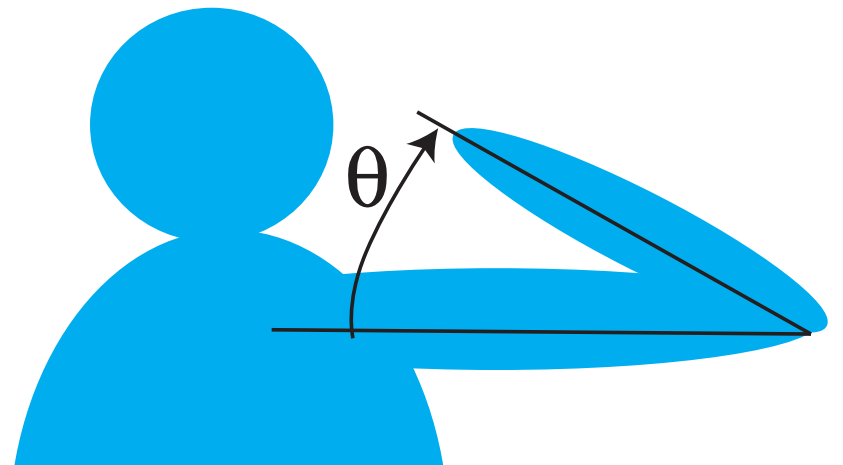


# Human motor control

Gregor Schöner

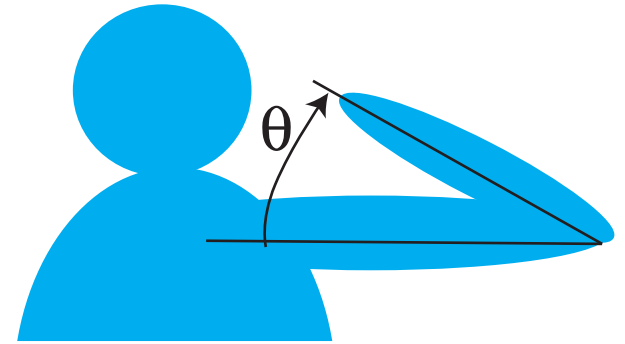
# Human motor control

- human movement is highly compliant...



# Is posture “controlled”?

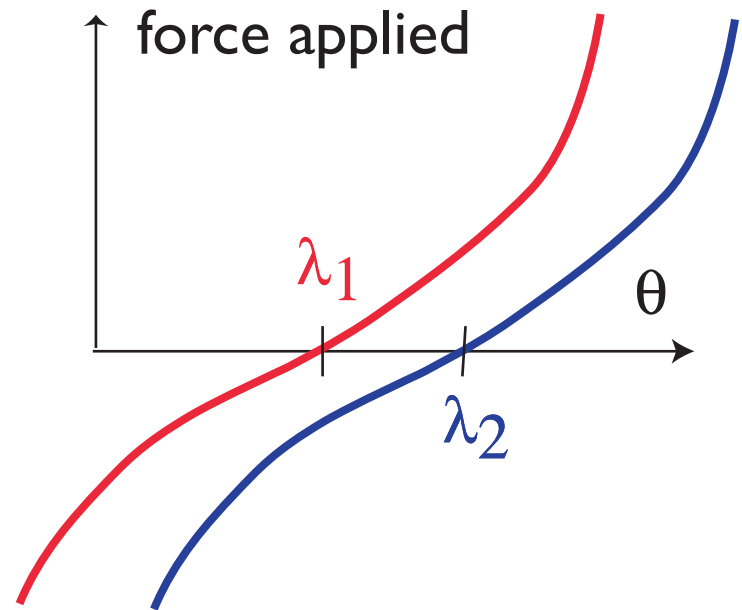
- the elbow does not behave like a passive mechanical system with a free joint at the elbow:  $J\ddot{\theta} = 0$ 
  - where  $J$  is inertial moment of forearm (if upper arm is held fixed)
- Instead, the elbow resists, when pushed => there is active control = stabilization of the joint



=>experiment

# the mass spring model

- Anatol Feldman has figured out, what the macroscopic description of this stabilization is



- the invariant characteristic

# the mass-spring model

- this is an elastic force (because it is proportional to position)
- there is also a viscous component (resistance depends on joint velocity)

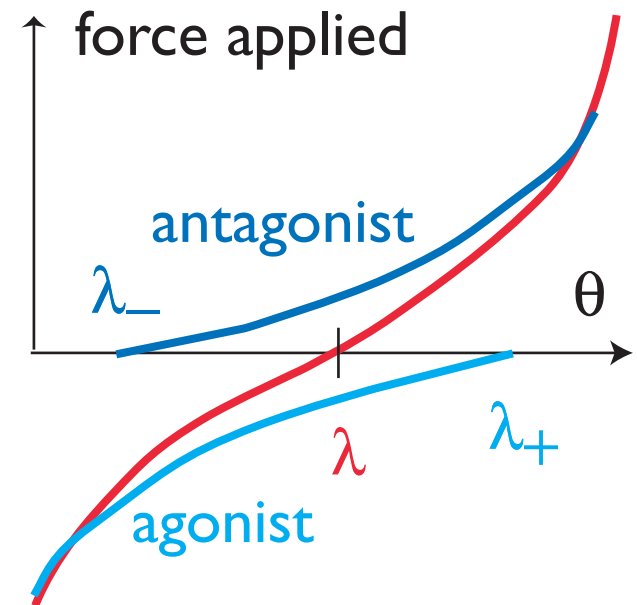
$$J\ddot{\theta} = \boxed{-k(\theta - \lambda) - \mu\dot{\theta}}$$



