

Higher-dimensional  
dynamics fields  
enable new cognitive  
function

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# Core of DFT

- field dynamics combines input

- with strong interaction:

- local excitation

- global inhibition

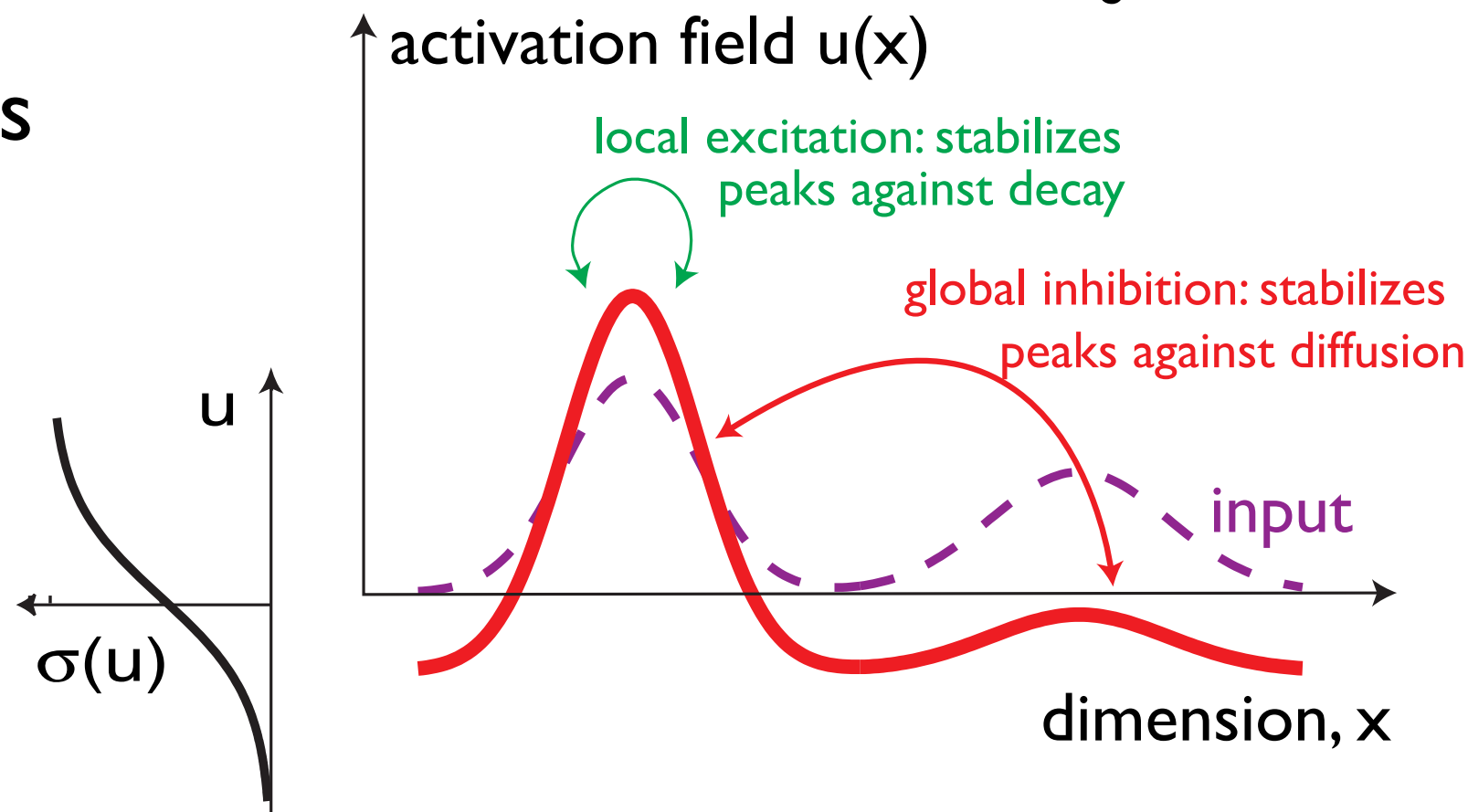
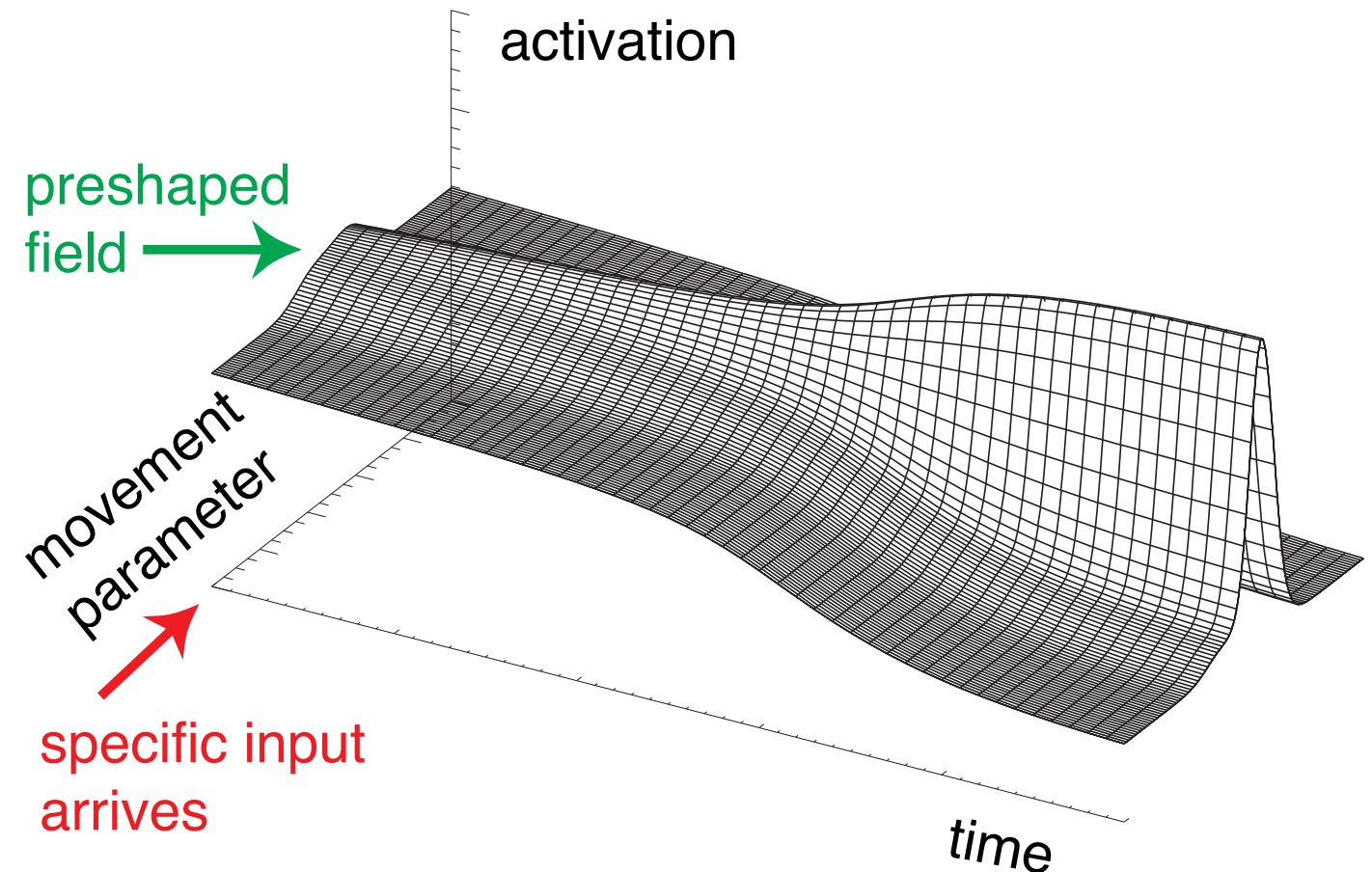
- leading to stable peaks

- instabilities:

- detection

- selection

- memory

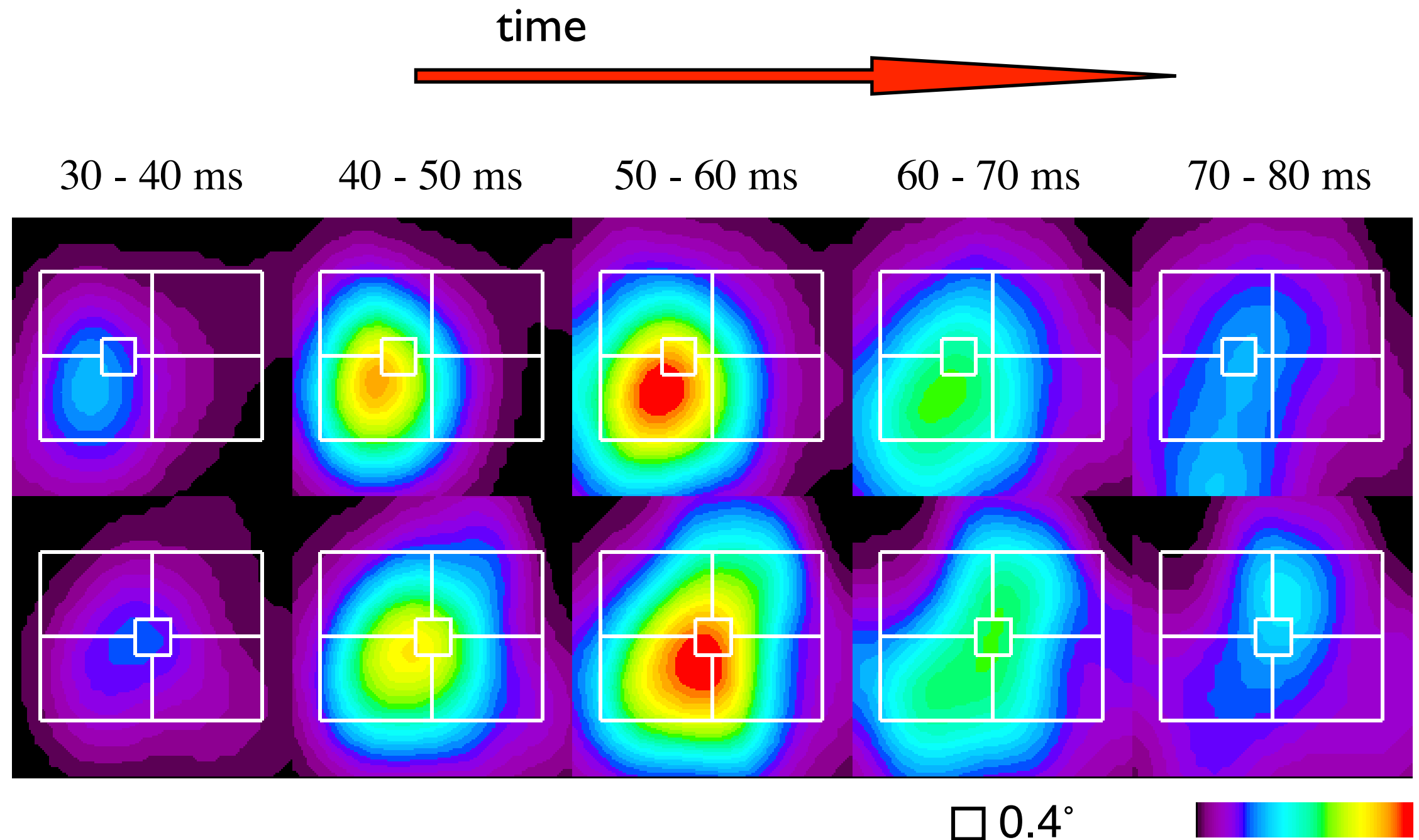


# Dimensionality of fields

- all this was done primarily in fields defined over a single dimension...
- multi-dimensional fields are not per se fundamentally different....
- in particular, they have the same kind of dynamics as one-dimensional fields

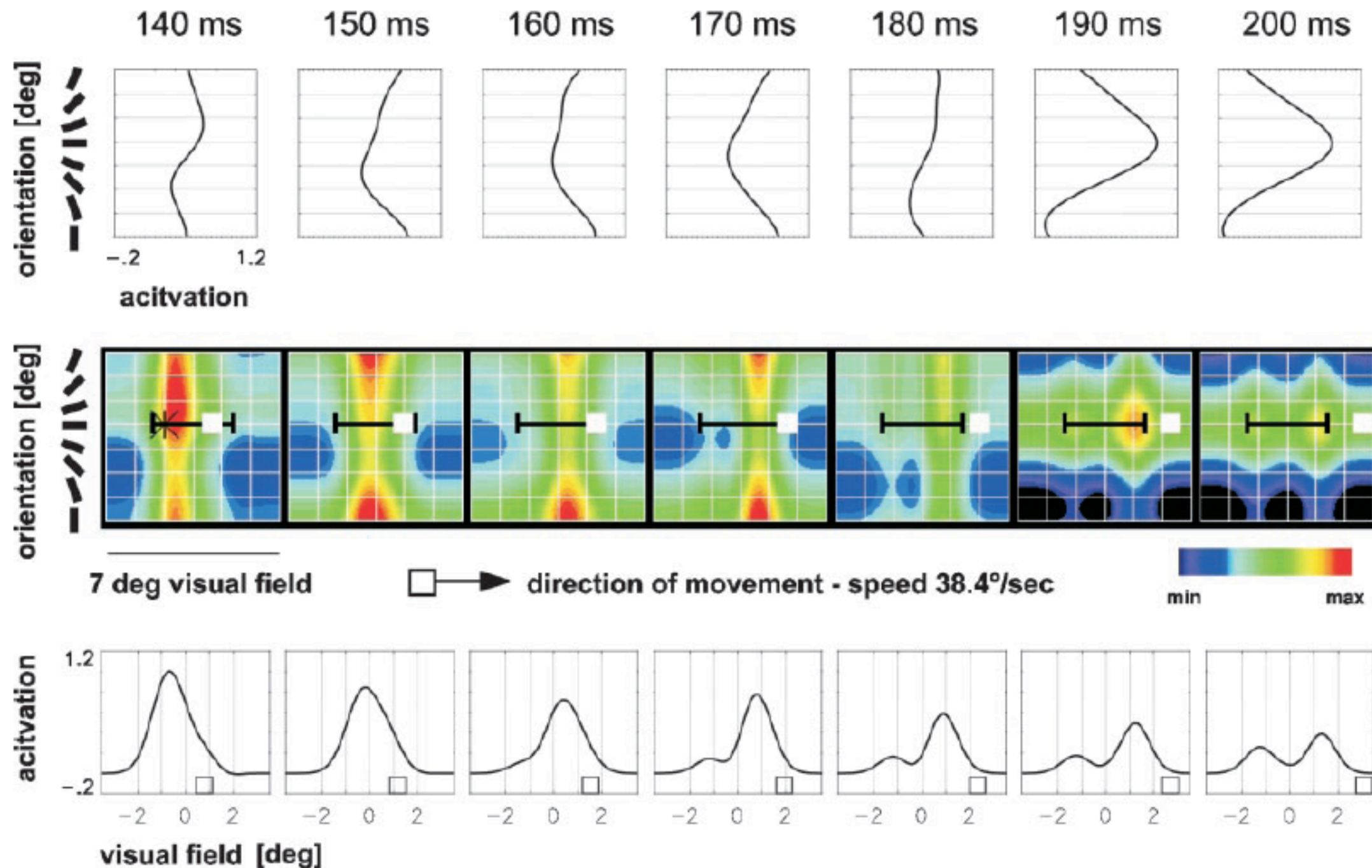
# example: retinal space

■ obviously two-dimensional



# example: visual feature map

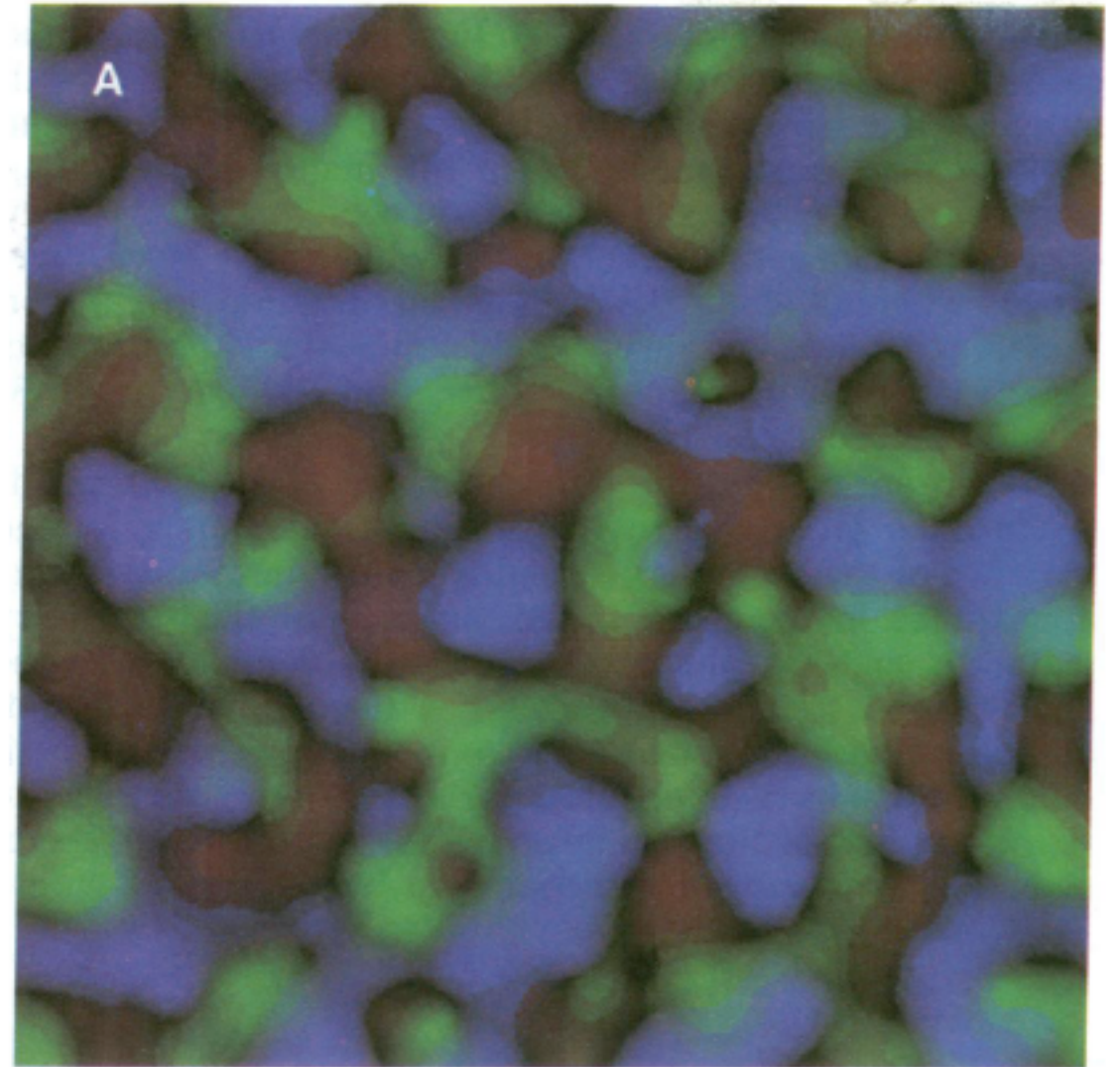
## ■ orientation-retinal location



[Jancke, JNeurosci (2000)]

