



# **COMPUTER VISION: DEEP LEARNING LAB COURSE**

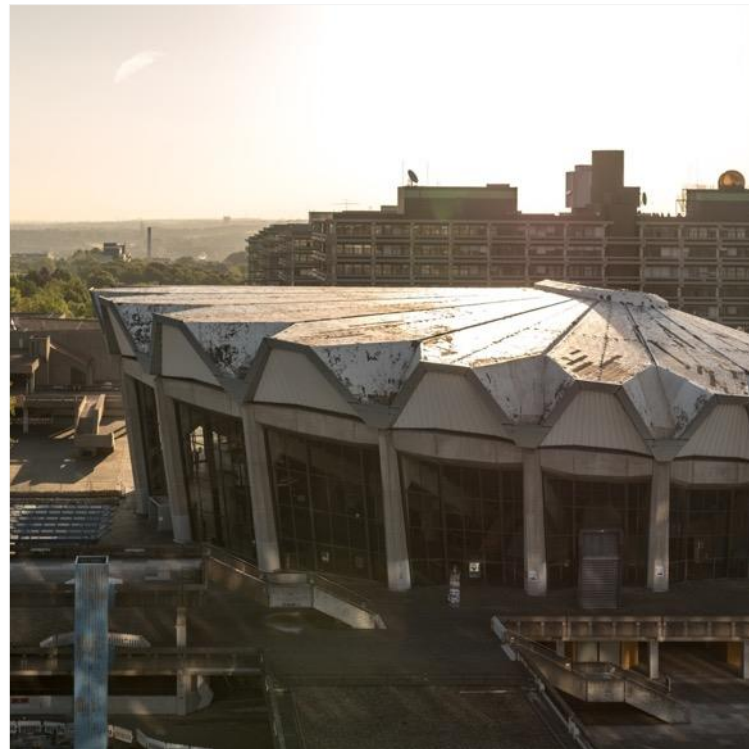
## **DAY 3 – CONVOLUTIONAL NEURAL NETWORKS**

SEBASTIAN HOUBEN

# Schedule

## Today

- Neural Nets
- Training of Neural Nets
- Gradient Computation
- Deep Neural Nets
- Bare Necessities for Training Deep Neural Nets
- Tensorflow