active torques generated by the muscle

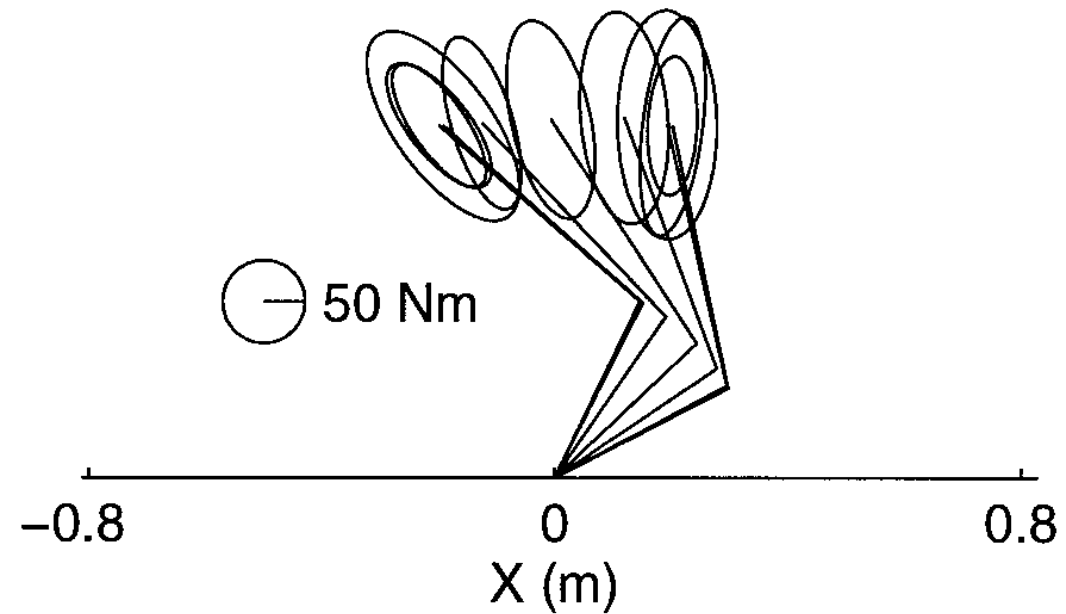
# agonist-antagonist action

- one lambda per muscle
- tested on muscles detached at one end
- co-contraction controls stiffness



# stiffness

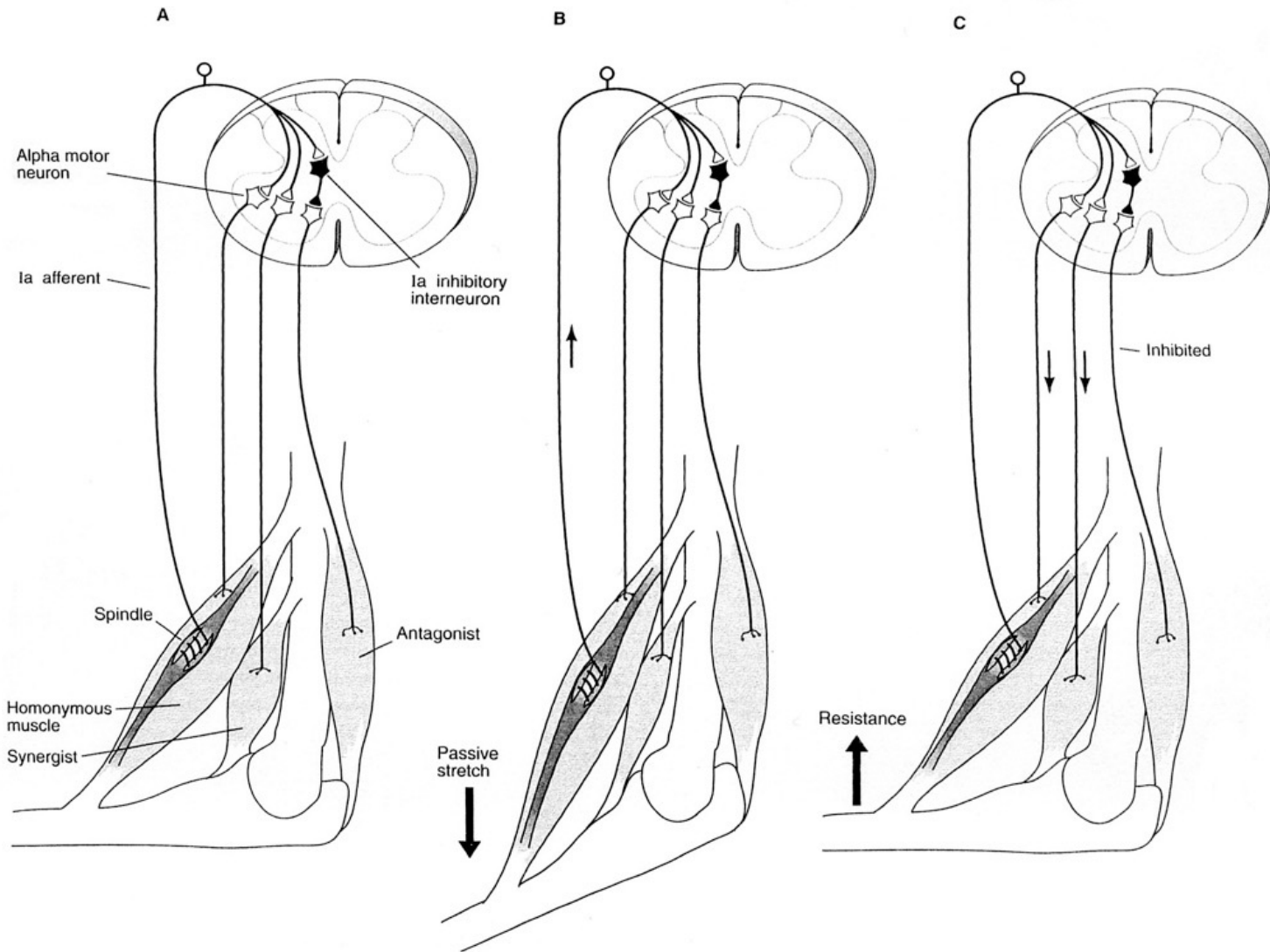
- the stiffness,  $k$ , can be measured from perturbations
- the viscosity “ $\mu$ ” is more difficult to determine