# example: visual feature maps

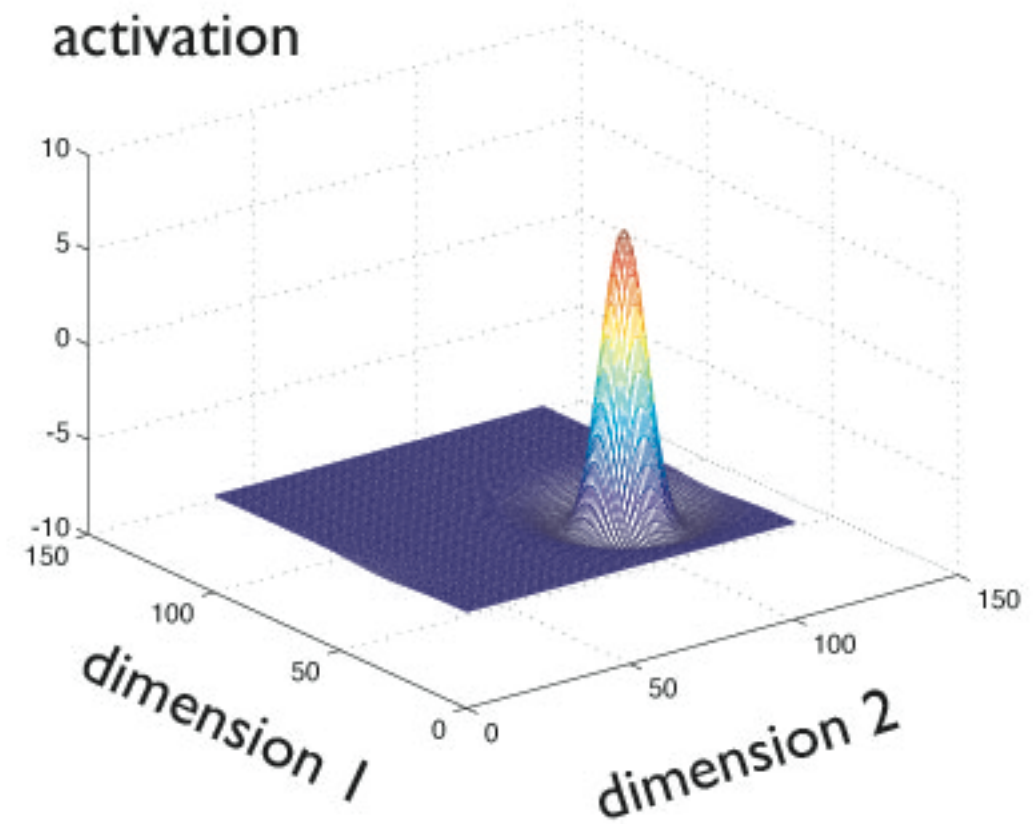
- the neural field representation a single feature (e.g. orientation) as well as retinal location is at least three-dimensional
- cannot be mapped onto cortical surfaces without cuts ...





# dynamics of 2D fields

- => simulation
- no problem ... self-stabilized peaks work just fine...

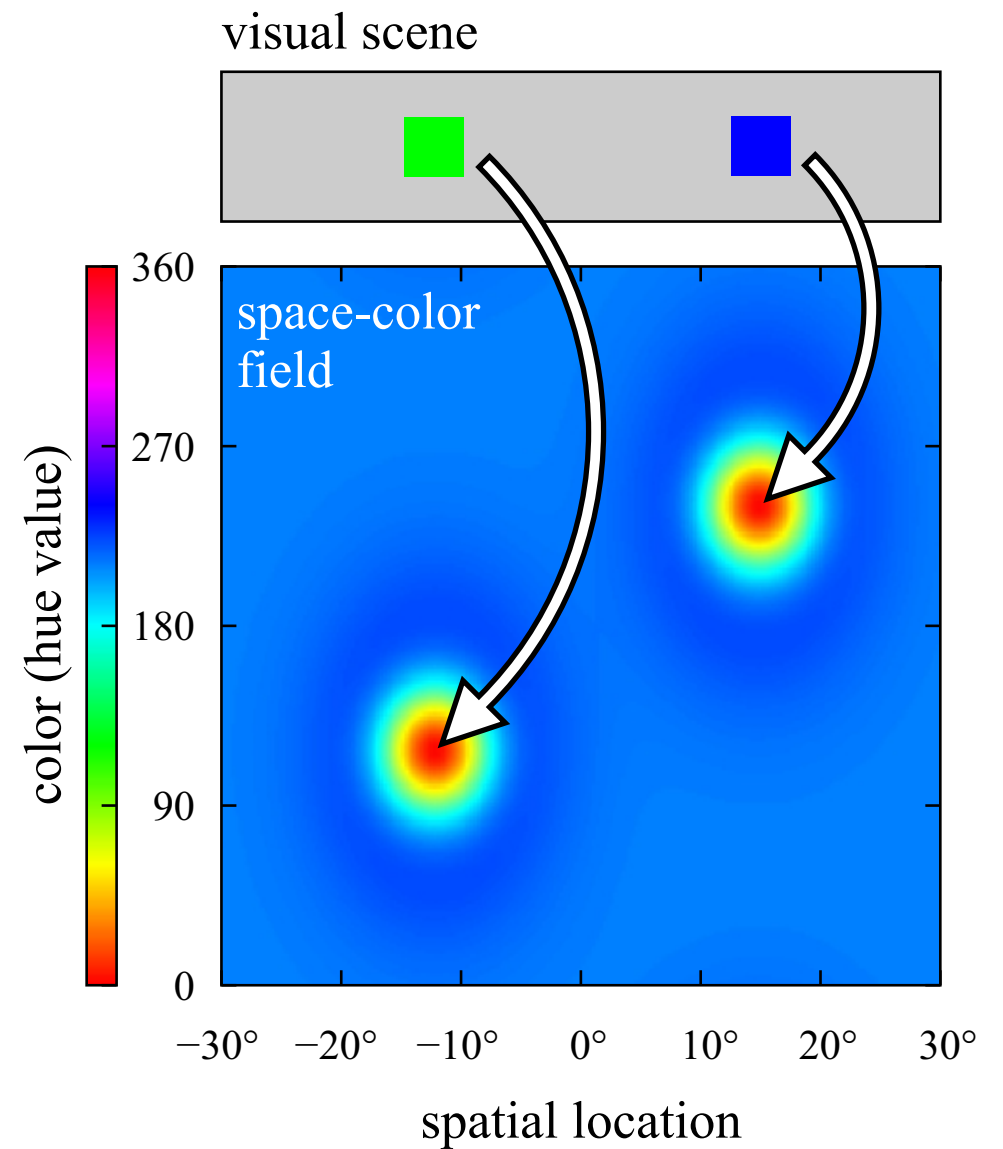


But: higher-dimensional  
fields enable new  
cognitive functions



# Example I: Feature binding

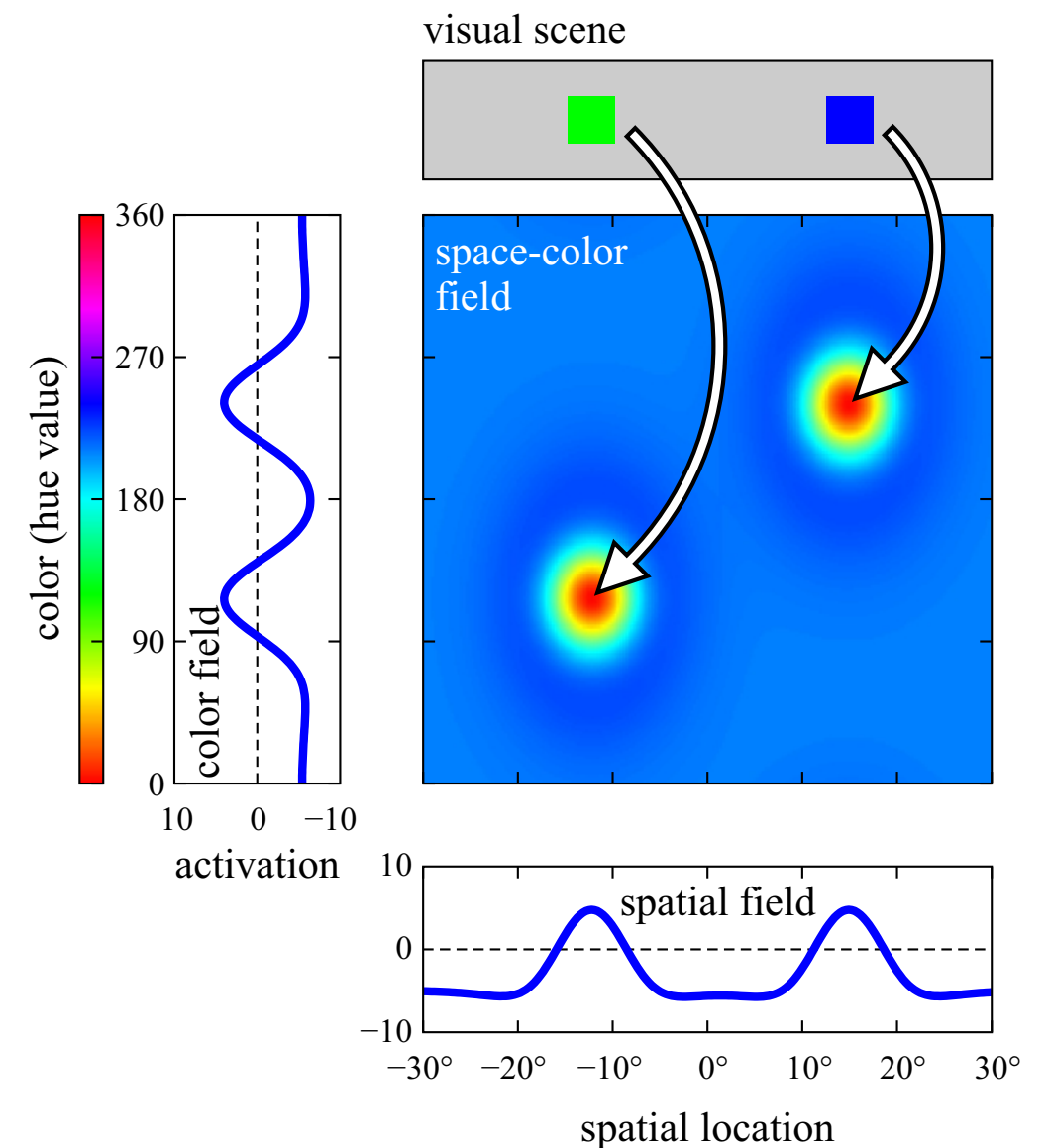
- 1D spatial location (for illustration)
- 1D color dimension (hue)
- visual input: 2D
- $\Rightarrow$  2D peaks



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

# 2D input

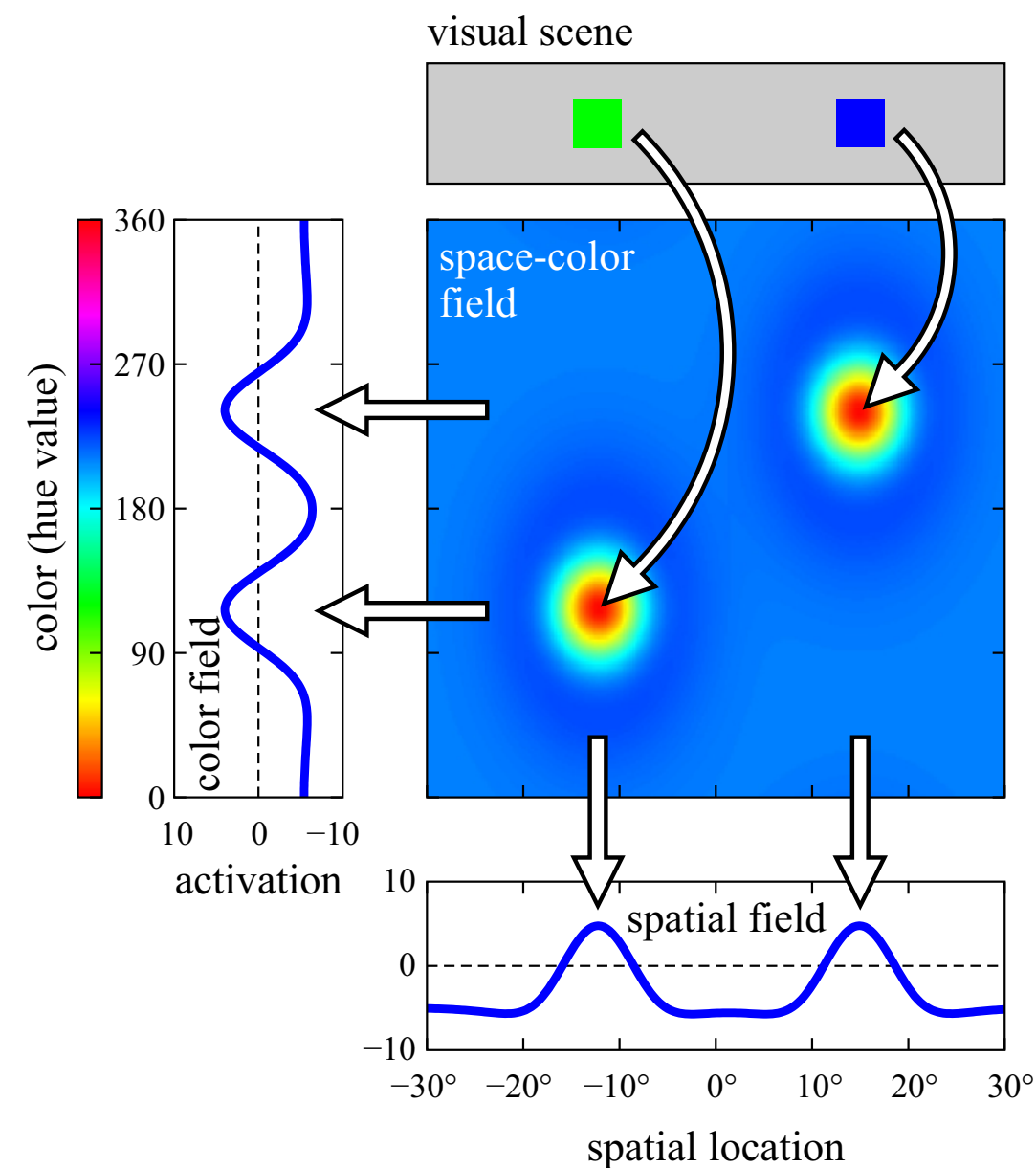
- creates 2D peaks that form combined (bound) representations of objects



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

# extracting features

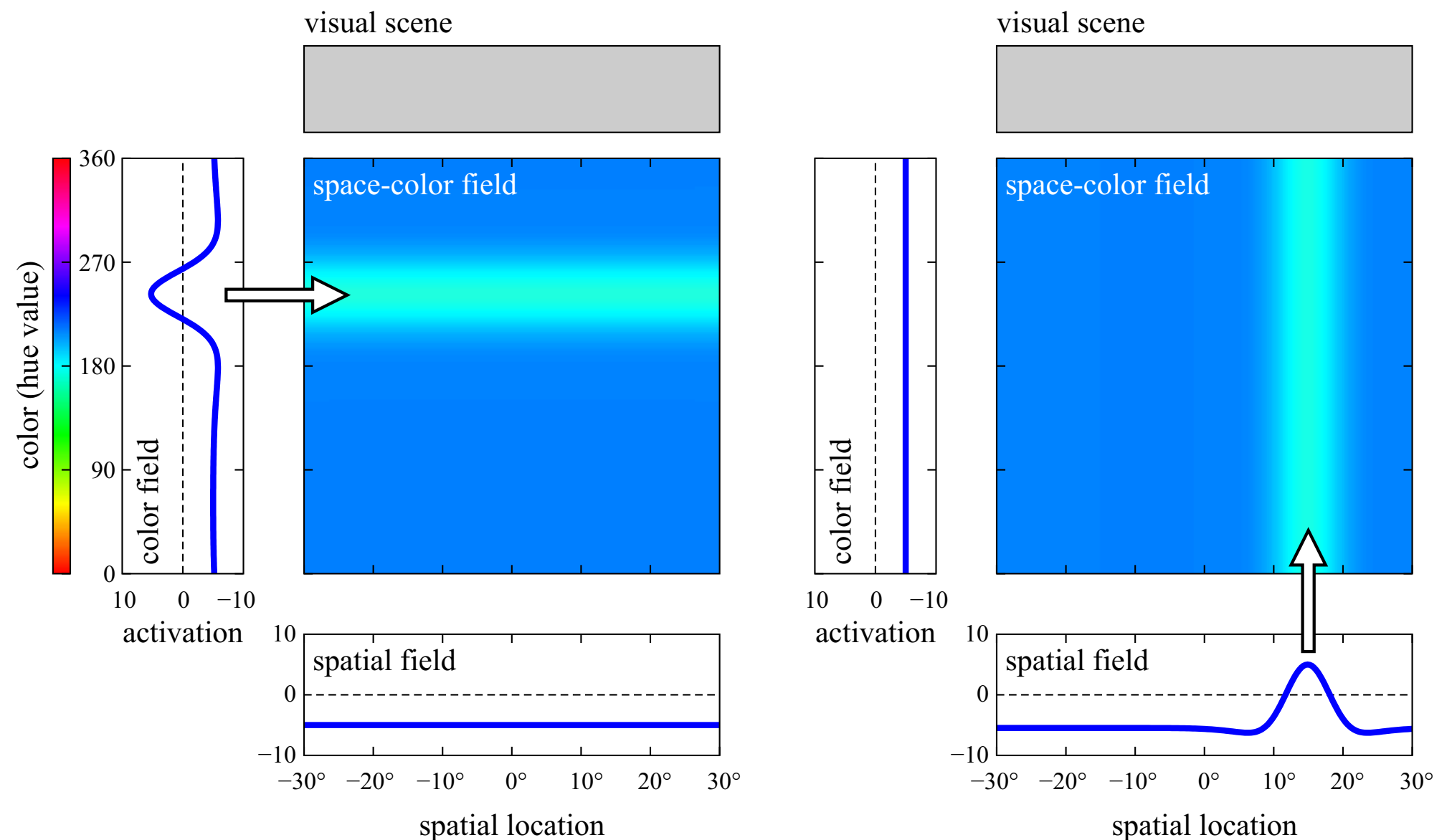
- read-out from 2D to 1D by projection
- by summing along the other dimension (marginalization)
- or by taking the (soft)max