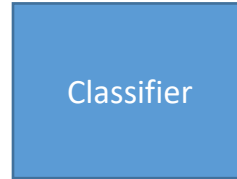


# Neural Net – Multilayer Perceptron



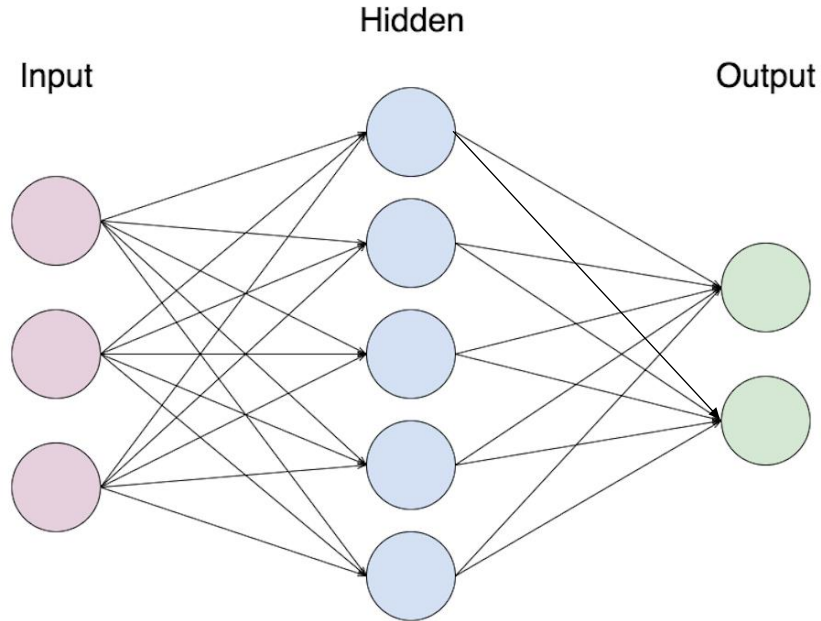
Feature Extraction

$$\begin{bmatrix} 2 \\ 5 \\ 1 \\ 8 \end{bmatrix}$$

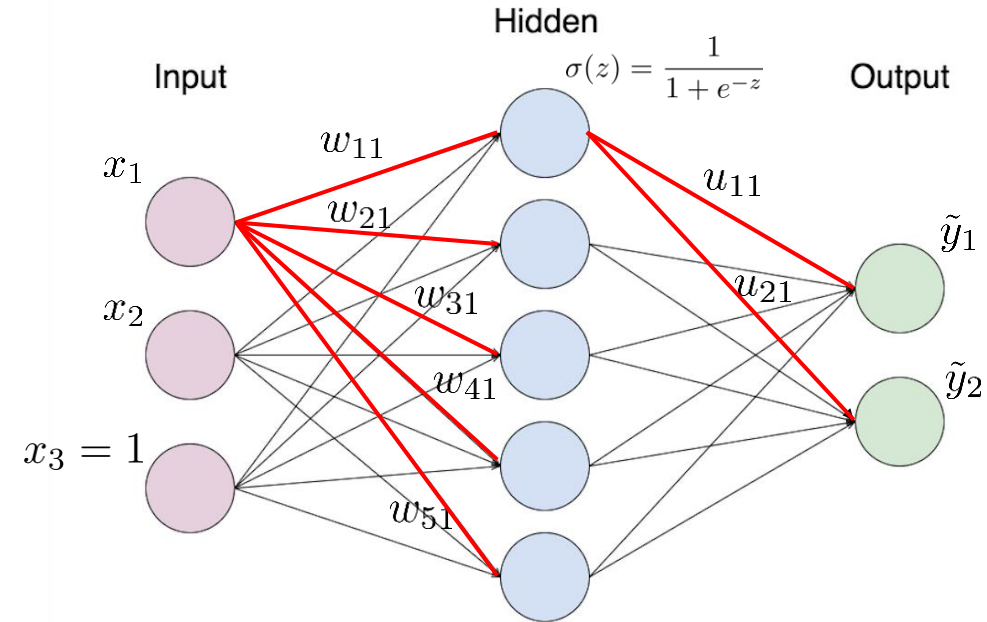


{cat,dog}

# Neural Net – Multilayer Perceptron



# Neural Net – Multilayer Perceptron



$$W := \begin{pmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \\ w_{31} & w_{32} & w_{33} \\ w_{41} & w_{42} & w_{43} \\ w_{51} & w_{52} & w_{53} \end{pmatrix}$$

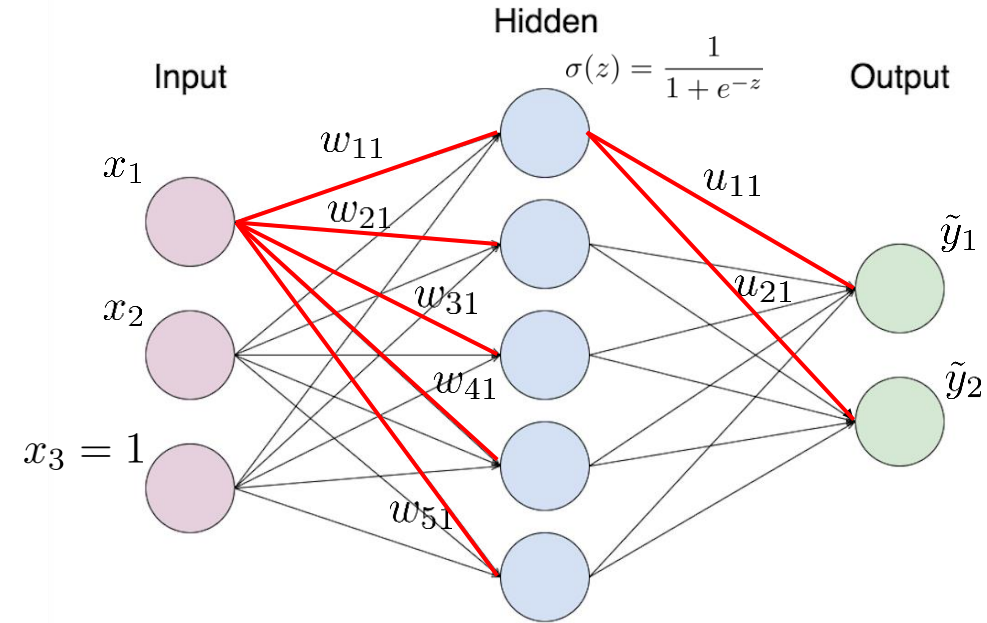
$$U := \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} \\ u_{21} & u_{22} & u_{23} & u_{24} & u_{25} \end{pmatrix}$$