$$J\ddot{\theta} = -k(\theta - \lambda) - \mu\dot{\theta}$$

# neural basis of EP model: spinal reflex loops

■ alpha-gamma reflex loop generates the stretch reflex

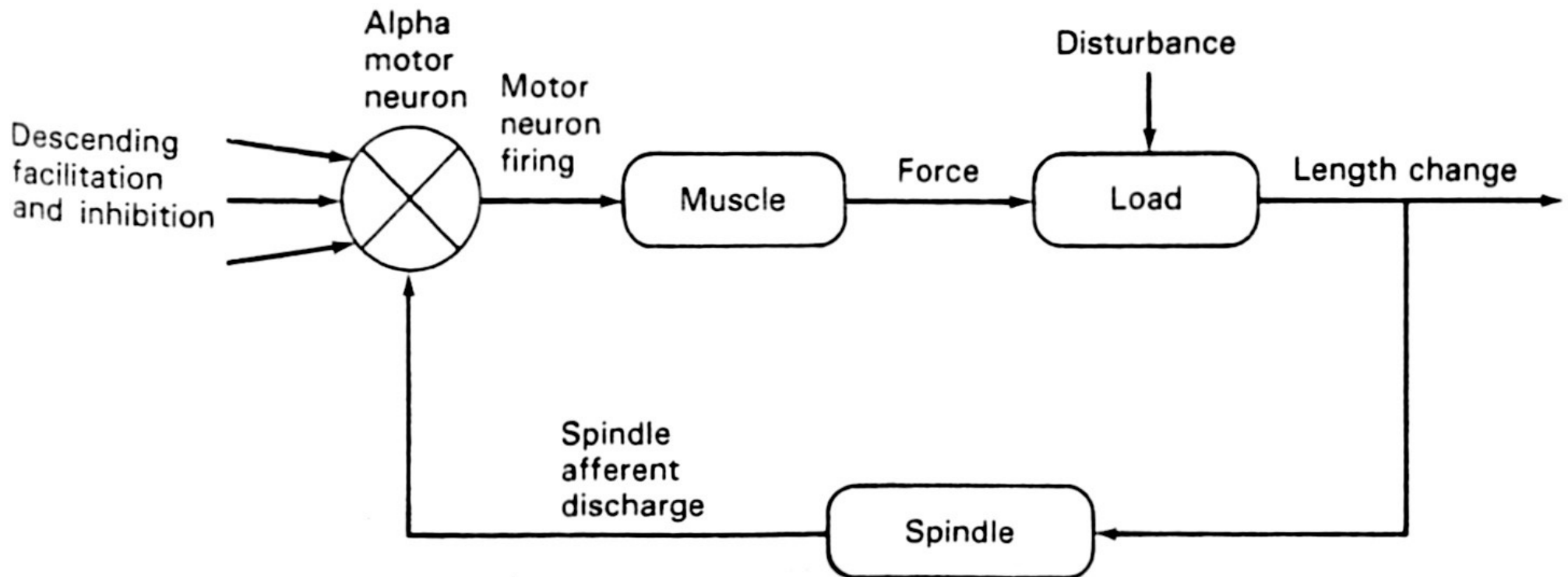


[Kandel, Scharz, Jessell, Fig. 37-11]