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

# assembling bound representations

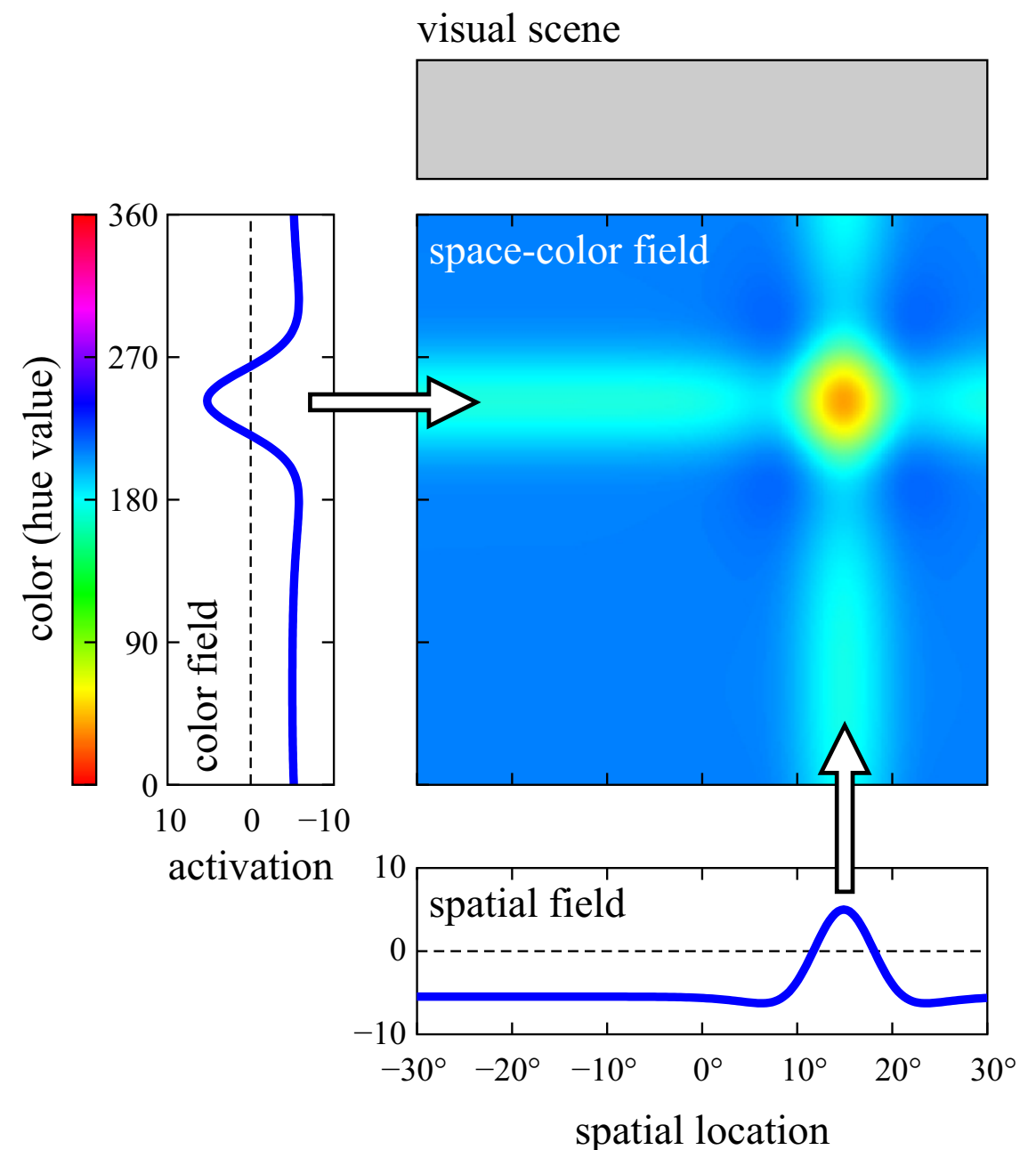
- from 1D to 2D: ridge input is constant along the other dimension



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

# assembling bound representations

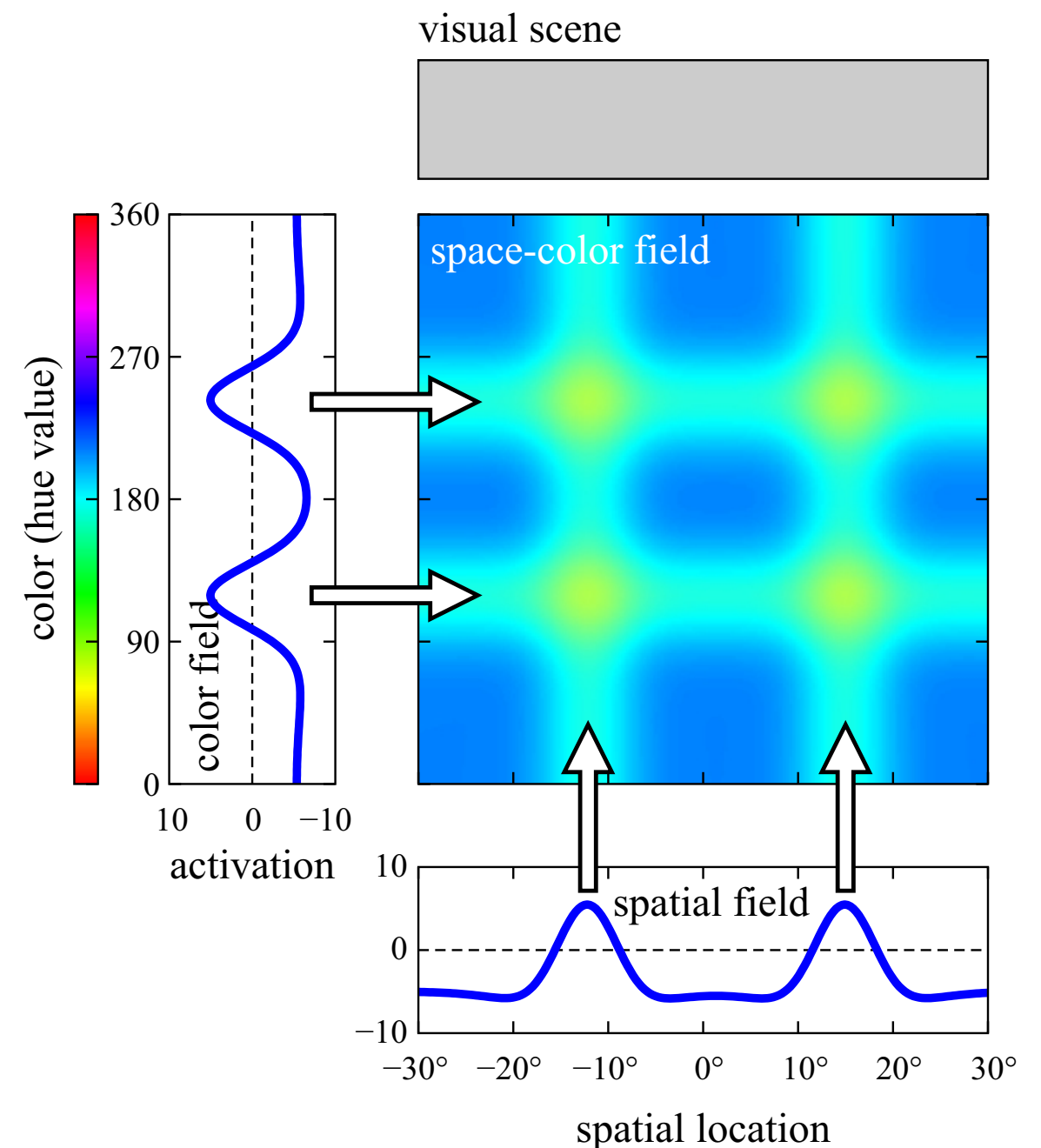
- peaks form at the intersections of ridges and form bound representations of the two dimensions



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

# assembling bound representations

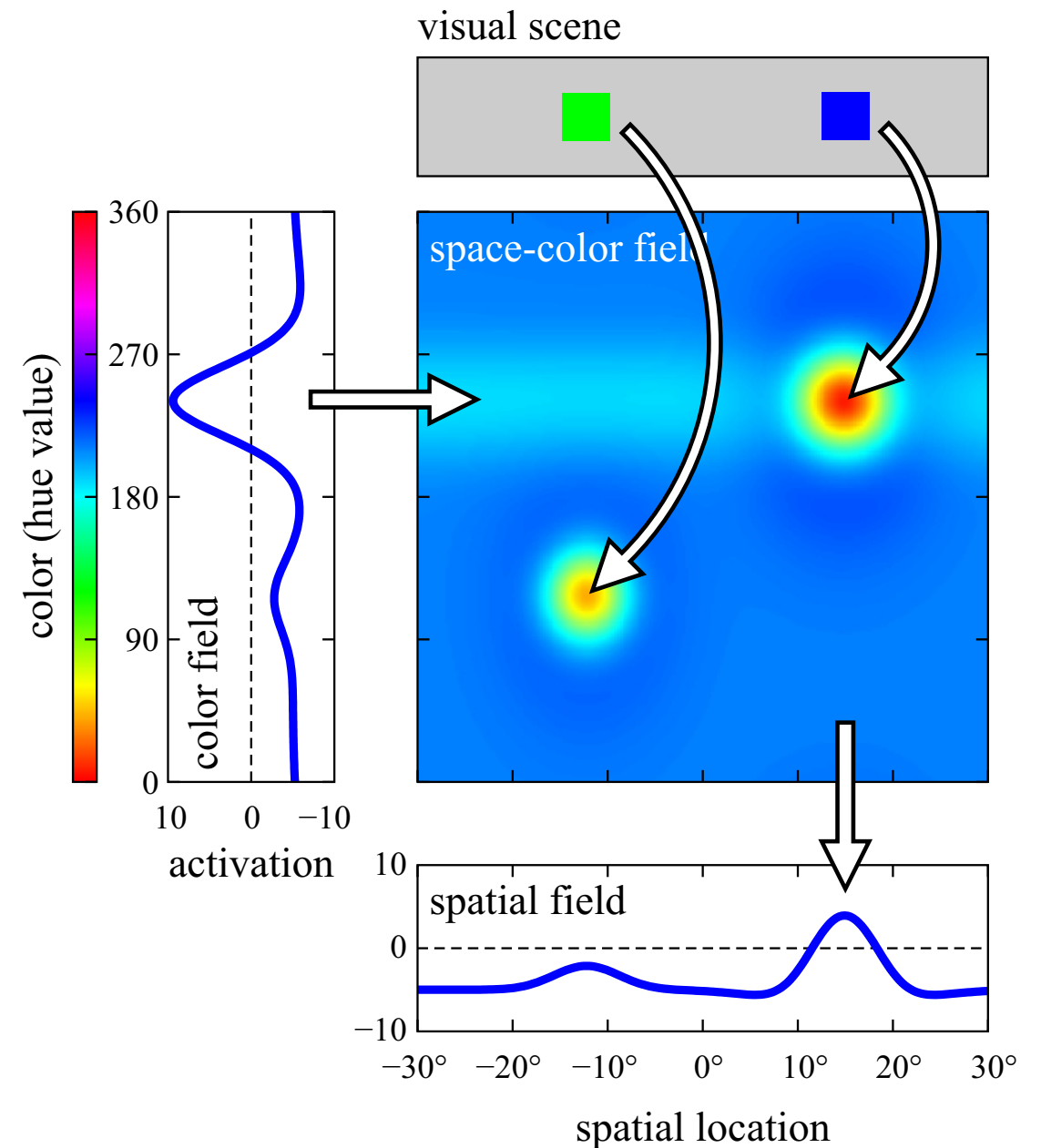
- binding problem: multiple ridges lead to a correspondence problem
- => assemble one object at a time... sequentiality bottleneck



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

# visual search

- combine 1D (ridge) input with 2D input..
- so that only those 2D locations can form peaks that overlap with ridge (boost driven detection)
- activates objects consistent with 1D feature value



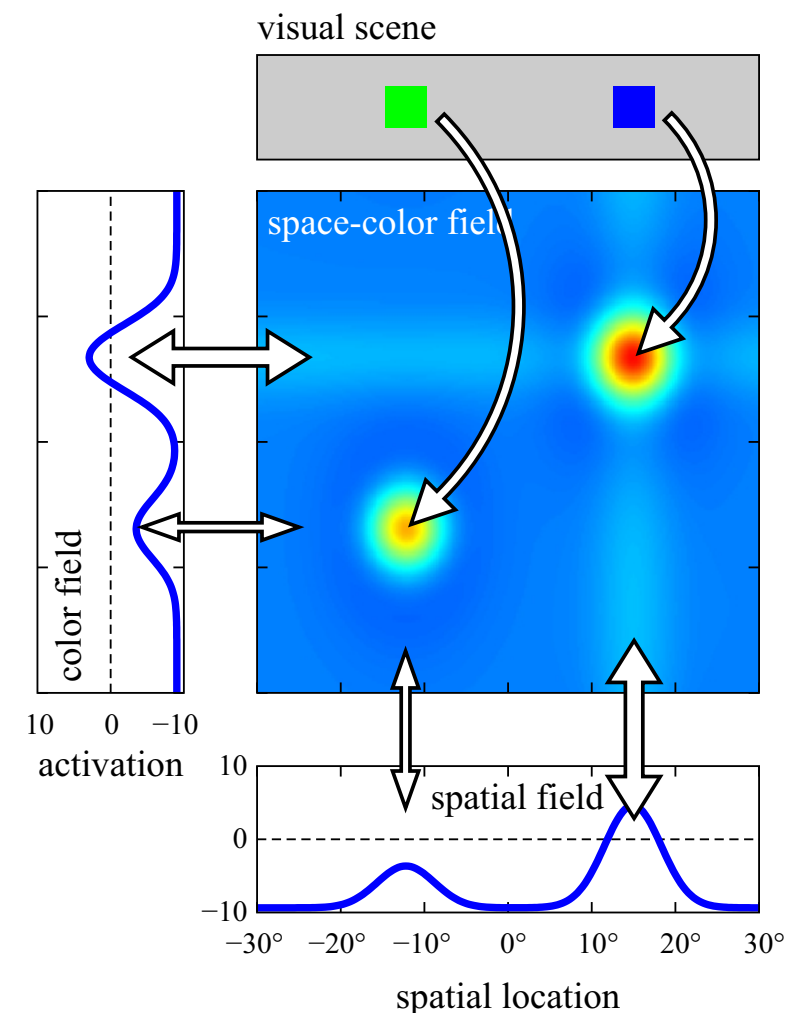
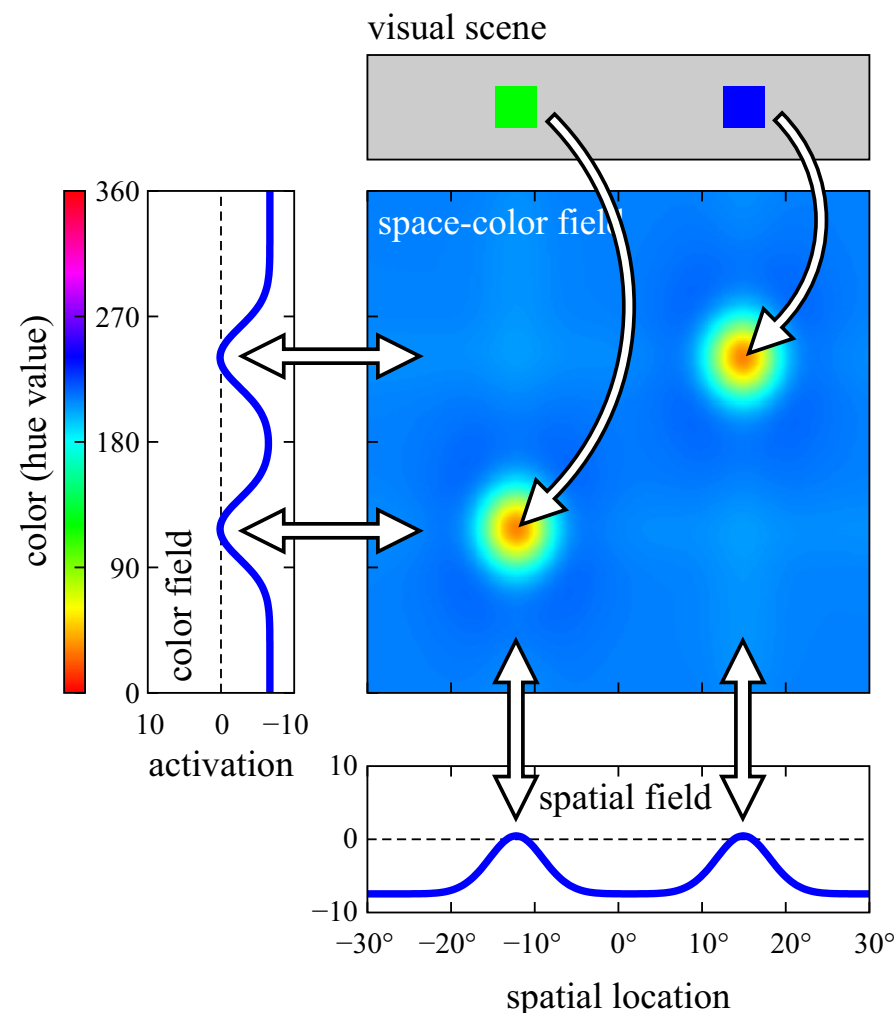
[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]



