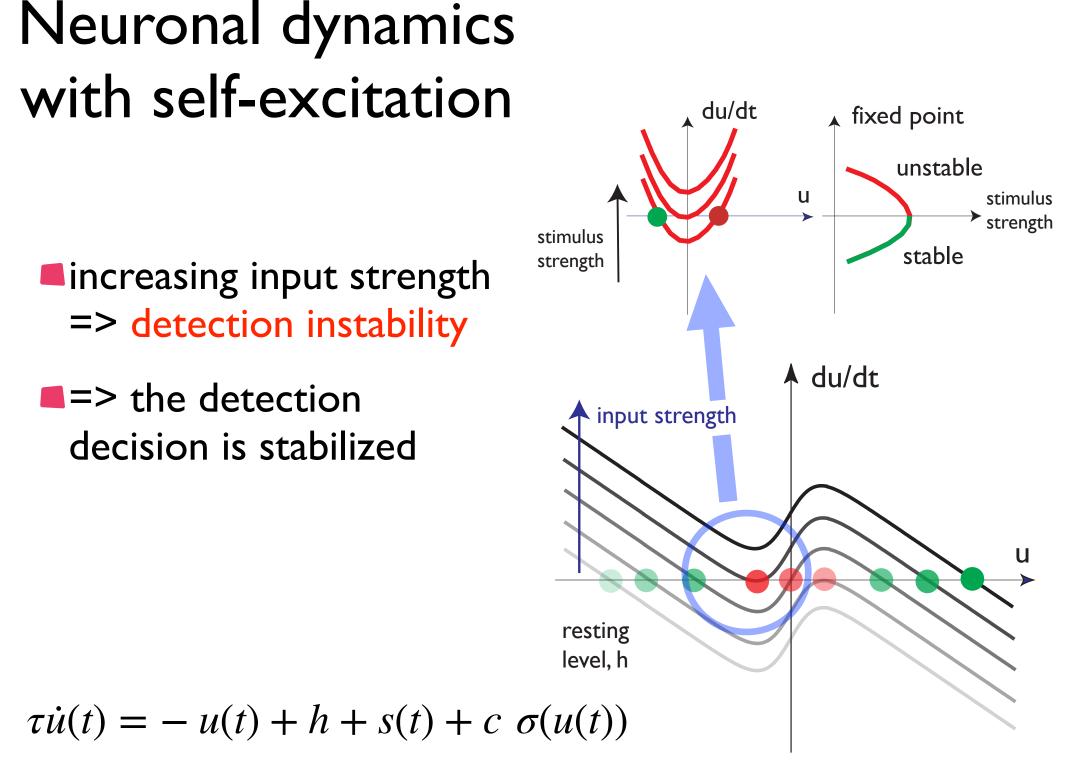
$$\tau \dot{u}(t) = -u(t) + h + s(t) + c \ \sigma(u(t))$$