$$x := \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \quad \tilde{y} := \begin{pmatrix} \tilde{y}_1 \\ \tilde{y}_2 \end{pmatrix}$$

$$\tilde{y} = U \sigma(Wx)$$



# Neural Net – Multilayer Perceptron



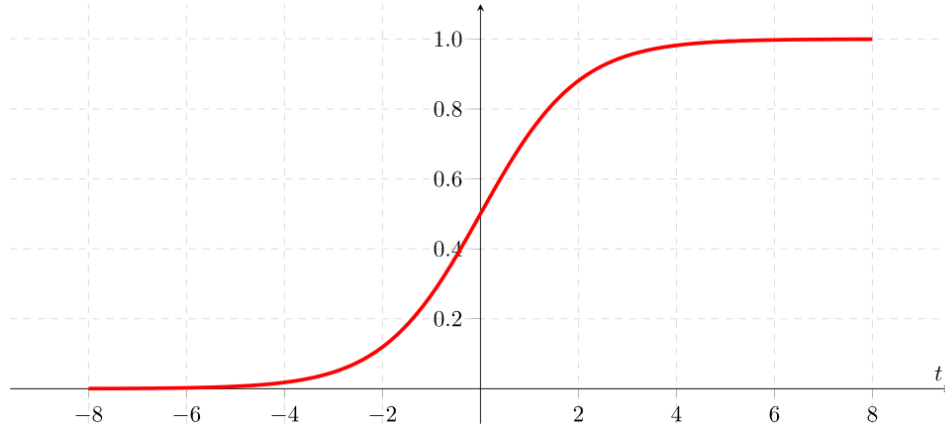
$$W := \begin{pmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \\ w_{31} & w_{32} & w_{33} \\ w_{41} & w_{42} & w_{43} \\ w_{51} & w_{52} & w_{53} \end{pmatrix}$$

$$U := \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} \\ u_{21} & u_{22} & u_{23} & u_{24} & u_{25} \end{pmatrix}$$

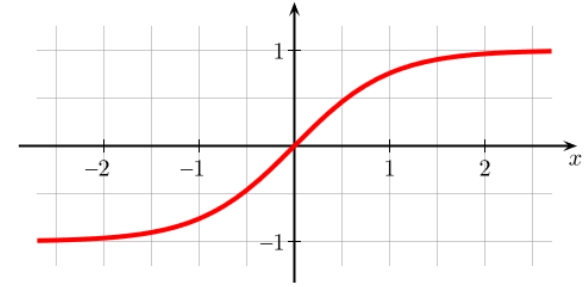
$$x := \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} \quad \tilde{y} := \begin{pmatrix} \tilde{y}_1 \\ \tilde{y}_2 \end{pmatrix} \quad y := \begin{pmatrix} y_1 \\ y_2 \end{pmatrix}$$