# visual search

- the selection from visual search can be propagated to the ID feature representations

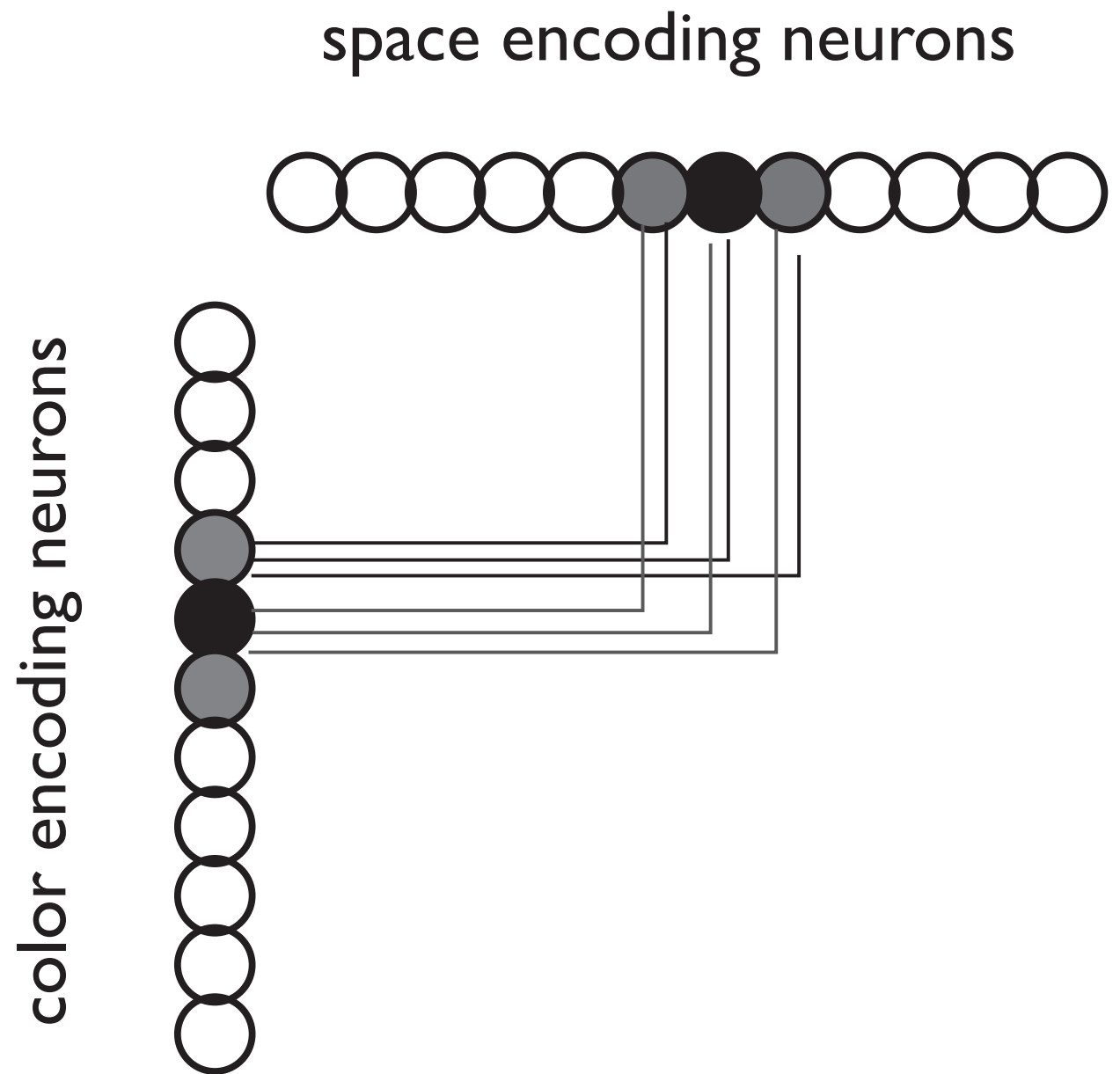
...



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

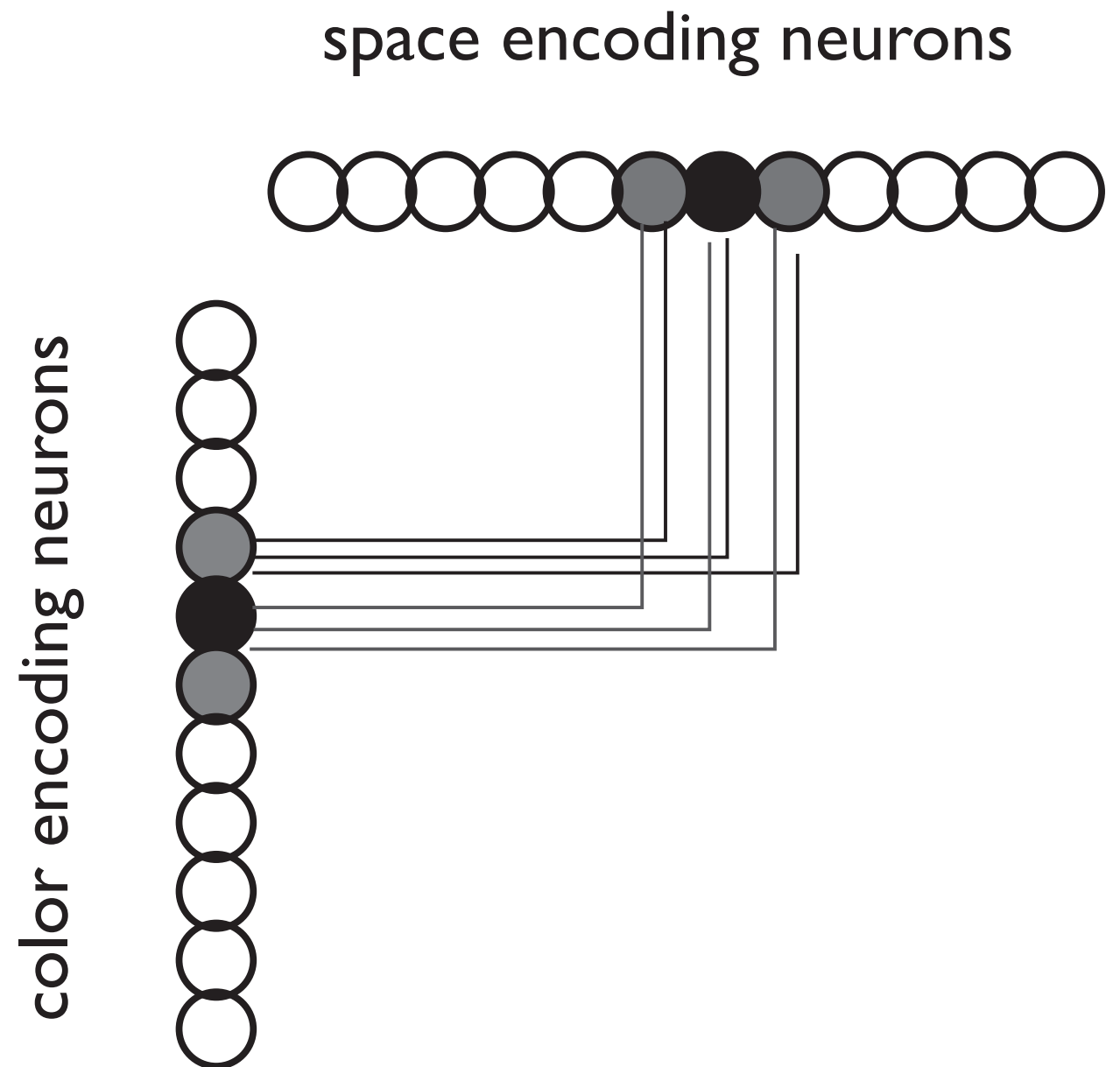
# contrast: synaptic association

- in conventional connectionist networks associative relationships are learned by adjusting synapses between those color and space neurons that have been co-activated



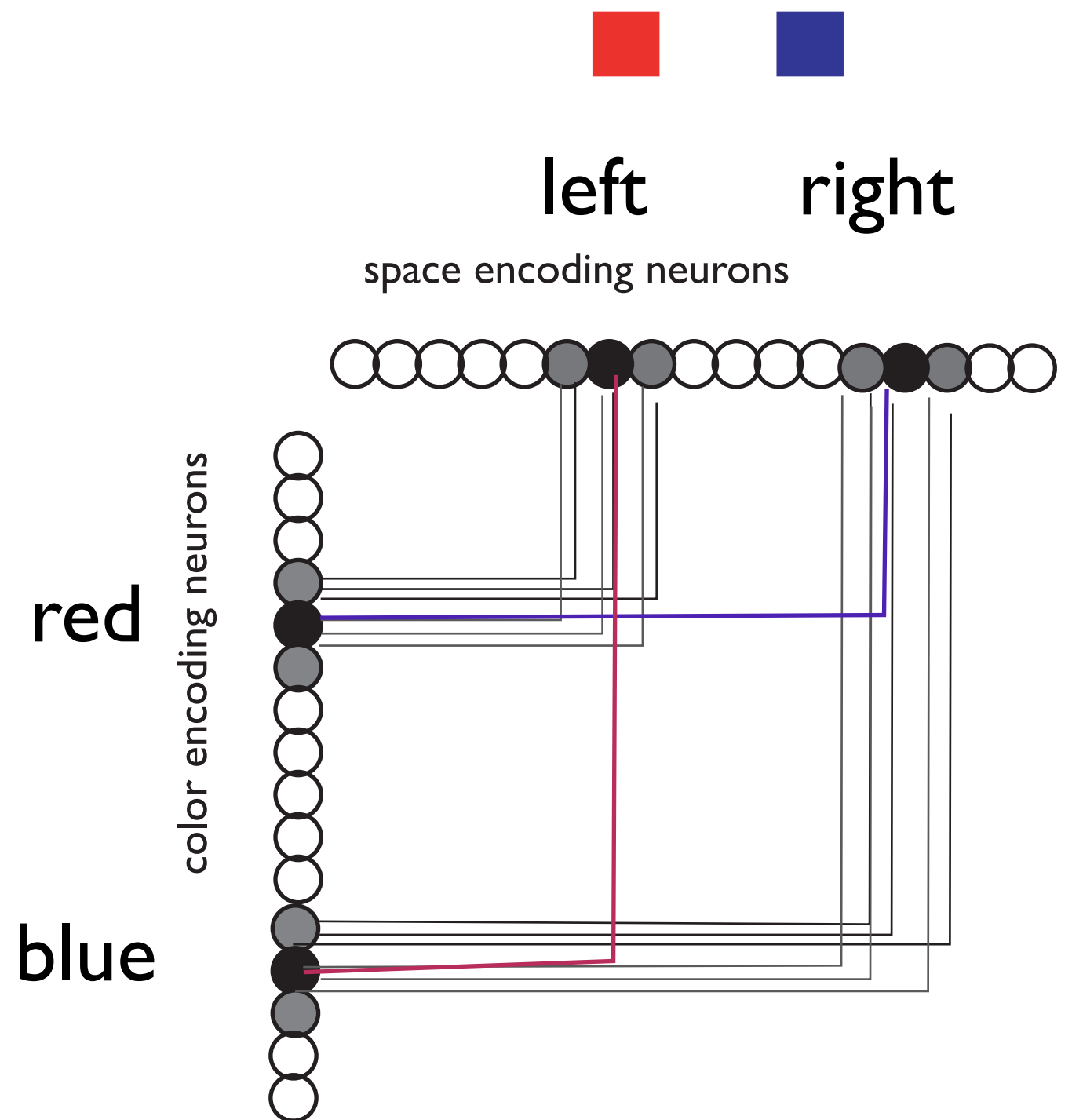
# limitations of synaptic association

- connections must be learned, so does not account for how “where is the red square” works from current stimulation (seen for the first time ever)



# limitations of synaptic association

- learning multiple associations poses a binding problem:
- connectionist associators learn one item at a time and need separate presentation of individual items!



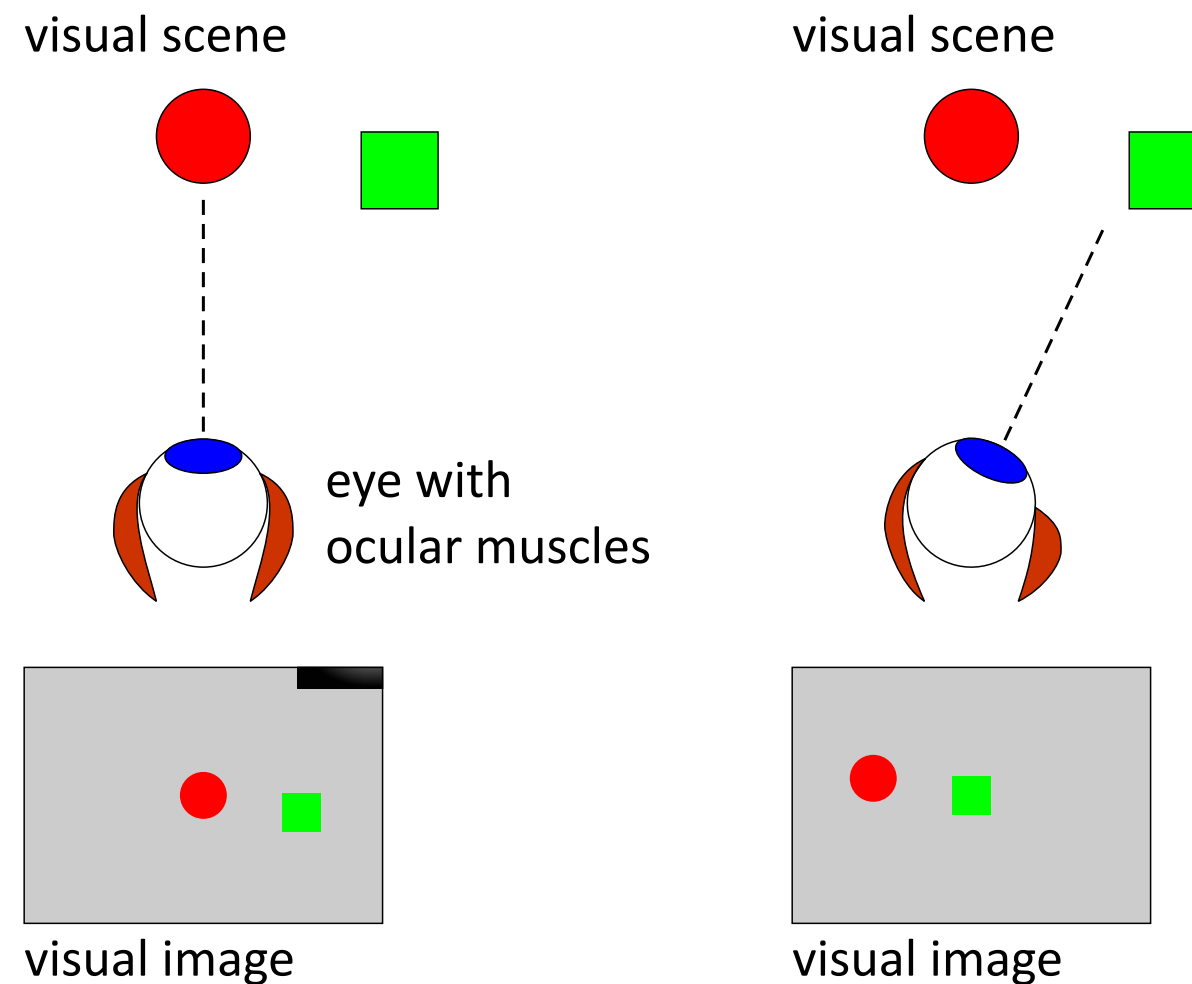
the network may associate blue with left and red with right

# Example 2: coordinate transformations

- which are analogous to the instantaneous associations between stimulus features demonstrated earlier

# coordinate transformations

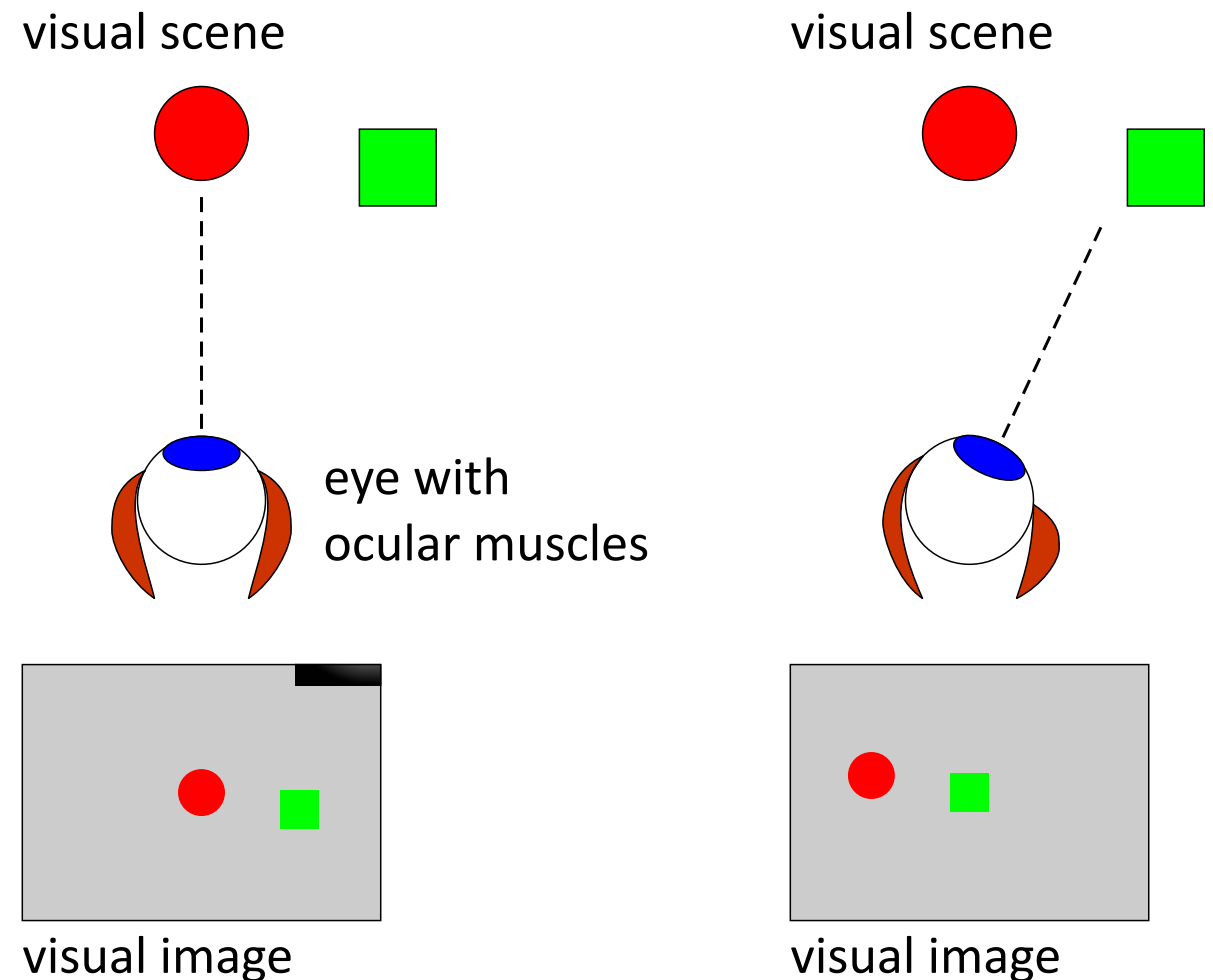
- eye movement: visual target from retinal representation to head-centered representation for reaching