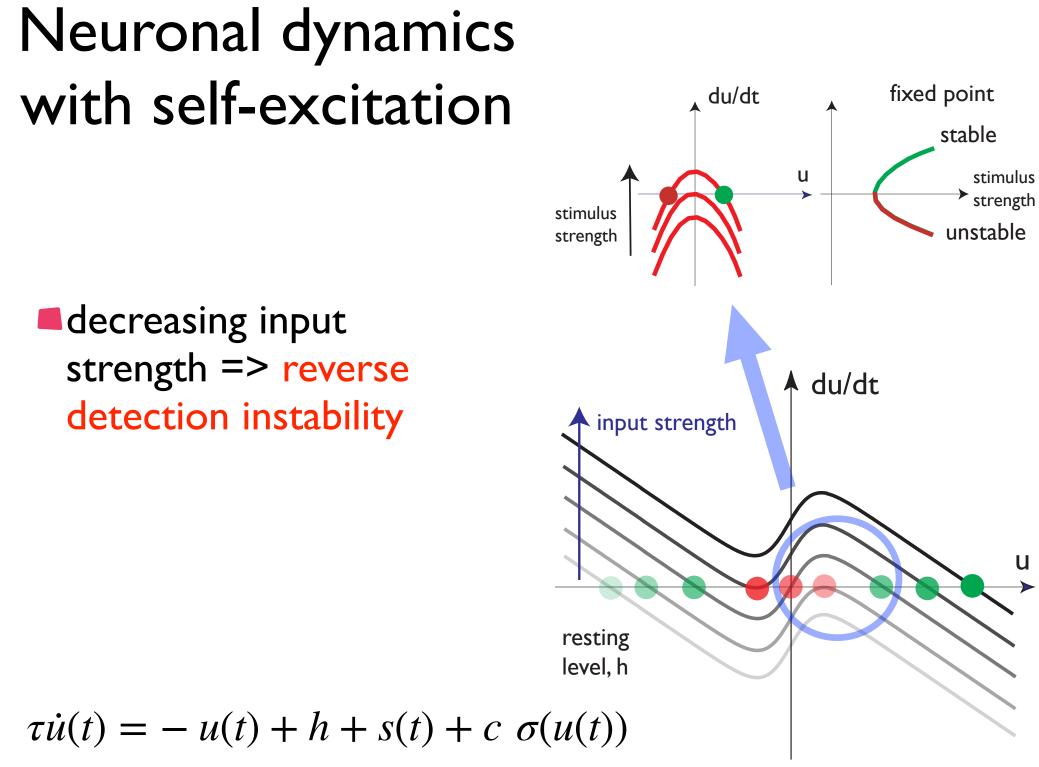






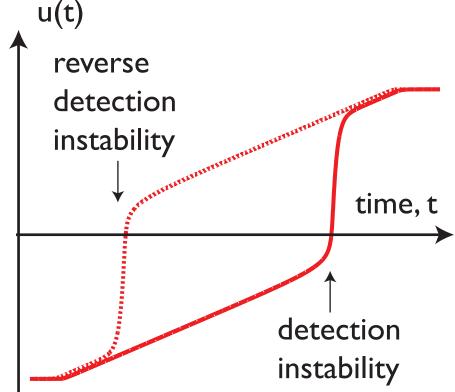
 $\tau \dot{u}(t) = -u(t) + h + s(t) + c \ \sigma(u(t))$ 





$$\tau \dot{u}(t) = -u(t) + h + s(t) + c \ \sigma(u(t))$$

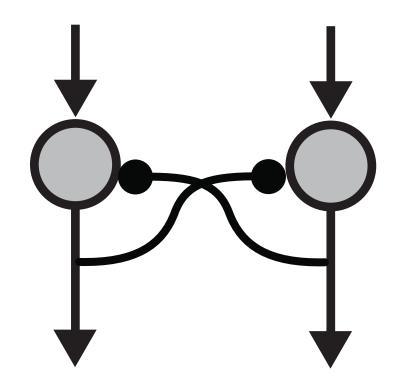
#### the detection and its reverse => create discrete events from time-continuous changes



## Neuronal dynamics with self-excitation

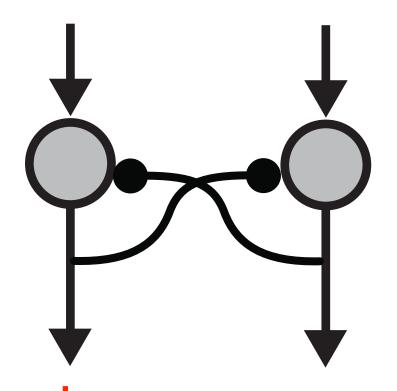
## => simulation

- two activation variables with reciprocal inhibitory coupling
- representing two small populations that are inhibitorily coupled



$$\tau \dot{u}_1(t) = -u_1(t) + h + s_1(t) - c_{12}\sigma(u_2(t))$$
  
$$\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) - c_{21}\sigma(u_1(t))$$

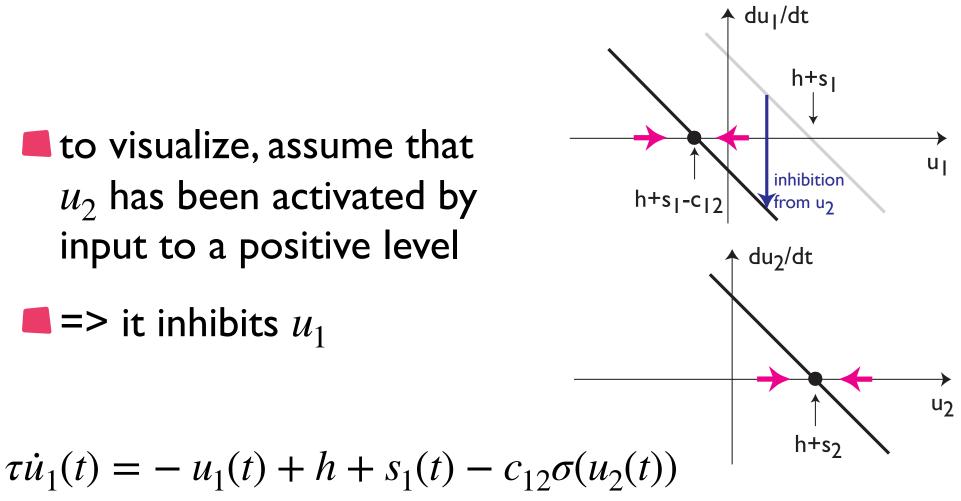
Coupling: the rate of change of one activation variable depends on the level of activation of the other activation variable