$$\tilde{y} = U \sigma(Wx)$$

# Neural Net – Non-Linearities

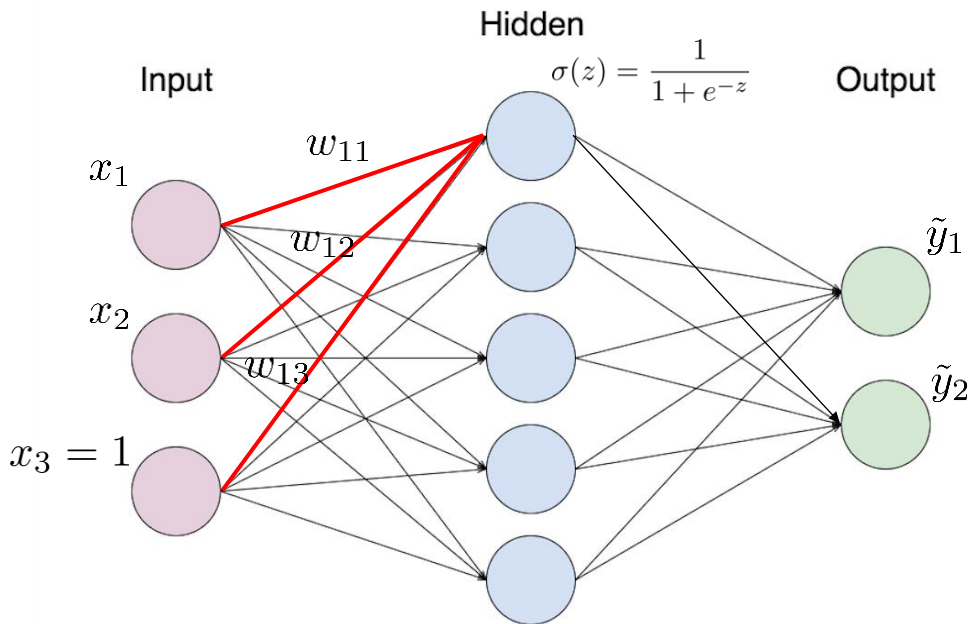


$$\sigma(z) = \frac{1}{1 + e^{-z}} = \frac{1}{2} \left( 1 + \tanh \frac{z}{2} \right)$$
$$\sigma'(z) = \sigma(z)(1 - \sigma(z))$$



$$\tanh'(z) = 1 - \tanh^2(z)$$

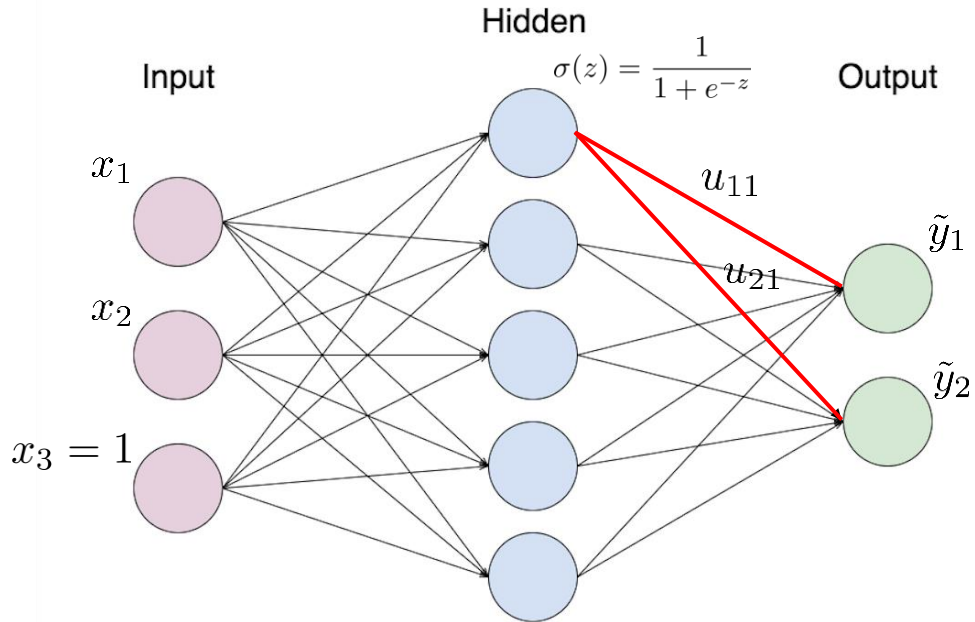
# Neural Net – Interpretation



- Input norm should be limited
- Nothing should fire for zero input
- Shift by mean and normalize by standard deviation (over training set)
$$x := \frac{\hat{x} - \text{mean}}{\text{std}}$$
- Hidden neuron reacts if input is similar to weight vector
- Hidden neurons code regions of feature space
- More hidden neurons can divide the feature space in more regions



# Neural Net – Interpretation



- Second layer weights control output for each region
- Net can approximate each continuous function
- Polynomials can
- Sine functions can (Fourier series)