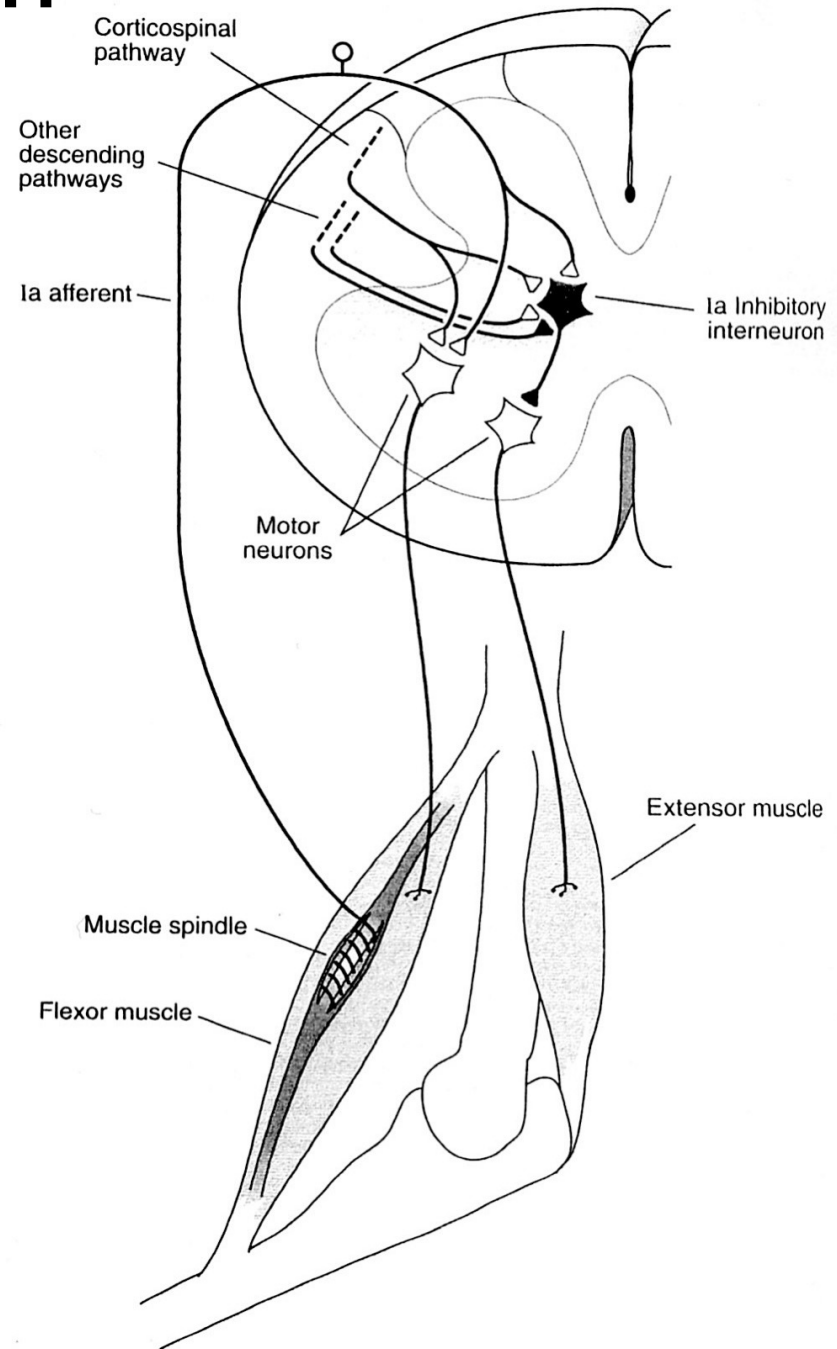
# spinal cord: reflex loops

- the stretch reflex acts as a negative feedback loop



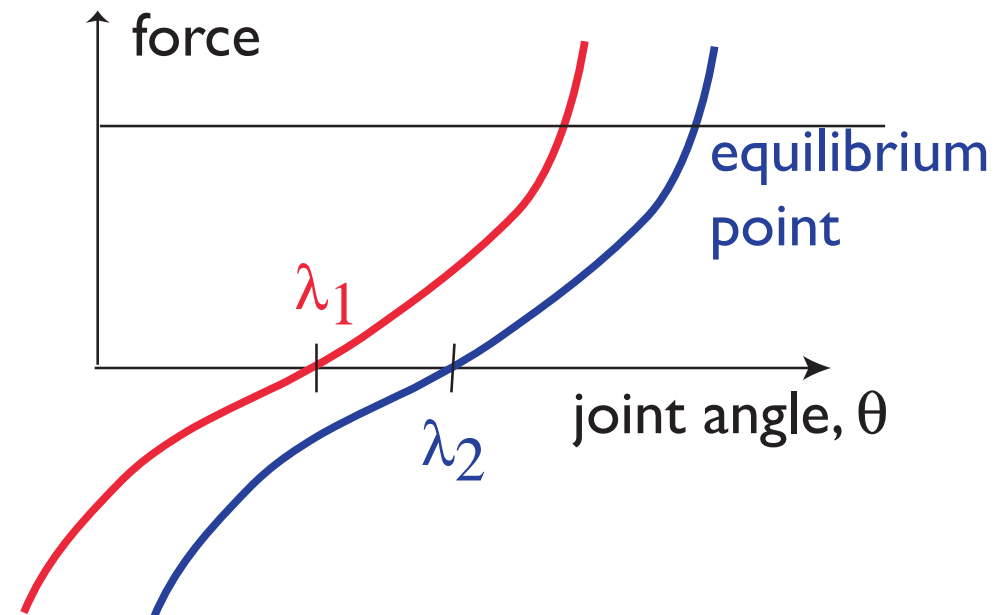
# spinal cord: coordination

- Ia inhibitory interneuron mediates reciprocal innervation in stretch reflex, leading to automatic relaxation of antagonist on activation of agonist