coupling

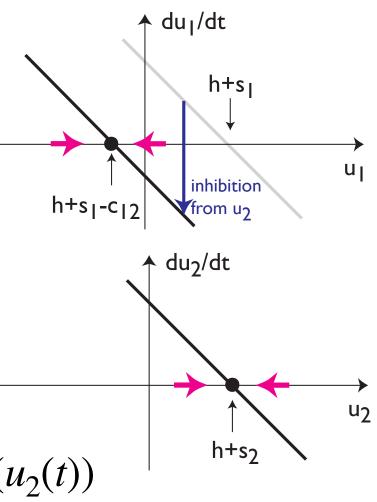
 $\tau \dot{u}_1(t) = -u_1(t) + h + s_1(t) - c_{12}\sigma(u_2(t))$  $\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) - c_{21}\sigma(u_1(t))$ 

- to visualize, assume that  $u_2$  has been activated by input to a positive level
- => it inhibits  $u_1$



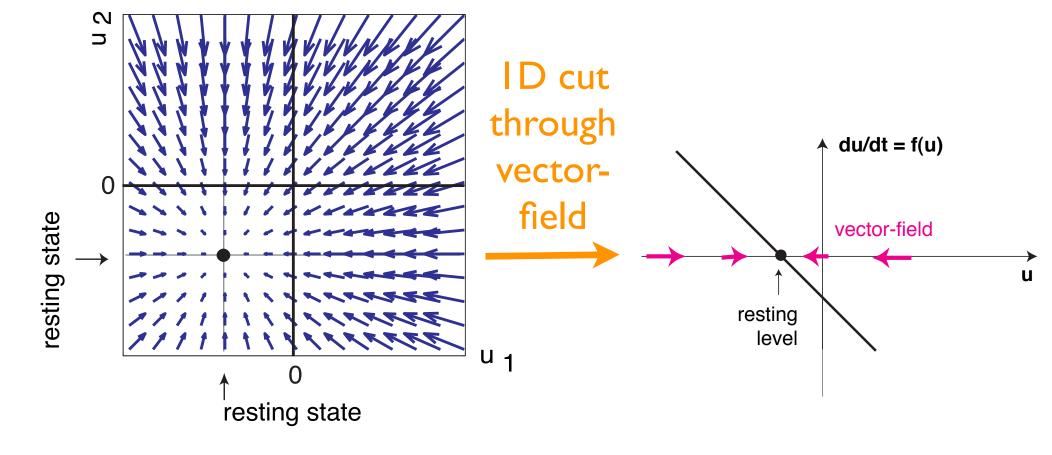
 $\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) - c_{21}\sigma(u_1(t))$ 

- why would  $u_2$  be positive before  $u_1$ ?
- more input to u<sub>2</sub> (better "match") => faster increase
- input advantage <=> time advantage <=> competitive advantage

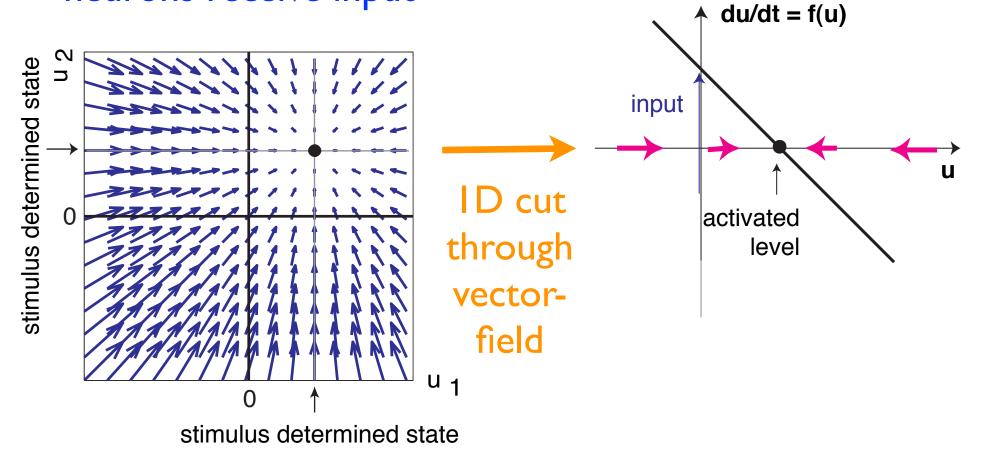


 $\tau \dot{u}_1(t) = -u_1(t) + h + s_1(t) - c_{12}\sigma(u_2(t))$  $\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) - c_{21}\sigma(u_1(t))$ 