# Neural Net – Training

- Training data:  $(x^{(i)}, y^{(i)}); i = 1, \dots, n; y^{(i)} \in \{0; 1\}^m; x^{(i)} \in \mathbb{R}^d$
- Predictions (!):  $\tilde{y}^{(i)} = \sigma \left( U \sigma \left( W x^{(i)} \right) \right)$
- Accuracy:  $\frac{1}{n} \sum_{i=0}^n \mathbf{1} \left[ \underset{j}{\operatorname{argmax}} \tilde{y}_j^{(i)} = \underset{j}{\operatorname{argmax}} y_j^{(i)} \right]$
- Loss: 
$$L(x, y, W, U) = \sum_{i=1}^n \sum_{j=1}^m \left( \tilde{y}_j^{(i)} - y_j \right)^2$$
$$= \sum_{i=1}^n \sum_{j=1}^m \left( \sigma \left( U \sigma \left( W x^{(i)} \right) \right)_j - y_j \right)^2$$
- Training: 
$$W^{(k+1)} = W^{(k)} - \eta \frac{\partial}{\partial W} L(x, y, W^{(k)}, U^{(k)})$$
$$U^{(k+1)} = U^{(k)} - \eta \frac{\partial}{\partial U} L(x, y, W^{(k)}, U^{(k)})$$

$$y^{(i)} = \begin{pmatrix} 0 \\ \vdots \\ 0 \\ 1 \\ 0 \\ \vdots \\ 0 \end{pmatrix} \quad \tilde{y}^{(i)} = \begin{pmatrix} 0.1 \\ \vdots \\ 0.23 \\ 0.99 \\ 0.61 \\ \vdots \\ 0.44 \end{pmatrix}$$

- $n$  samples
- $m$  classes
- $d$  input size

# Neural Net – Training

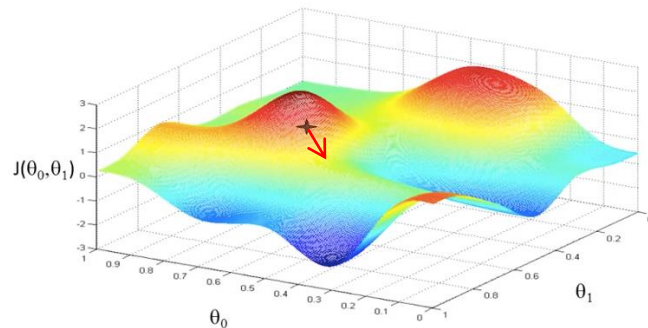
- Simple case:  $d = 1, m = 1$

$$L(x, y, w, u) = \sum_{i=1}^n \left( \sigma \left( u \sigma \left( w x^{(i)} \right) \right) - y \right)^2$$

$$\frac{\partial}{\partial w} L(x, y, w, u) = \sum_{i=1}^n 2 \left( \sigma \left( u \sigma \left( w x^{(i)} \right) \right) - y \right) \cdot \sigma' \left( u \sigma \left( w x^{(i)} \right) \right) \cdot u \sigma' \left( w x^{(i)} \right) \cdot x^{(i)}$$

$$\frac{\partial}{\partial u} L(x, y, w, u) = \sum_{i=1}^n 2 \left( \sigma \left( u \sigma \left( w x^{(i)} \right) \right) - y \right) \cdot \sigma' \left( u \sigma \left( w x^{(i)} \right) \right) \cdot \sigma \left( w x^{(i)} \right)$$

- Vanishing Gradient



- $n$  samples
- $m$  classes
- $d$  input size

# Neural Net – Training

$$W^{(k+1)} = W^{(k)} - \eta \frac{\partial}{\partial W} L(x, y, W^{(k)}, U^{(k)})$$

$$U^{(k+1)} = U^{(k)} - \eta \frac{\partial}{\partial U} L(x, y, W^{(k)}, U^{(k)})$$