[Slides adapted from Sebastian Schneegans, see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

# coordinate transformations

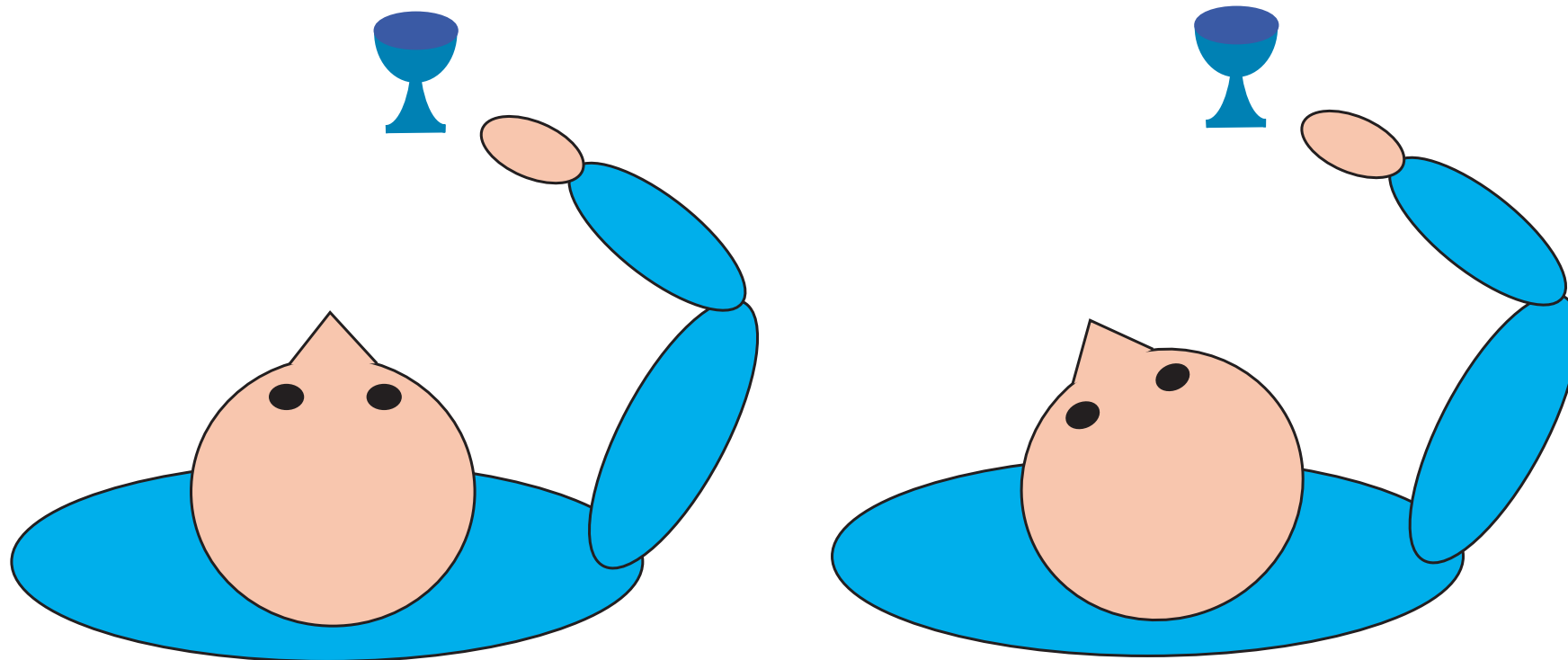
- every gaze shift changes the spatial reference frame of the visual perception
- how to memorize location when the reference frame keeps shifting?
- => transformation to gaze-invariant reference frame





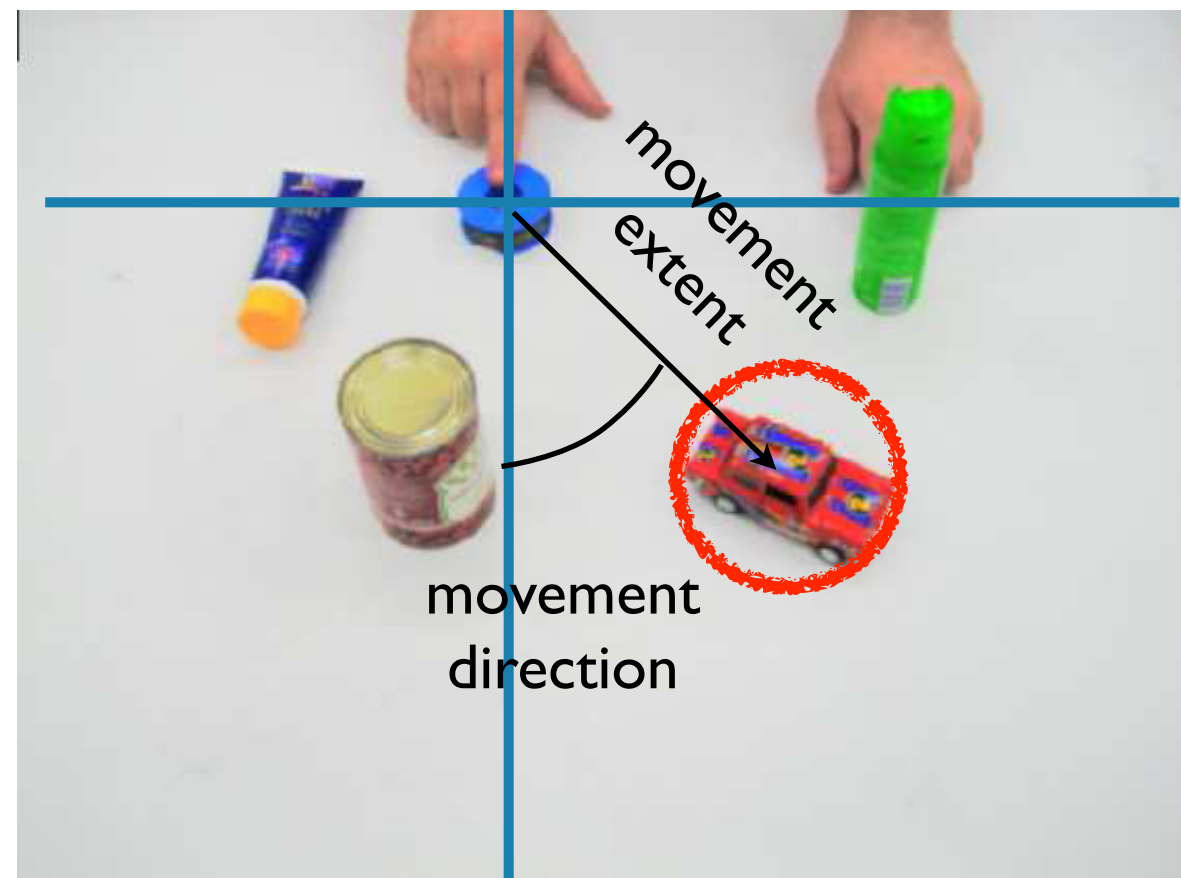
# coordinate transformations

- head movement: transform visual target from retinal representation to body-centered representation



# coordinate transformations

- hand movement: transform movement target from body-centered representation to hand-centered representation for reaching

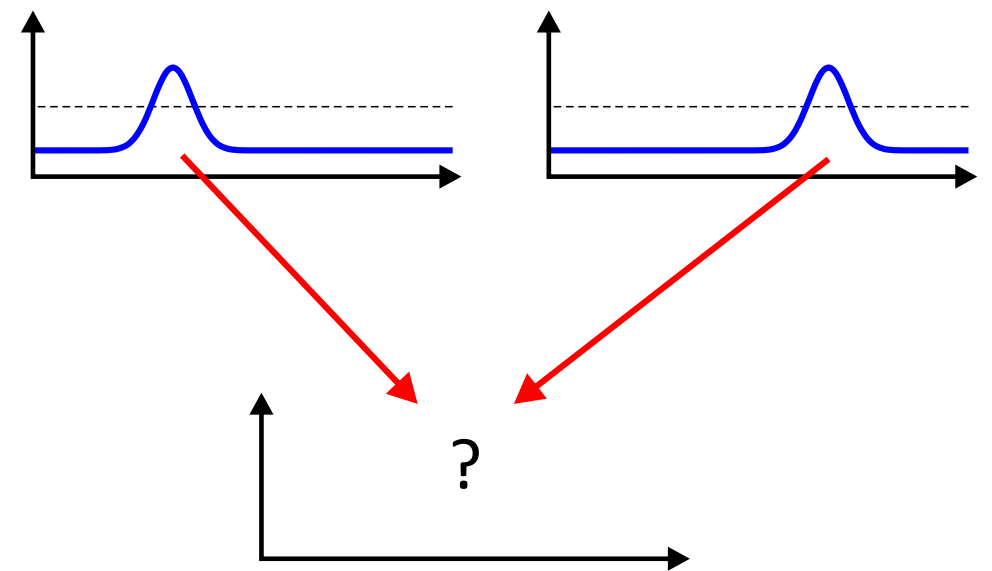
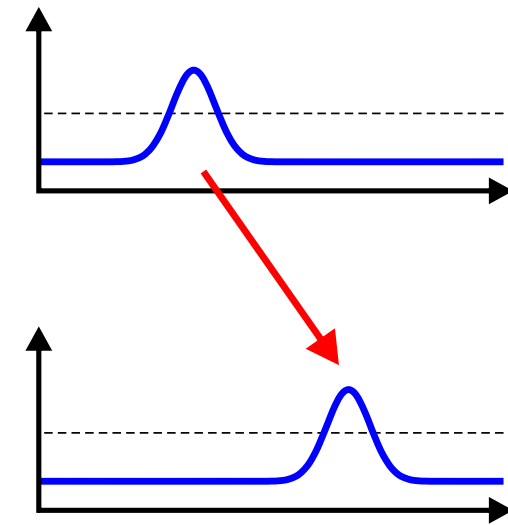


# coordinate transformations

- need mapping between different reference frame: retinocentric (moving with the eye) to body-centered (gaze-invariant)
- mapping is a variable shift, depends on current gaze direction
- as a formula  $x_{\text{body}} = x_{\text{retinal}} + x_{\text{gaze}}$
- but how to implement this in DNFs, using space code representations?

# coordinate transformations

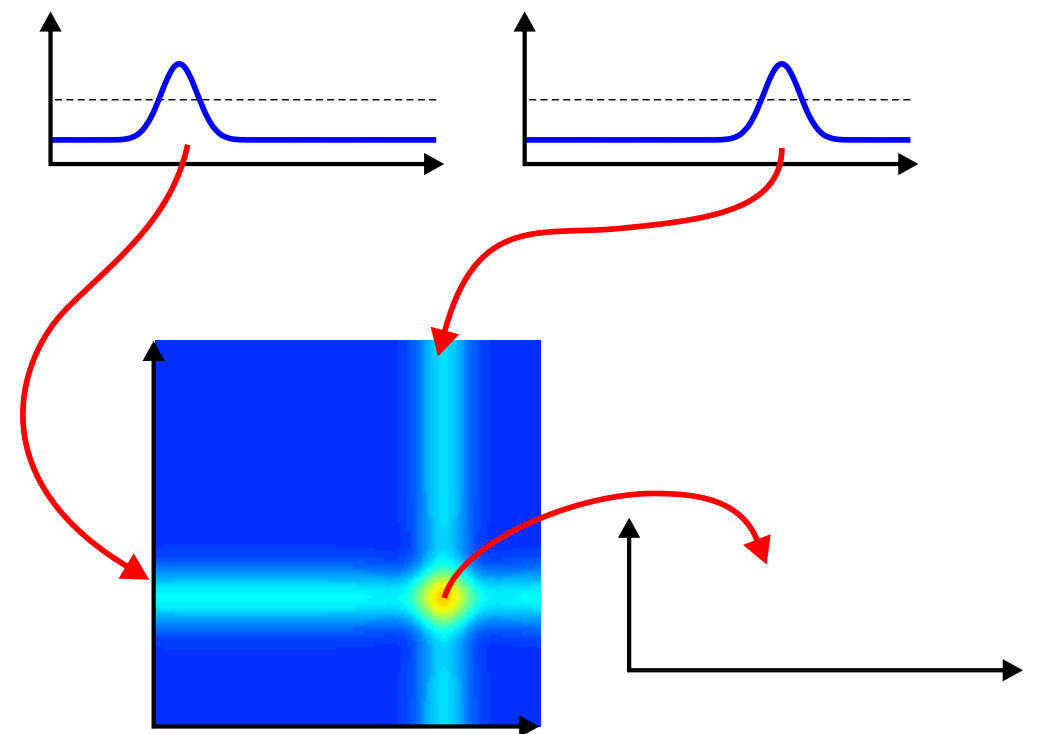
- fixed mapping: neural projection in a neural network
- flexible mapping that depends on gaze/eye position?



[Slides adapted from Sebastian Schneegans,  
see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

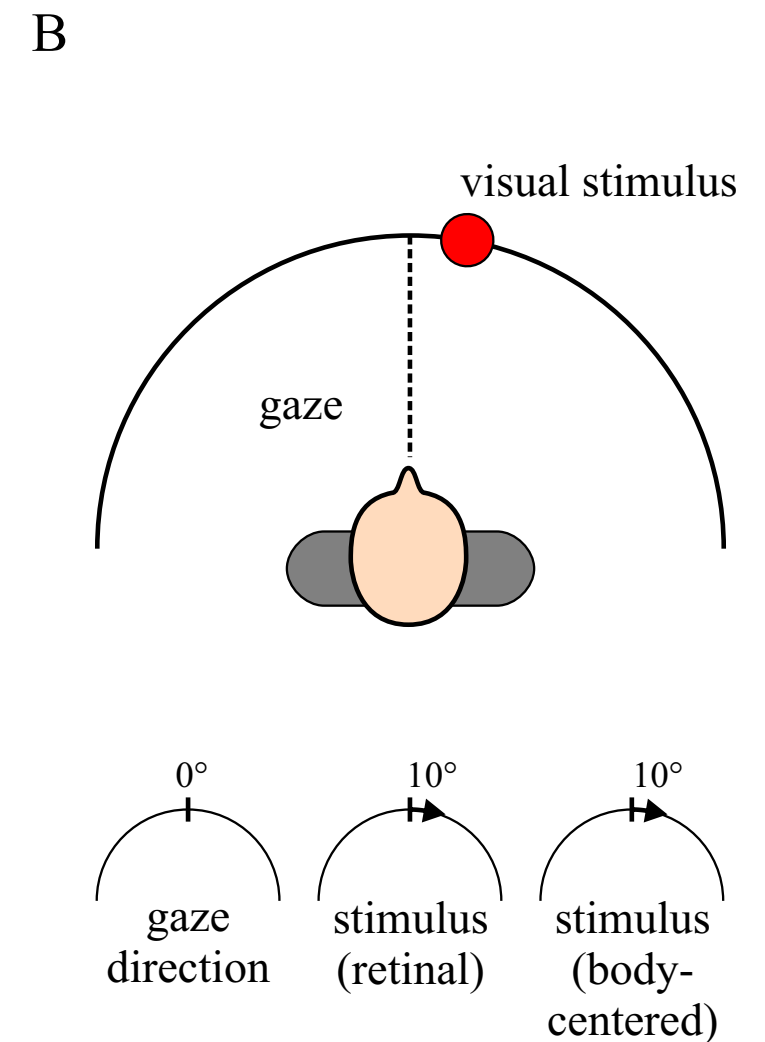
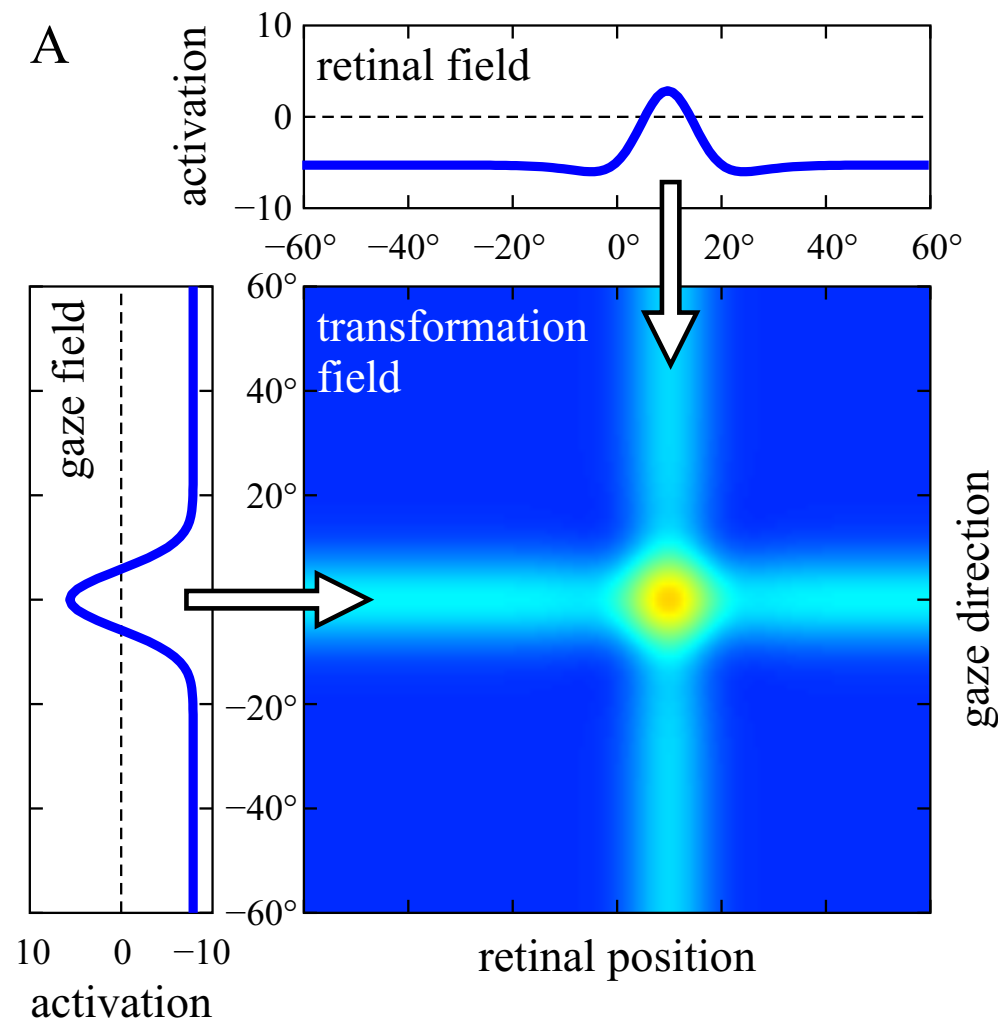
# coordinate transformations