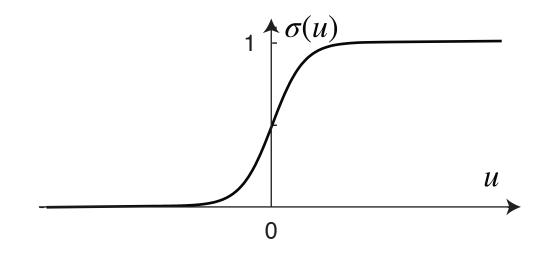




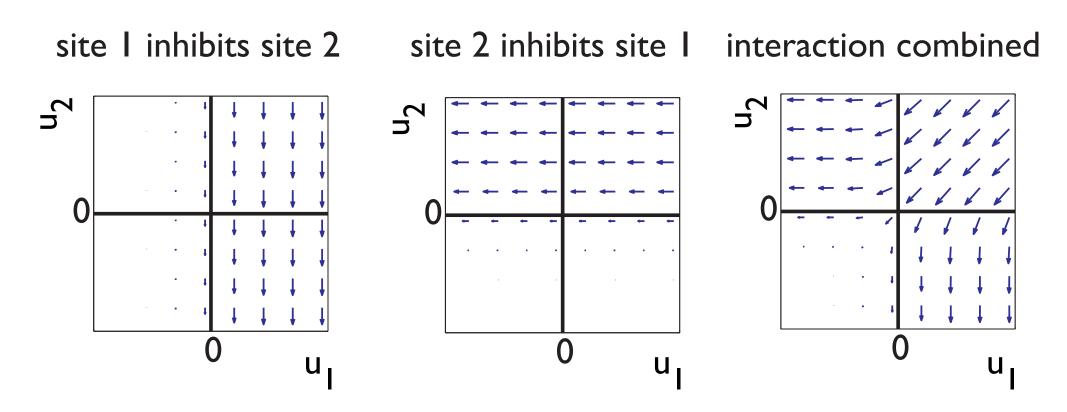
vector-field (without interaction) when both neurons receive input



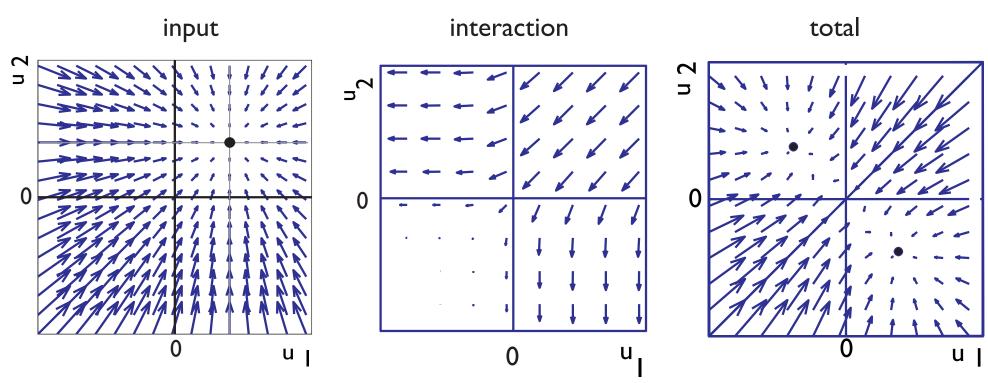
only activated neurons participate in interaction!