- Basic form of gradient:  $\sum_{i=1}^n d(x^{(i)}, y^{(i)}, W, U)$

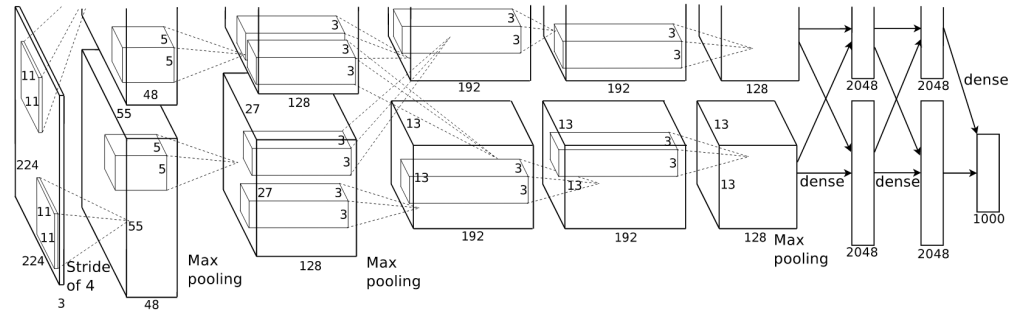
- Gradient descent:  $W^{(k+1)} = W^{(k)} - \eta \sum_{i=1}^n d(x^{(i)}, y^{(i)}, W^{(k)}, U^{(k)})$

- Stochastic gradient descent:  $W^{(k+1)} = W^{(k)} - \eta d(x^{(i)}, y^{(i)}, W^{(k)}, U^{(k)})$

- Batch gradient descent  $W^{(k+1)} = W^{(k)} - \eta \sum_{i \in \text{BATCH}} d(x^{(i)}, y^{(i)}, W^{(k)}, U^{(k)})$

# Deep Neural Nets

- 3-Layer network can approximate any continuous function
- More layers tend to work better
  - Not quite clear why
  - Handwavy: Natural phenonemons are hierarchically structered
  - Hopefully layers will adapt to those different phenomenons
- Vanishing Gradient Problem
- Many, many parameters



# Deep Neural Nets - Adaptations

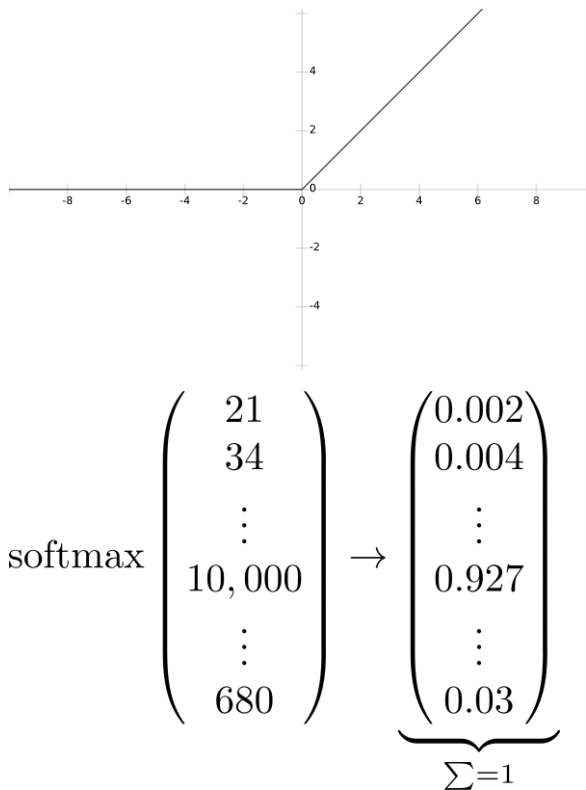
- Non-Linearity:  $\sigma(z) \rightarrow \text{ReLU}(z) = \max\{0, z\}$

Output: 
$$\text{softmax}(z) = \frac{\exp(z_i)}{\sum_k \exp(z_k)}$$

- Loss function:  $(f(x) - y)^2 \rightarrow -\sum_i y_i \log \text{softmax}(z)_i$   
Cross-entropy