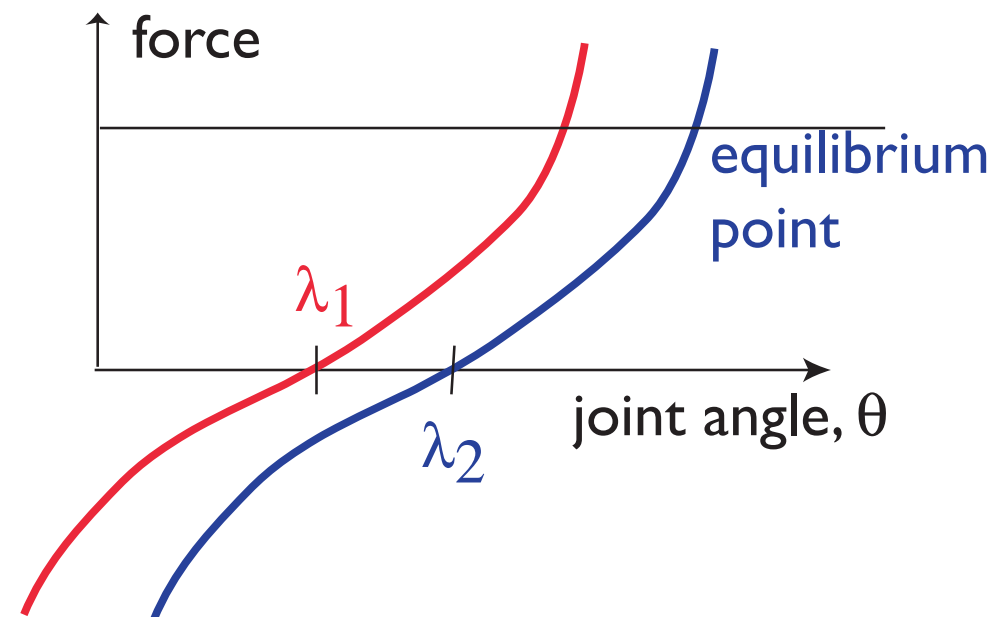
# Movement entails change of posture

- that equilibrium point is shifted during movement so that after the movement, the postural state exists around a new combination of muscle lengths/joint configurations



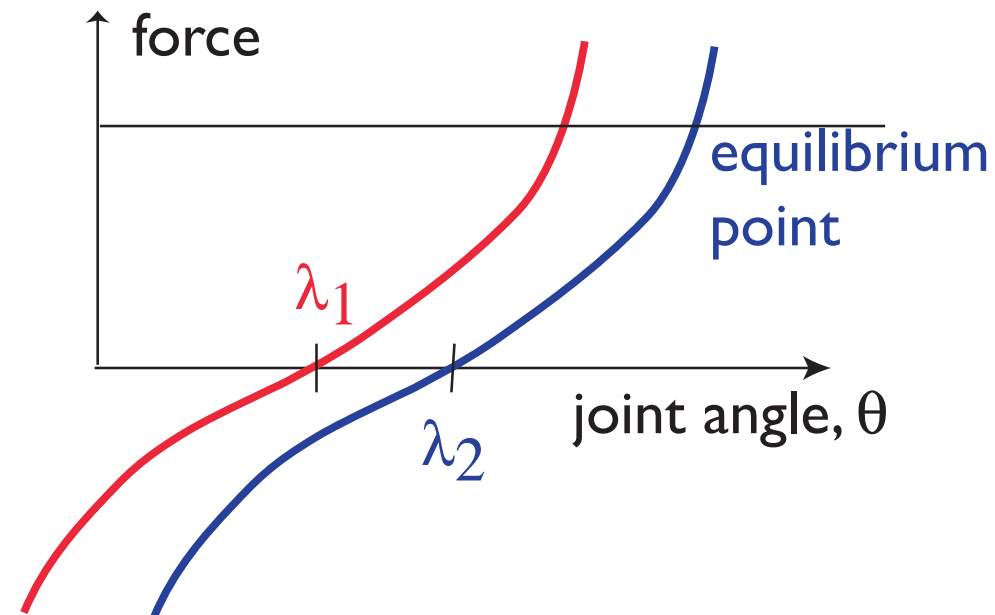
# Movement entails change of posture

- most models account for movement in terms of generation of joint torques....
- => the shift of the EP is the single most overlooked fact in control models of movement generation