- expand into a 2D field
- free output connectivity to implement any mapping



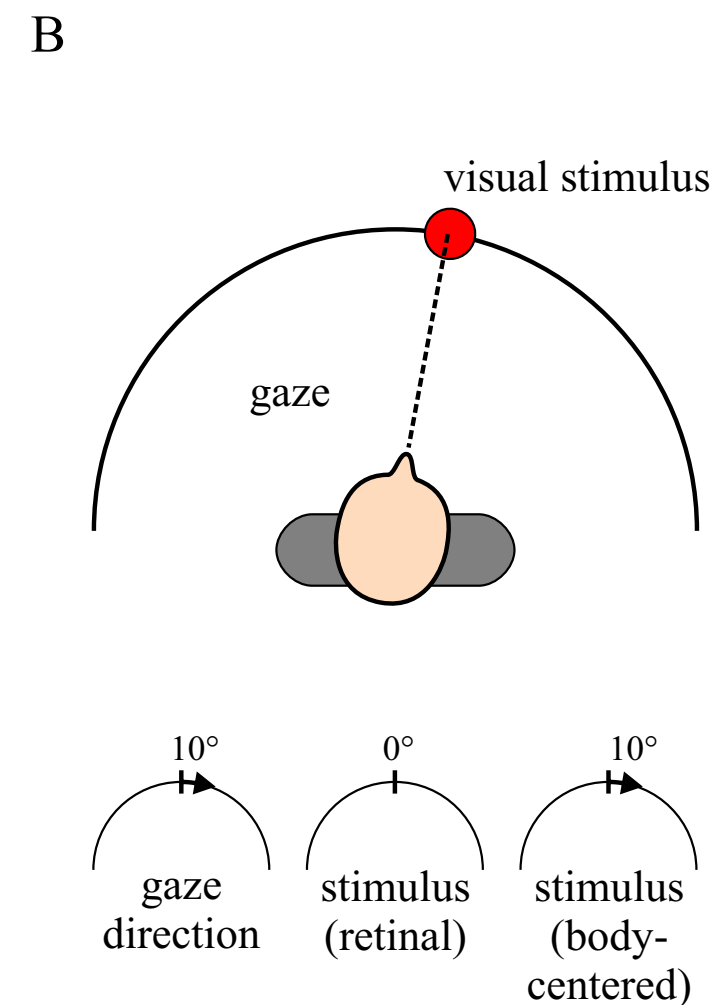
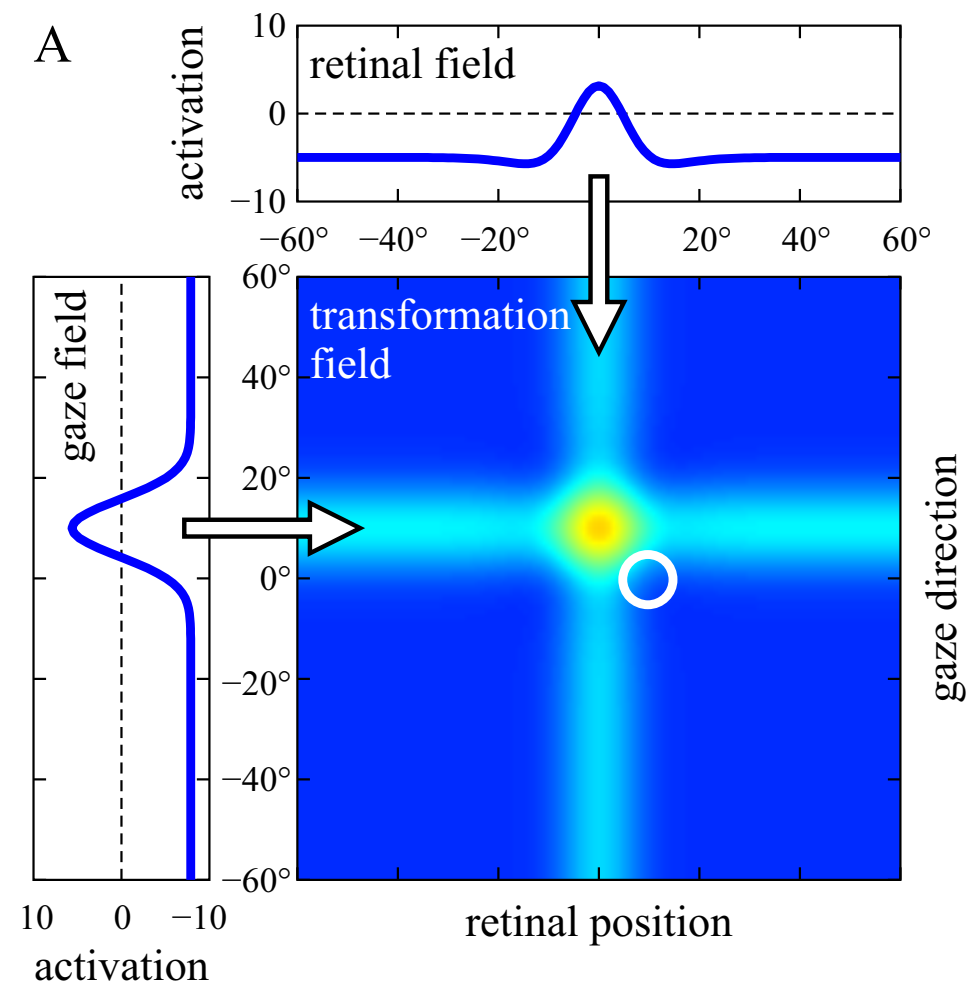
[Slides adapted from Sebastian Schneegans,  
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# coordinate transformations



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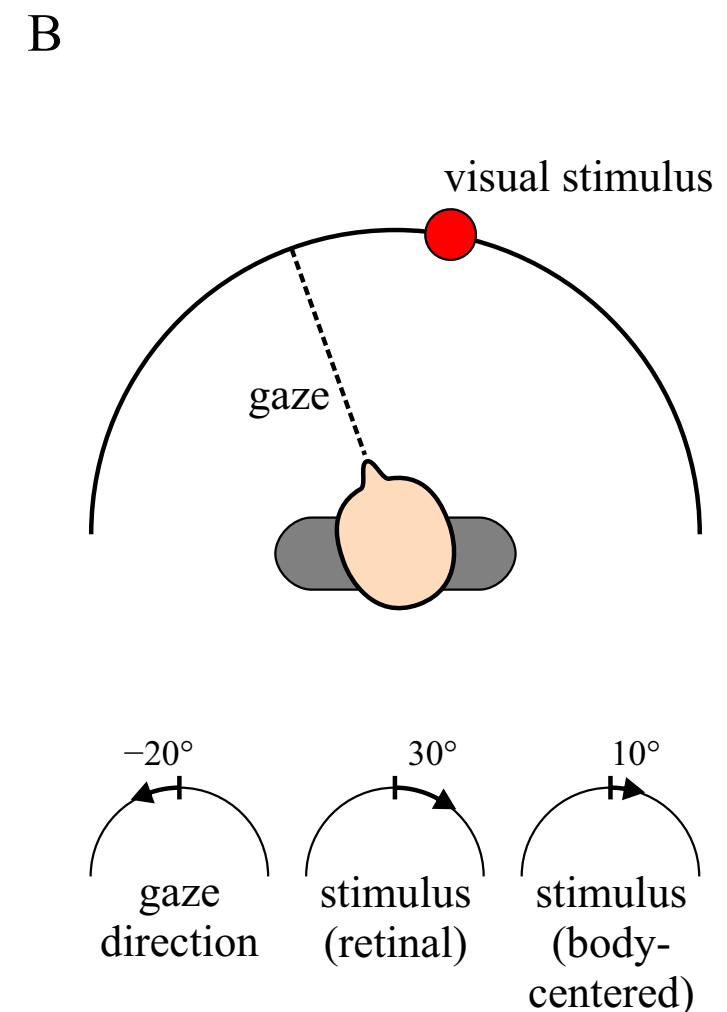
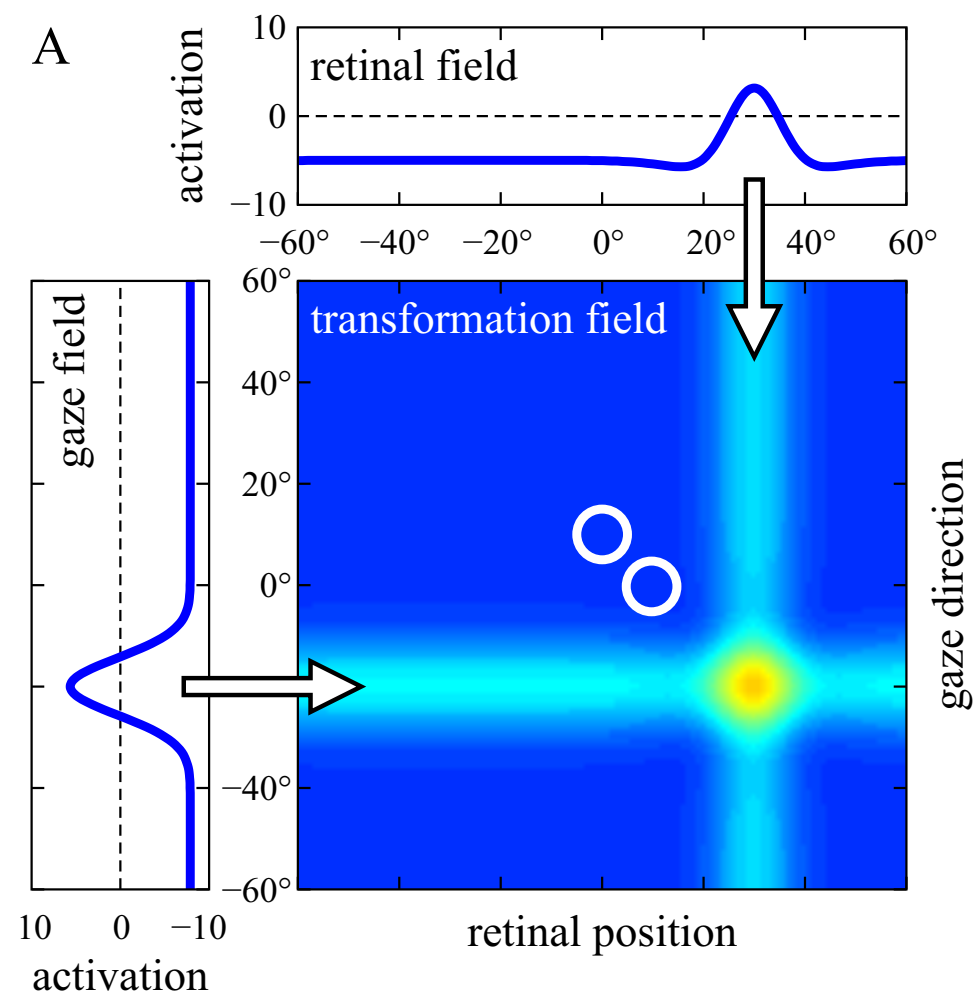
# coordinate transformations



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see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

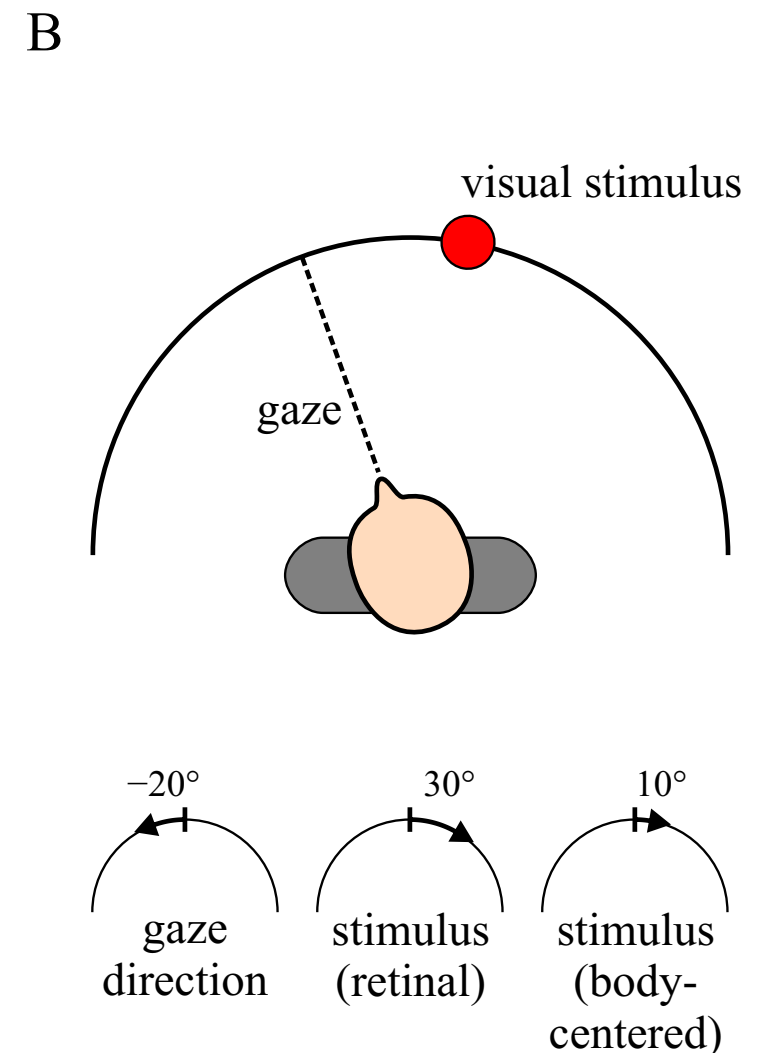
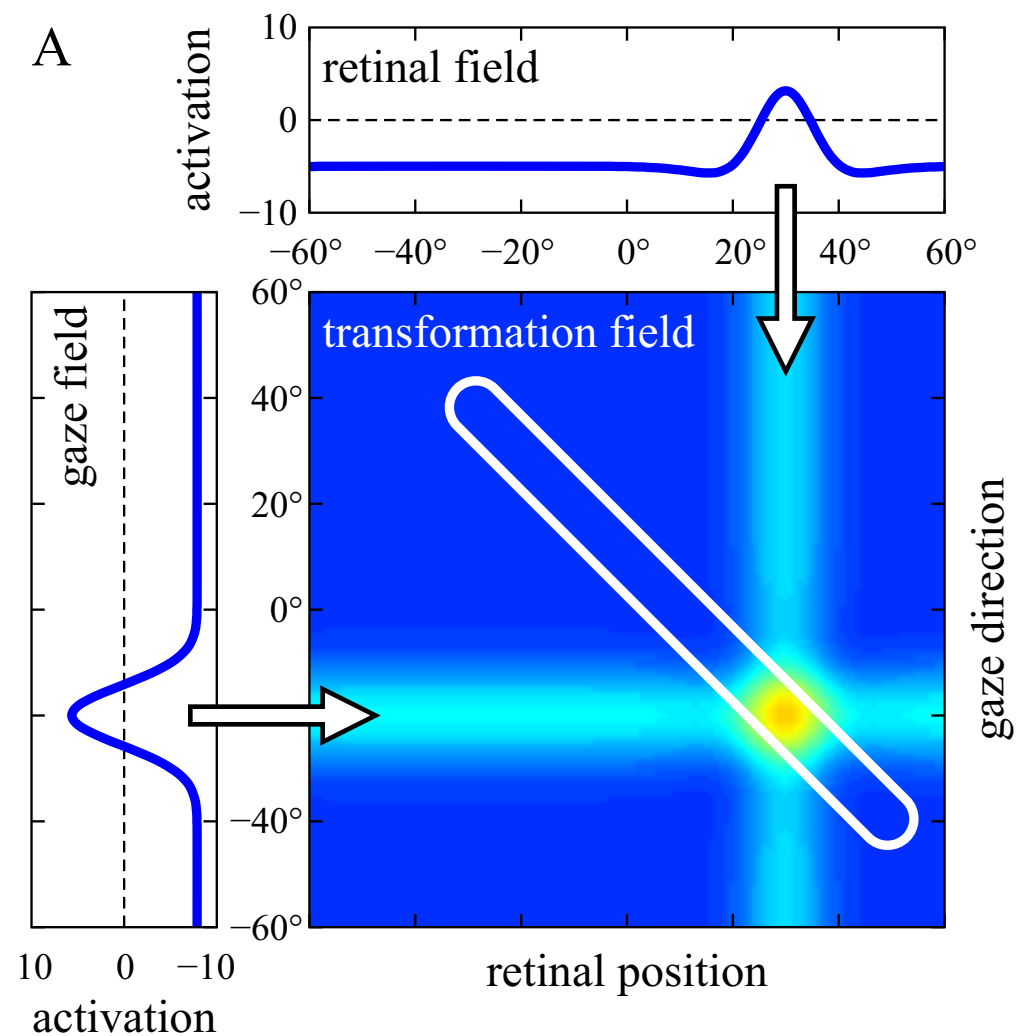