- Weight initialization:  $W \sim \mathcal{N}(0, 0.1)$

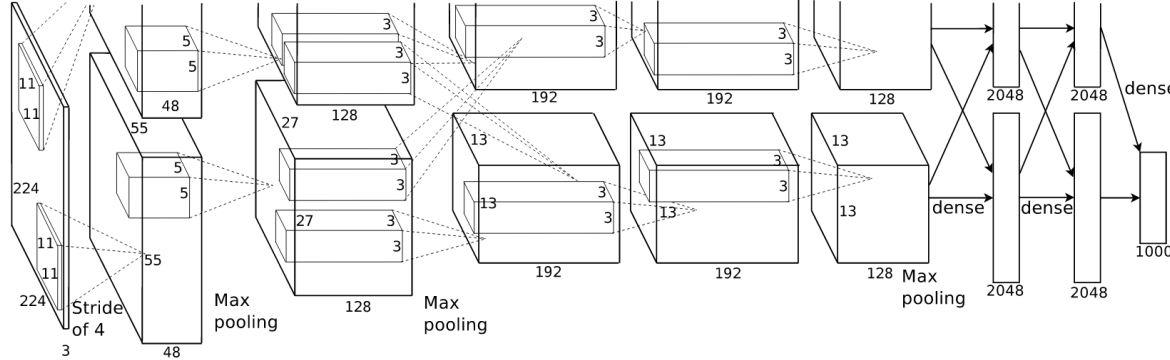
- Data preparation:  $x^{(k)} := \frac{x^{(k)} - \text{mean}(x^{(1)}, \dots, x^{(n)})}{\text{std}(x^{(1)}, \dots, x^{(n)})}$





# Convolutional Neural Nets

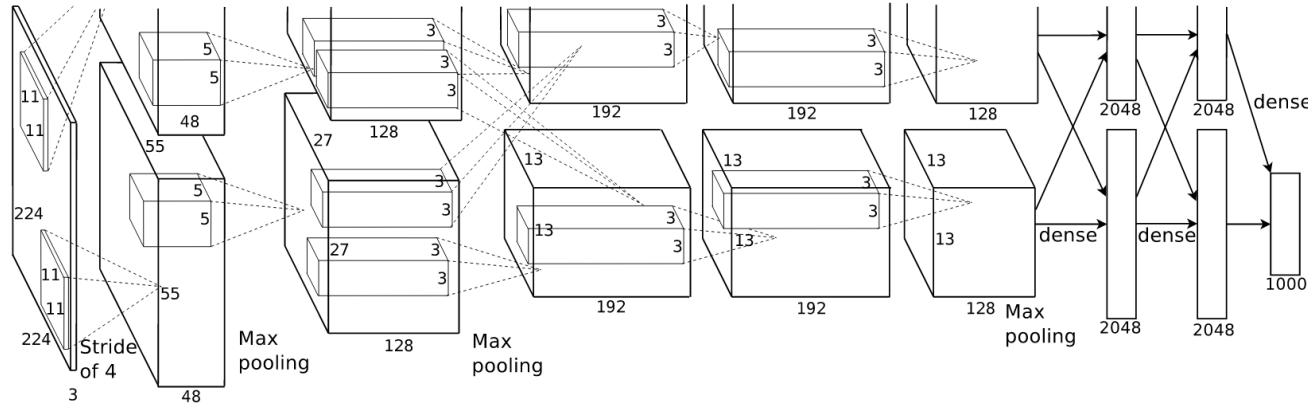
- Neural net with parameter reuse
- Each layer gets an image with  $c$  channels as input
- This is convoluted with  $d$  filters of size  $n \times n \times c$
- resulting in an image with  $d$  channels
- Idea: Find certain local image patches / patterns



Alex Krizhevsky et al.