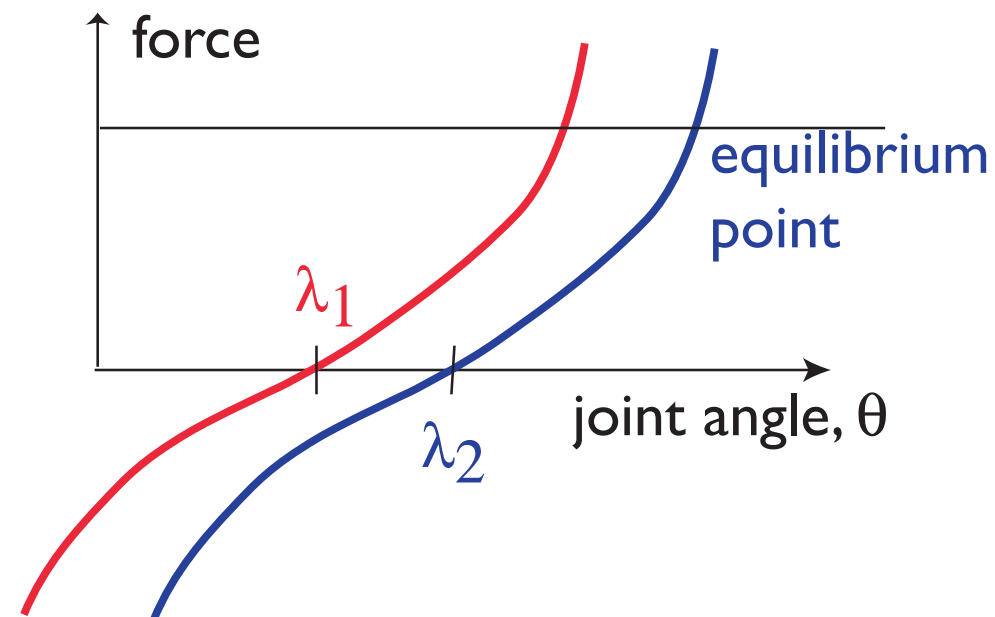
# Does the “motor command” specify force/torque?

- no! Because the same descendent neural command generates different levels of force depending on the initial length of the muscle