# coordinate transformations



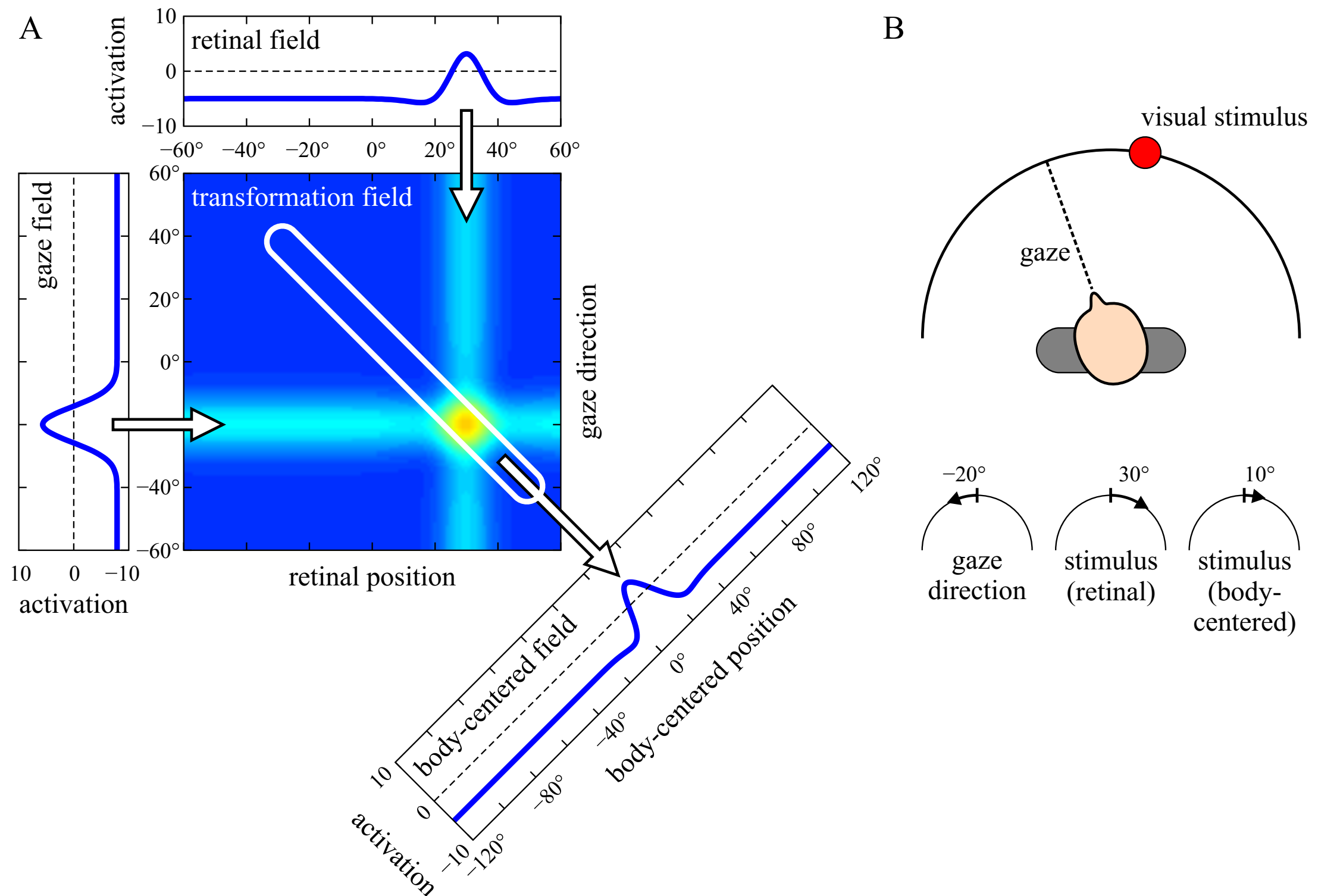
[Slides adapted from Sebastian Schneegans, see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

# coordinate transformations



[Slides adapted from Sebastian Schneegans,  
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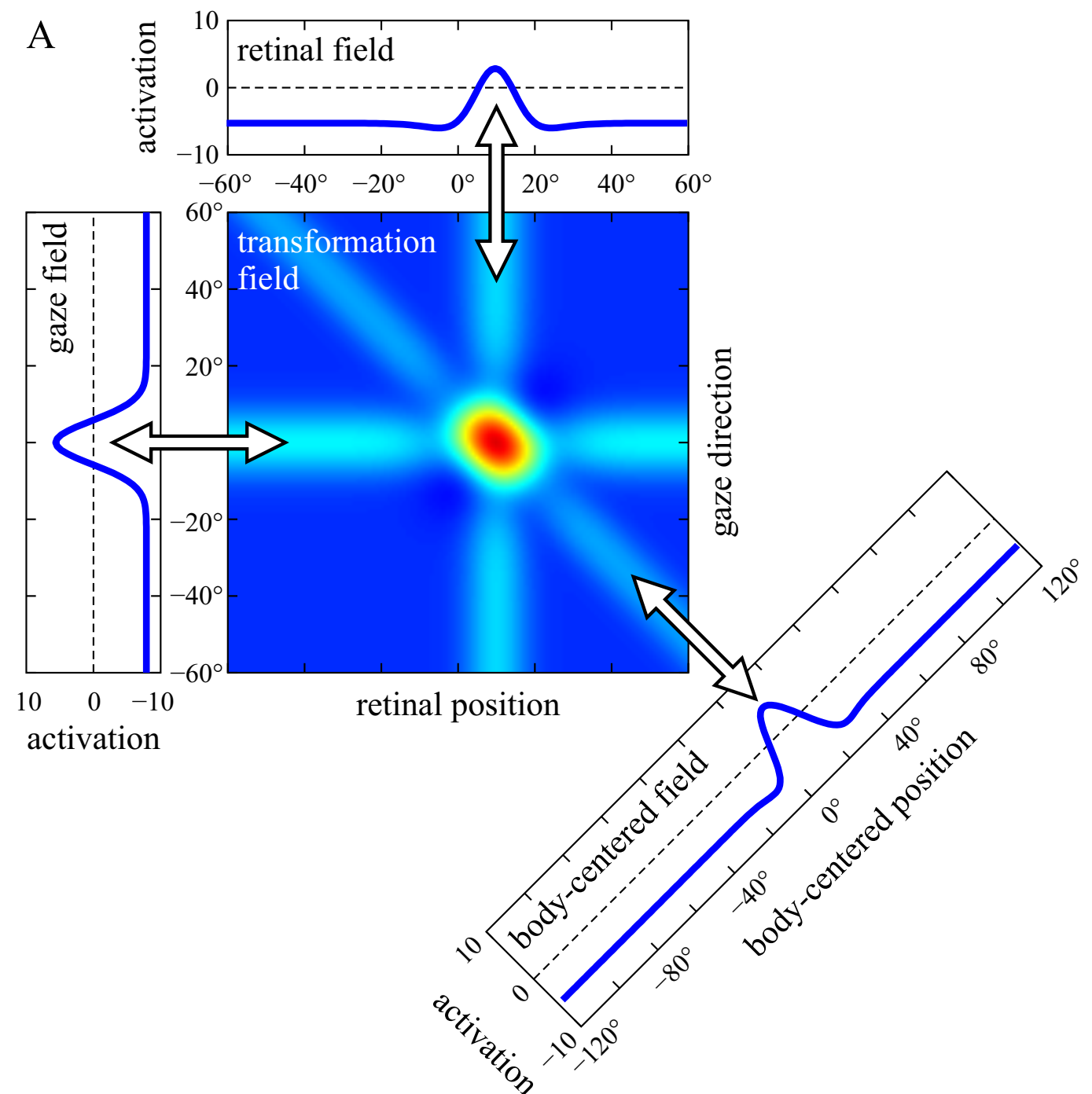
# coordinate transformations



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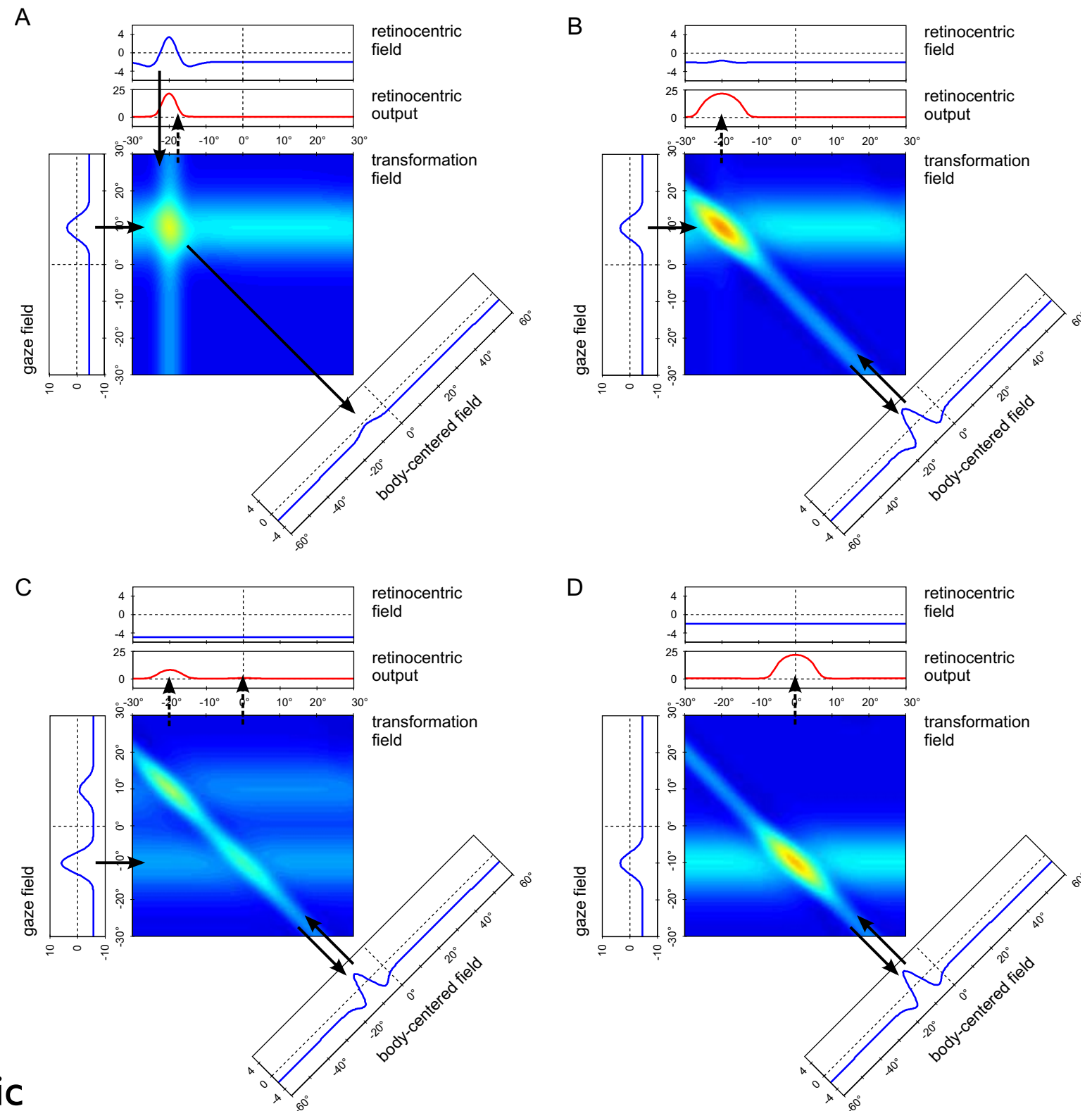
# coordinate transformations

- bi-directional coupling: reversing the transformations



[Slides adapted from Sebastian Schneegans,  
see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

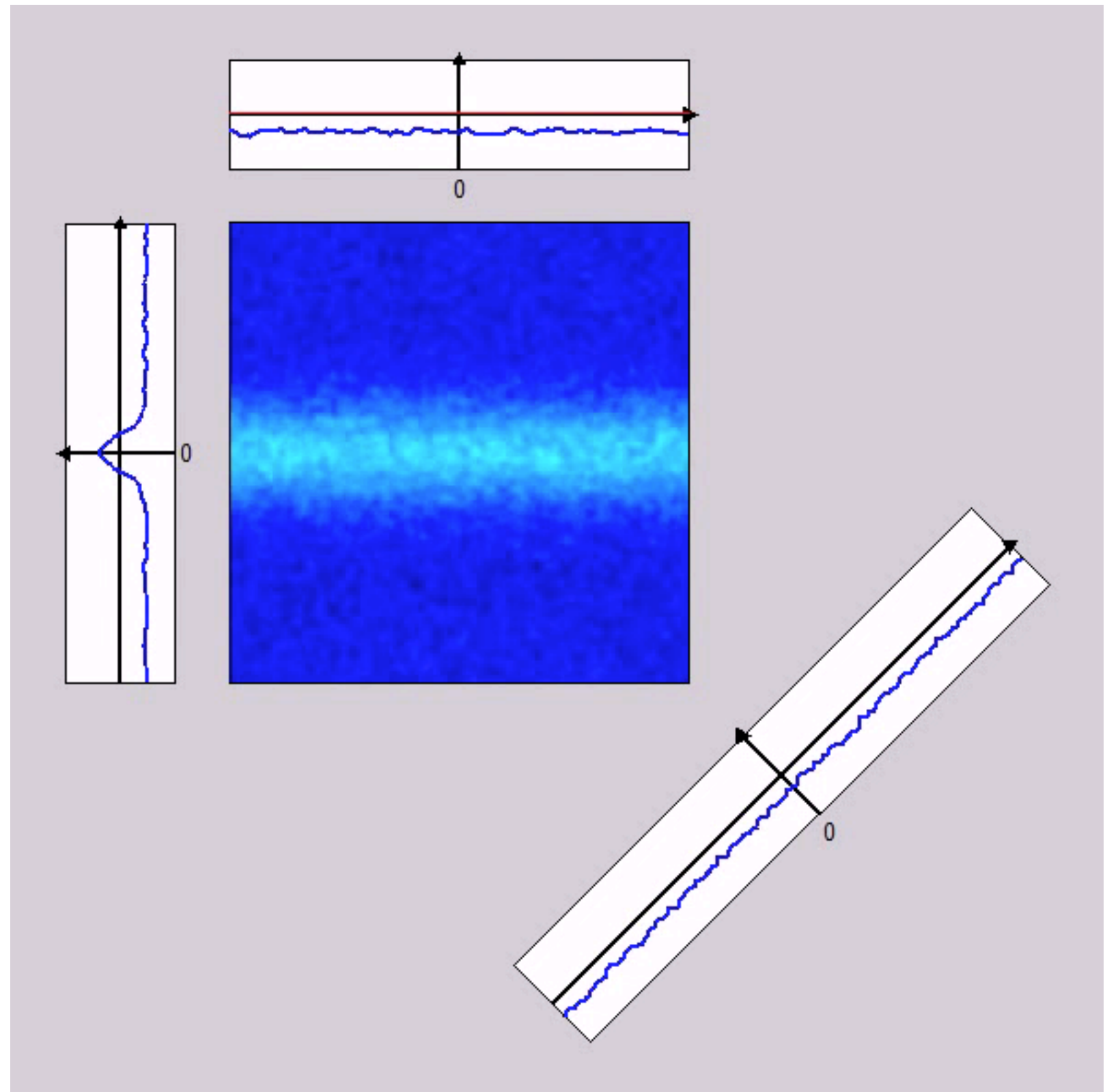
# spatial remapping during saccades

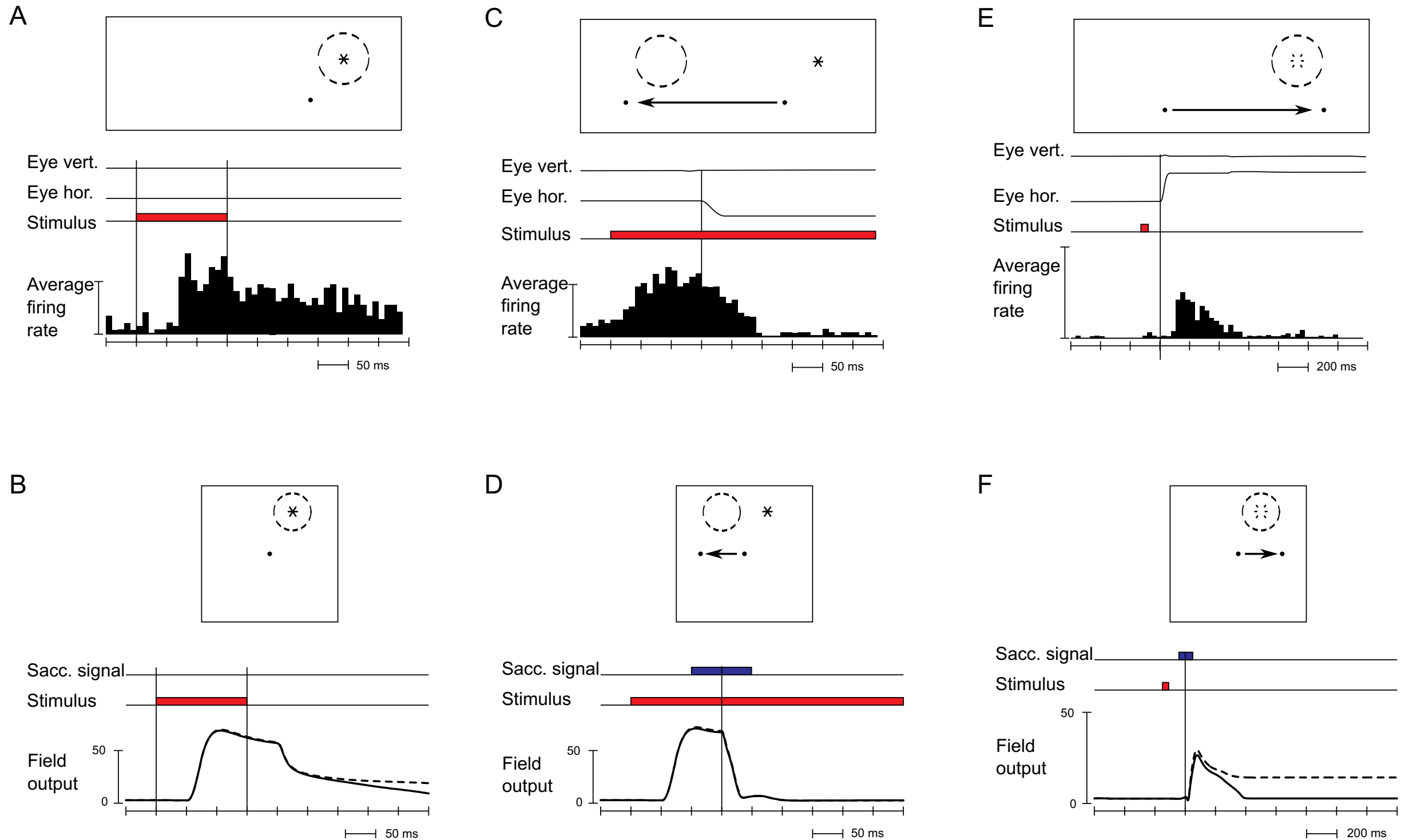


[Slides adapted from Sebastian Schneegans, see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