# Convolutional Neural Nets

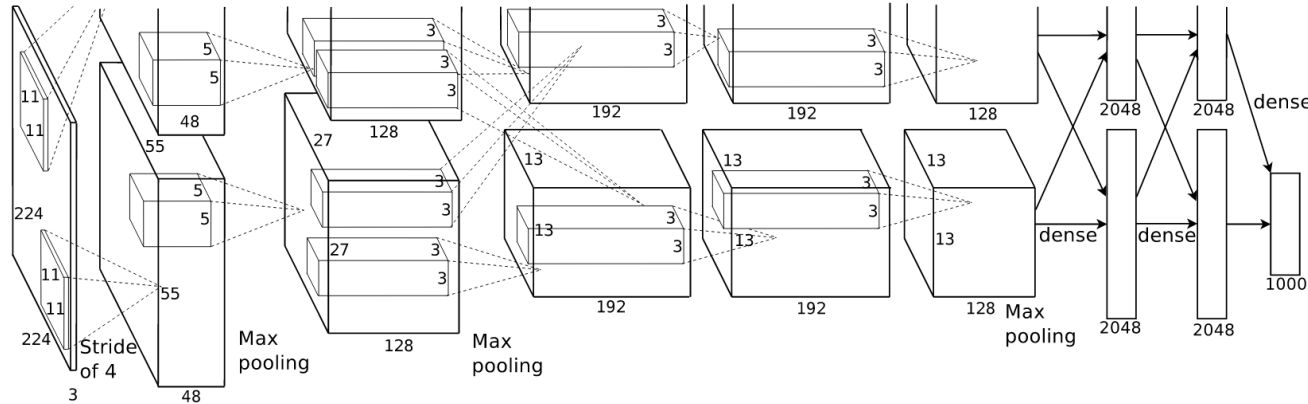
- Idea: Exact location of image patch is not so important
- Compress information
- Maxpool-Layers: Take small window (e.g., 2x2) and only propagate maximum value to next layer



*Alex Krizhevsky et al.*

# Convolutional Neural Nets

- Idea: at the end only relevant information is propagated
- Use classical neural net (fully-connected) to classify results



*Alex Krizhevsky et al.*

# Tensorflow

- Python library for Deep Learning
  - Gradient computation
  - Backpropagation
  - 2000+ operations (e.g., convolution, maxpooling)
- Symbolic computation
  - Write a program that writes (and executes) a program
  - Similar to Numpy



# Tensorflow

- GPU paralellization (via CUDA kernels)
- Caveats:
  - Slightly hard to learn
  - Hard to debug
- Alternatives:
  - PyTorch (Torch)
  - Theano (basically the same)
  - Caffe (C++)
  - Keras (Simplification of Theano / Tensorflow)



# Tensorflow: Layout



```
import tensorflow as tf
import numpy as np

tf.reset_default_graph() # tensorflow internal reset

x = tf.Variable( np.array( [2, 1] ), dtype=tf.float32, name= "x" ) # a variable in the program our program writes
y = tf.constant( np.array( [3, 5] ) , dtype=tf.float32, name= "y" ) # a constant in the program our program writes

z = tf.placeholder( shape=[None, 2], dtype=tf.float32, name= "z" ) # an input in the program our program writes

loss = tf.reduce_sum((x - y + z)**2) # many other numpy operations are implemented

train_step = tf.train.GradientDescentOptimizer(0.1).minimize(loss) # a subroutine that takes one gradient descent step on loss

z_ = np.array([[2,0]])

with tf.Session() as sess:
    sess.run(tf.global_variables_initializer()) # initialize variables in program
    print( loss.eval( feed_dict={z:z_}, x.eval() ) ) # 17.0, [ 2.  1.]
    for k in range(100):
        train_step.run( feed_dict={z:z_} ) # compute loss, compute backpass (derivative), one step downwards

    print( loss.eval( feed_dict={z:z_}, x.eval() ) ) # 9.66338e-13, [1.00000024  4.99999905]
```



# Tensorflow: Checkpointing



```
import tensorflow as tf
import numpy as np

tf.reset_default_graph()                                # tensorflow internal reset

# fancy model implemented here ...

train_step = tf.train.GradientDescentOptimizer(0.1).minimize(loss)

saver = tf.train.Saver()
epoch_cnt = 0

with tf.Session() as sess:
    sess.run(tf.global_variables_initializer())          # initialize variables in program
    saver.restore(sess, tf.train.latest_checkpoint(os.path.dirname(os.path.realpath(__file__)))) # restore last checkpoint
    for # ...
    epoch_cnt += 1
    # optimization going on here ...
    saver.save(sess, os.path.dirname(os.path.realpath(__file__)) + '/tsd_model', global_step=epoch_cnt, write_meta_graph=False)
    # save current state of variables (but not the model)
```

# Tensorflow

- NWHC order
  - stacking of images
  - number, width, height, channel
  - try to adapt to this order



**QUESTIONS?  
EXERCISES.**