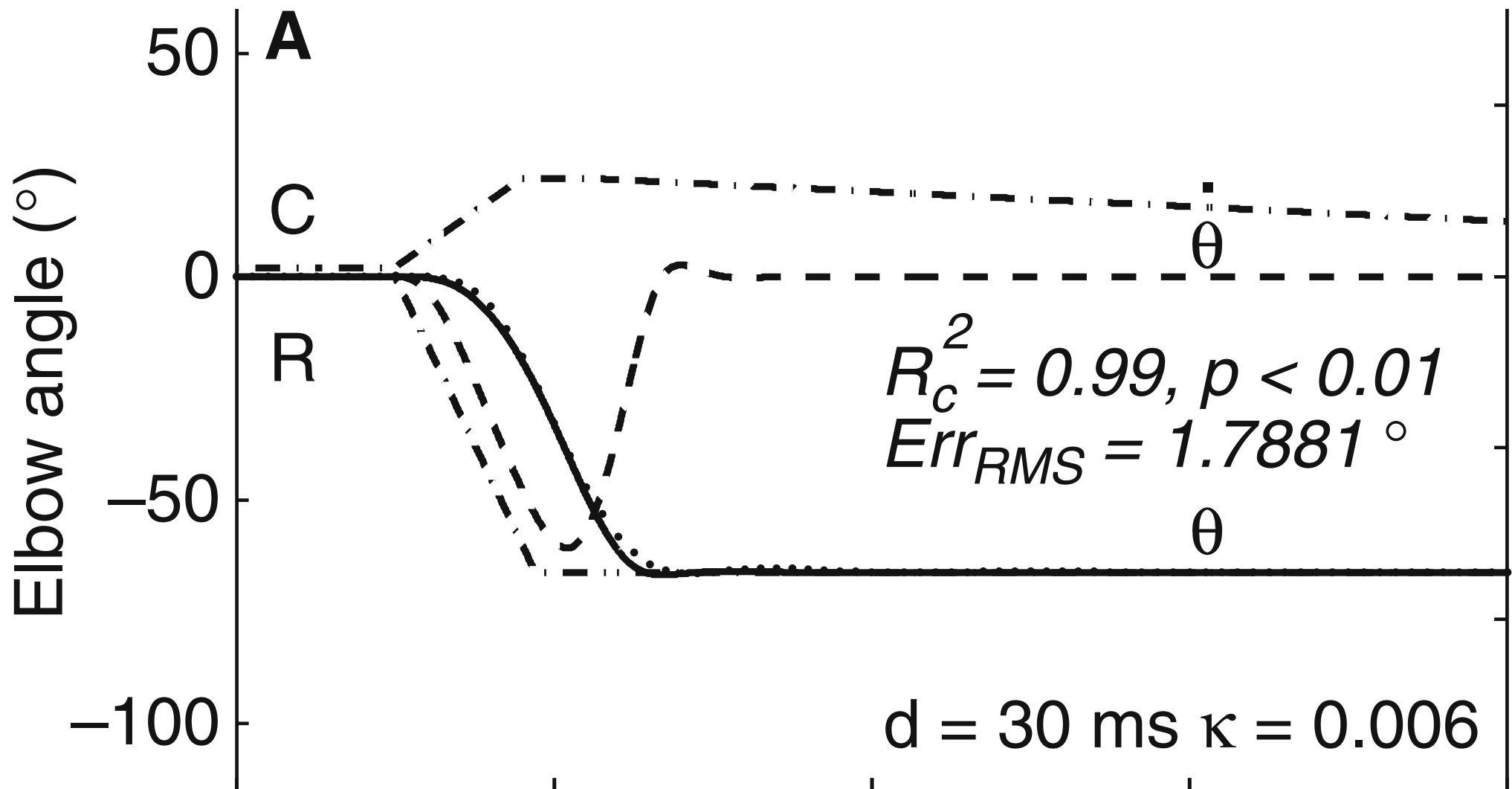


# Virtual trajectory

- shifting the equilibrium point is necessary, but is it also sufficient?
- first answer: yes... simple ramp-like trajectories of the “r” command (“virtual trajectories”) shift the equilibrium point smoothly in time...



# Pilon, Feldman, 2006



# Shifting the equilibrium point is necessary, but is it also sufficient?

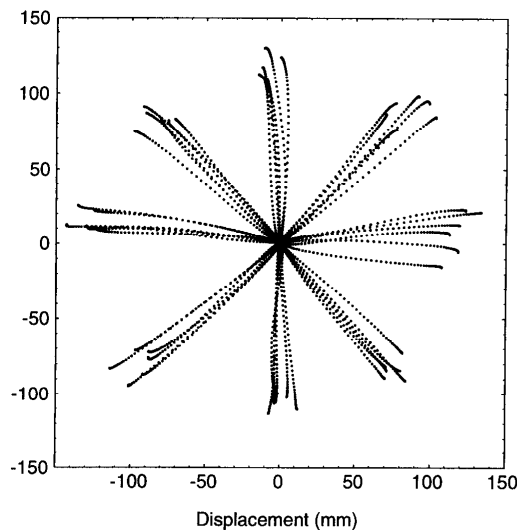
- such simple ramp-like trajectories of the “r” command (“virtual trajectories”) may be sufficient when movements
  - are sufficiently slow
  - interaction torques/mechanical conditions unchallenging
- but is this generally true?



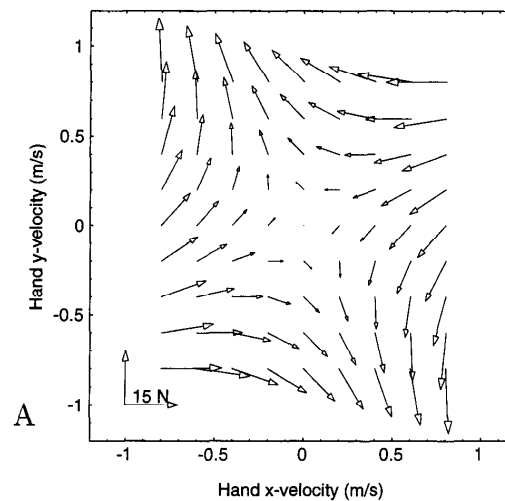
# Limit case: velocity dependent force field

- after adapting to a velocity dependent force field the hand reproduces the “natural” path, but must generate compensatory forces on the way

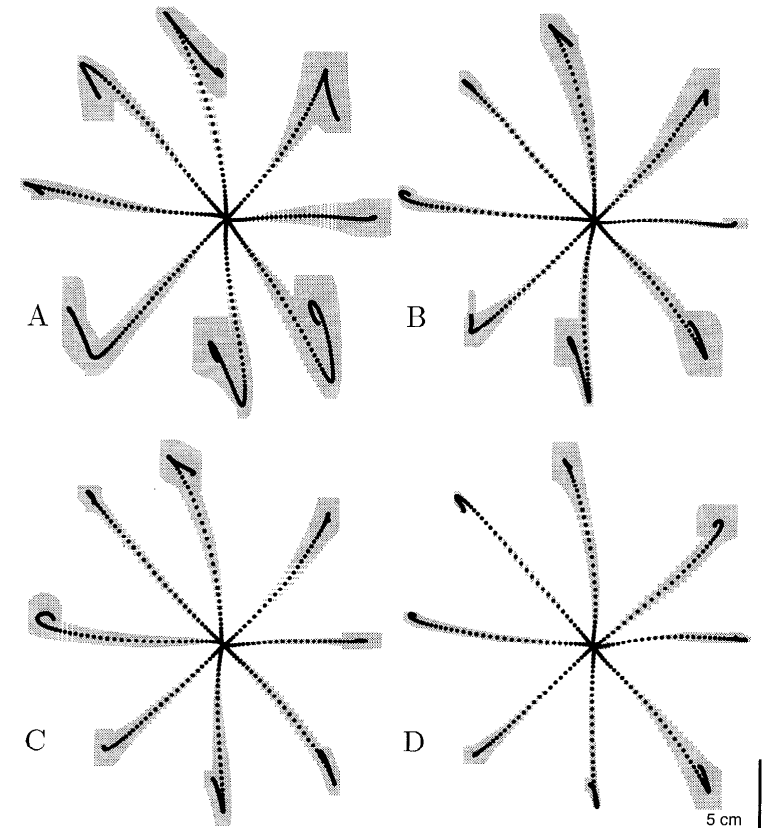
[Shadmehr, Mussa-Ivaldi, 1994]