# Coordinate transformations

- predict retinal location following gaze shift

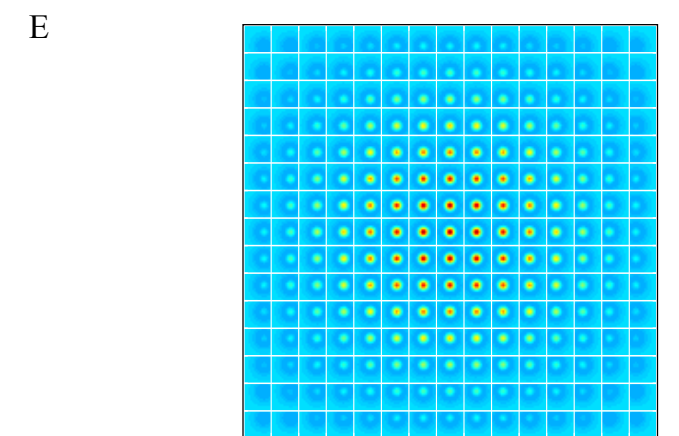
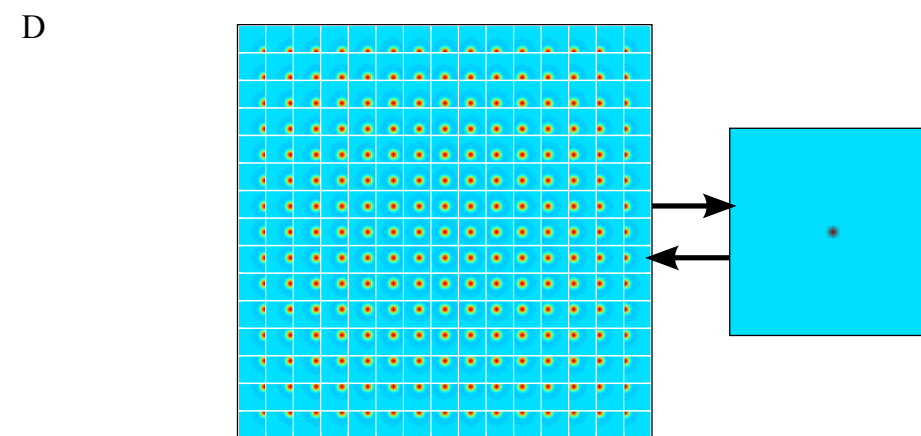
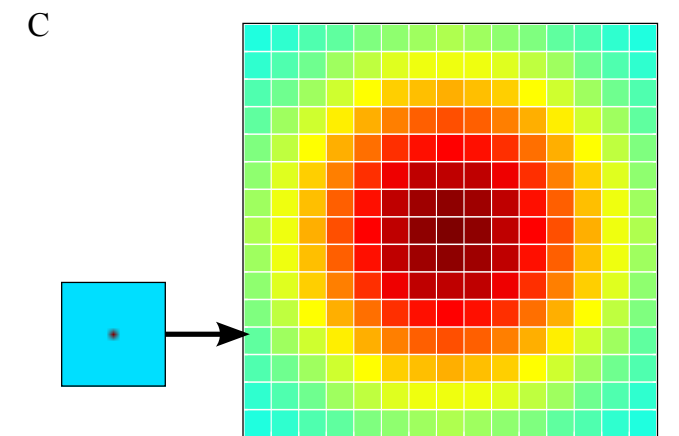
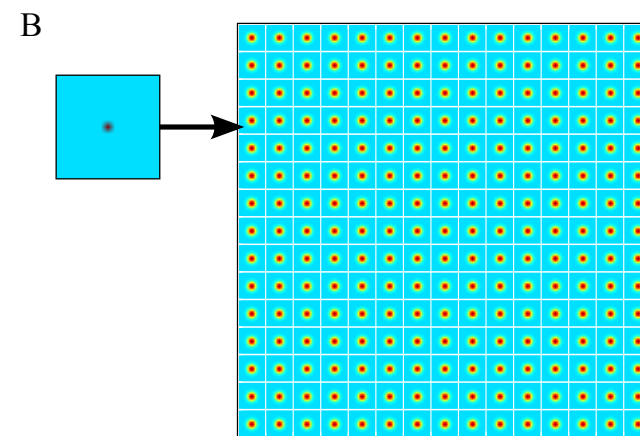
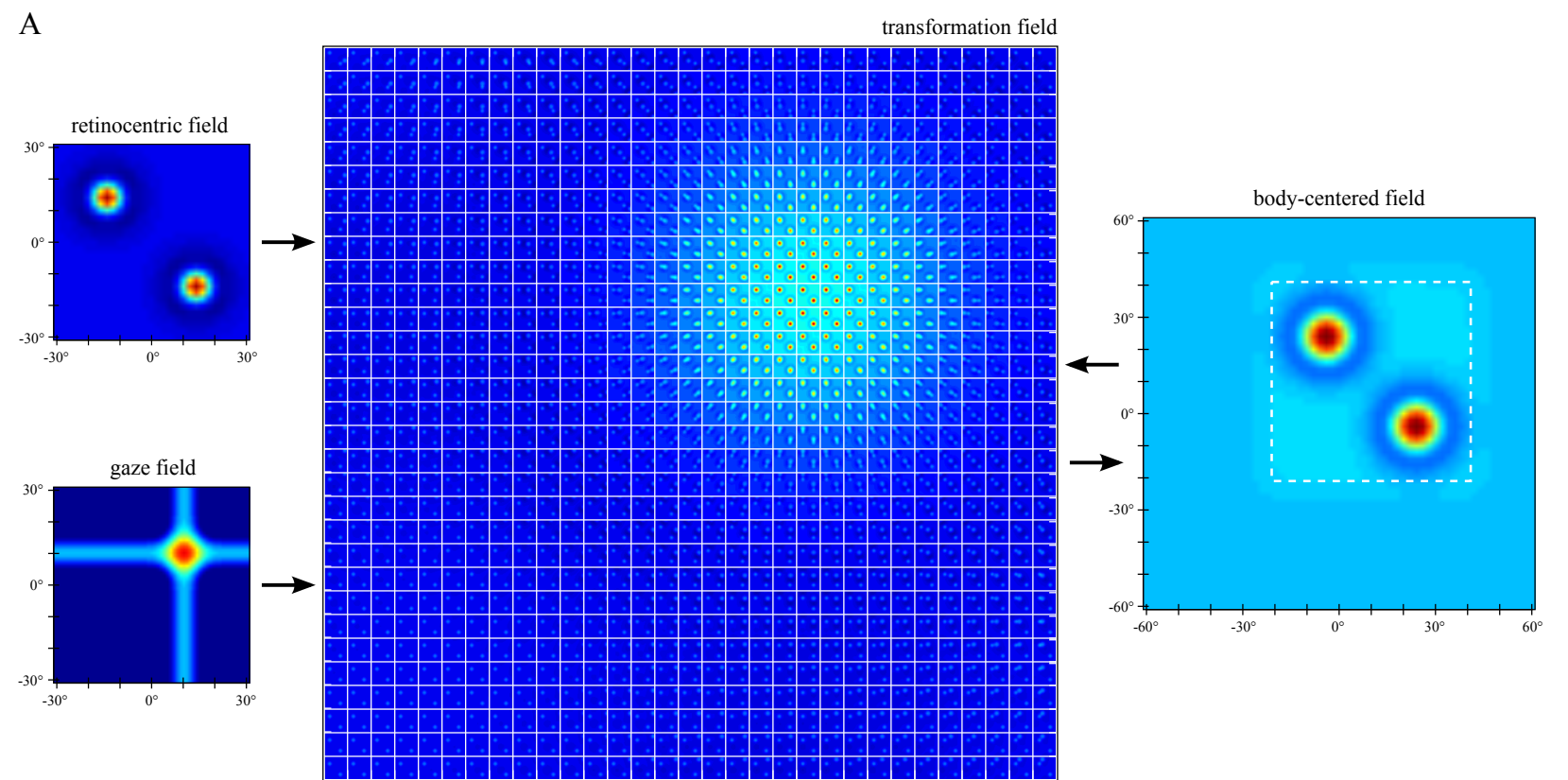




=> accounts for predictive updating of retinal representation



# Scaling dimensionality



[Slides adapted from Sebastian Schneegans, see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

# Scaling dimensionality

- example: a single 6-dimensional field is needed to transform the coordinates of a 3D field:
  - 1 feature dimension X 2 spatial dimensions on input side
  - 1 feature dimension X 2 spatial dimensions on output side
- sample each dimension with 100 neurons:  
 $10^{12}$  neurons = entire brain!

# Scaling dimensionality

■ Example: a few features over space

■ color

■ orientation

■ disparity

■ line-length

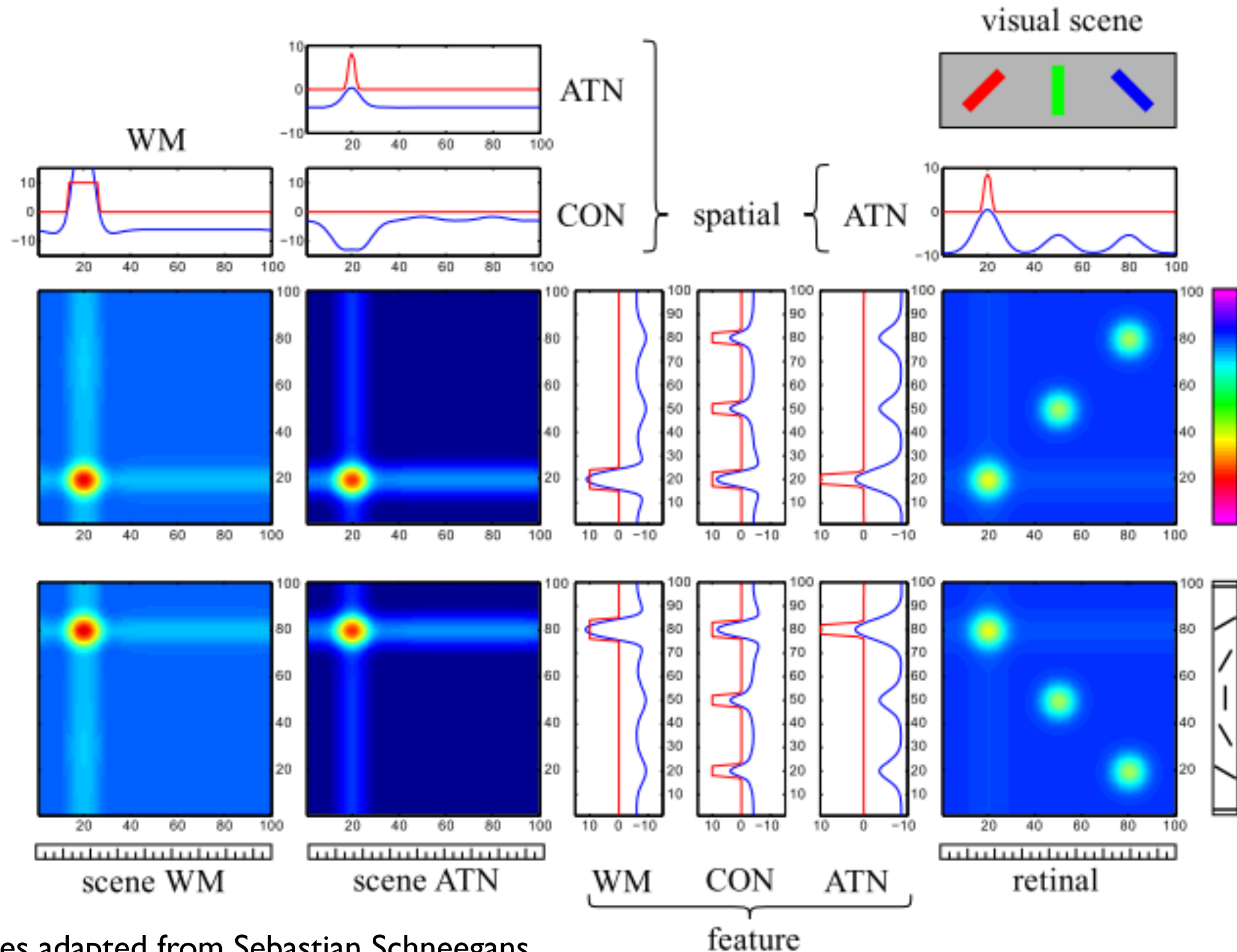
■ 2D space

■  $\Rightarrow$  6 dimensions  $\sim 10^{12}$  neurons!

# Solution

- break down the feature fields into many low dimensional fields... all 3 or maximally 4 dimensional
- coordinate transform only space...
- and bind the features to space by combining the ridge values: operating sequentially!
- => coordinate transforms are at the origin of the binding bottleneck

# Memorization of left item

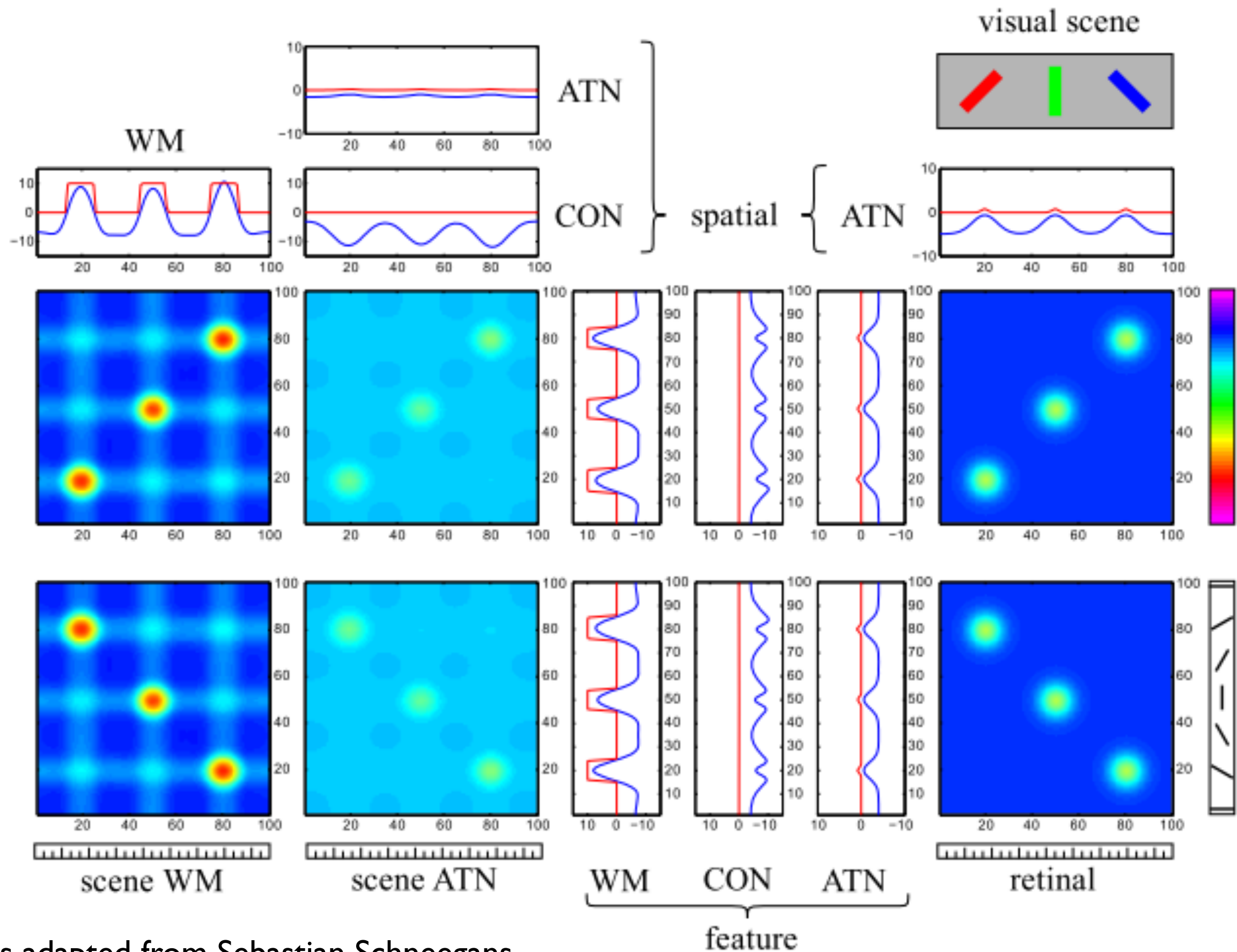


[Slides adapted from Sebastian Schneegans, see Schneegans, Spencer, Schöner, Chapter 9 of Dynamic Field Theory-A Primer, OUP, 2015]





# Post sequential memorization of all three items



[Slides adapted from Sebastian Schneegans, see Schneegans, Spencer, Schöner, Chapter 9 of Dynamic Field Theory-A Primer, OUP, 2015]



# Conclusion: multi-dimensional fields

- enable new cognitive functions that derive from association and cannot be realized by synaptic networks
- instantaneous association or linkage (referral) enabling dimensional cuing
- cued recall
- coordinate transforms instantaneous real-time
- representing associations, rules etc. in a manner that can be activated/deactivated

# Conclusions continued

- need to span only a limited number of dimensions (2 and 3), which are expanded by binding through space
- span by small number of neurons

# Outlook

- multi-dimensional fields help us move toward higher cognition