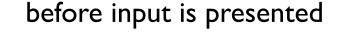


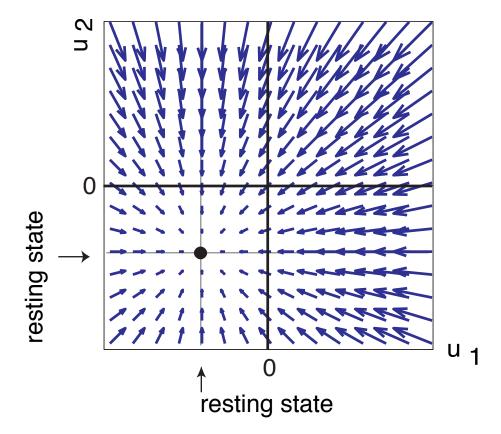
vector-field of mutual inhibition



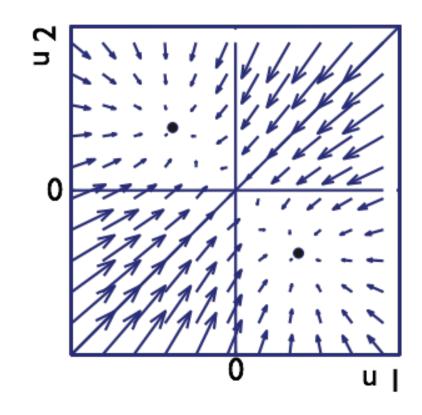
#### vector-field with strong mutual inhibition: bistable



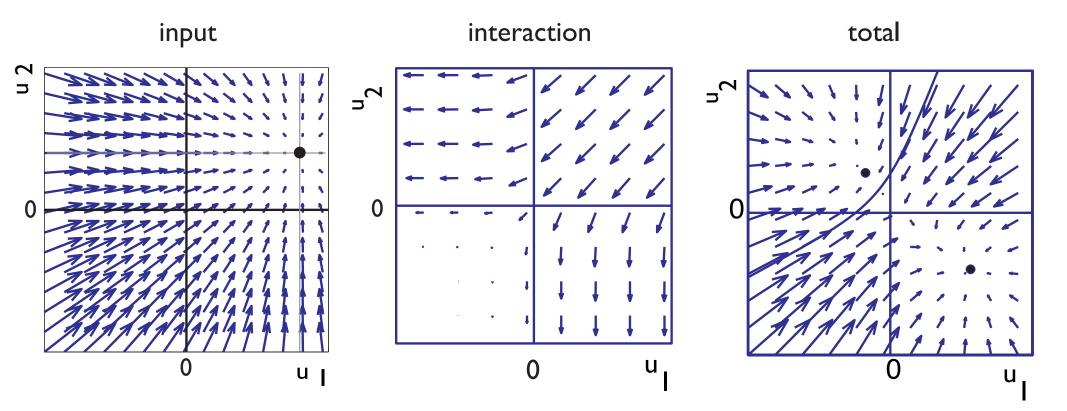




after input is presented



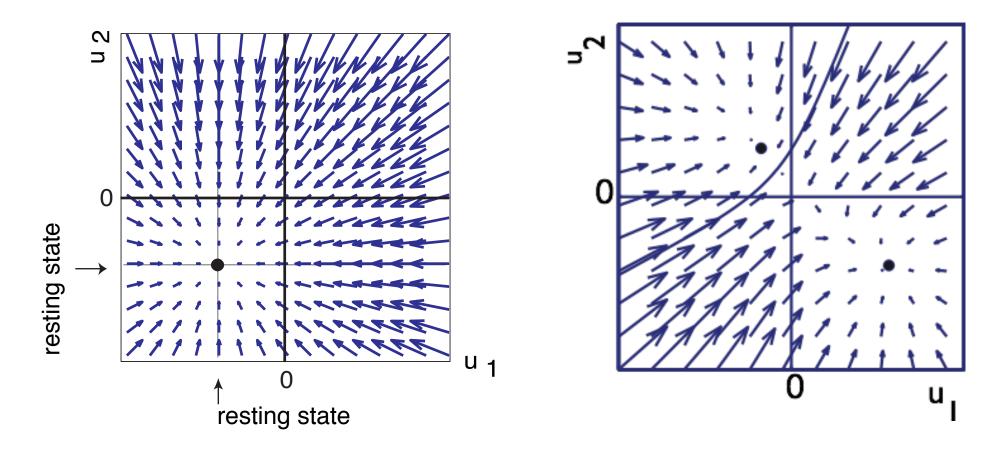
stronger input to  $u_1 =>$  attractor with positive  $u_1$  stronger, attractor with positive  $u_2$  weaker => closer to instability



decision made at detection instability!

before input is presented

after input is presented



## => simulation

## The neural dynamics of fields

- … the same underlying math
- coupling among continuously many activation variables
- Iocal excitatory coupling ("self-excitation")
- global inhibitory coupling ("mutual inhibition")

#### field vs. activation variables