center-out movements  
before force-field  
adaptation



velocity dependent  
force-field = zero at rest



center-out movements  
at four stages during  
force-field adaptation

# Shifting the equilibrium point is necessary, but is it also sufficient?

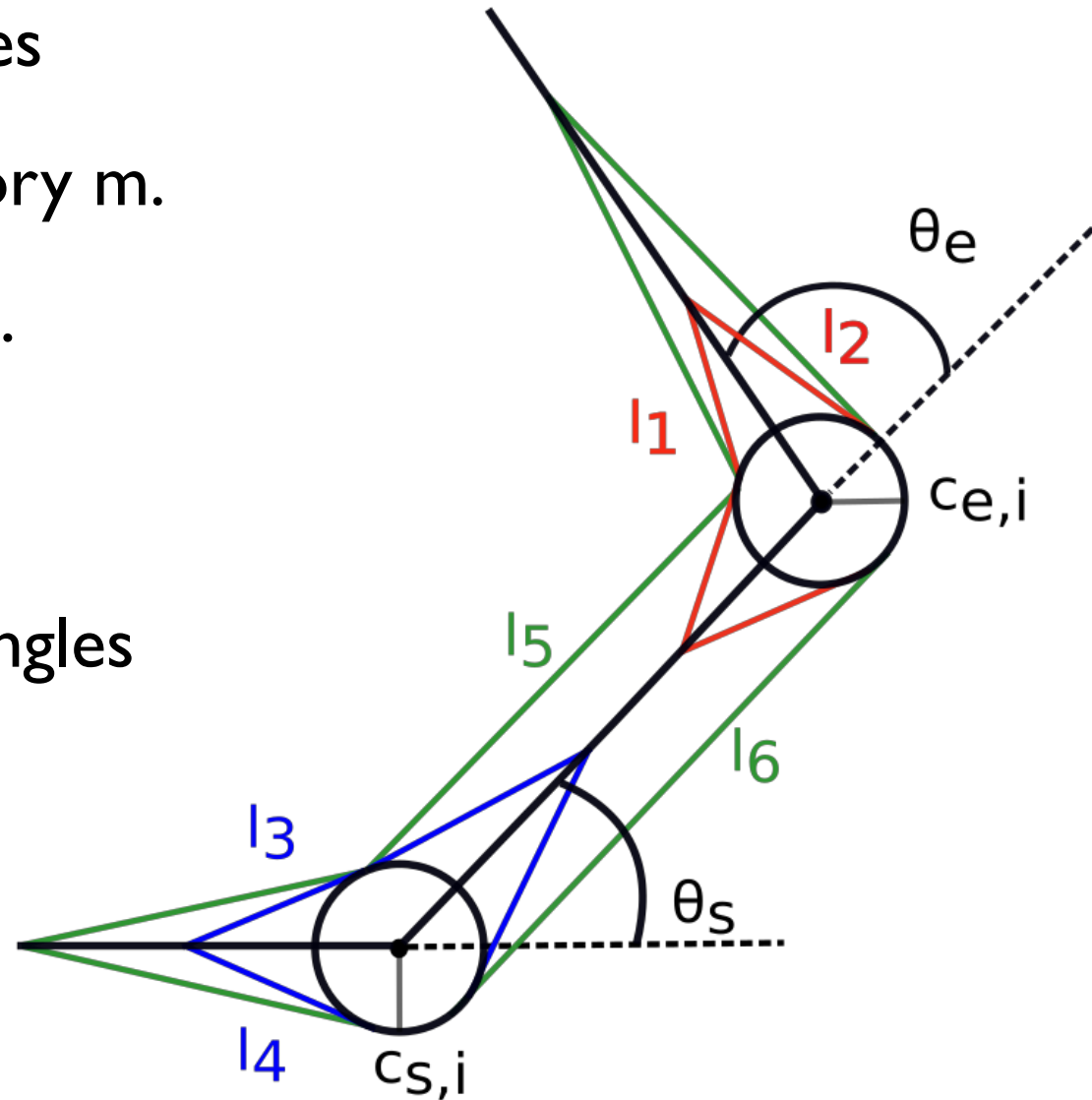
- => r-command must still shift from initial to final posture, but must also generate the forces to compensate for the force field during the movement
- that probably takes the form of non-monotonic, “complex” time courses...
- are such temporally complex (e.g., non-monotonic) r-commands necessary during unperturbed movement

# The minimal reference command

- two joint limb with 6 muscles
- = 2 pairs of mono-articulatory m.
- + 1 pair of bi-articulatory m.

- muscle length link to joint angles

$$l_i = c_i + c'_{i,s}\theta_s + c'_{i,e}\theta_e$$



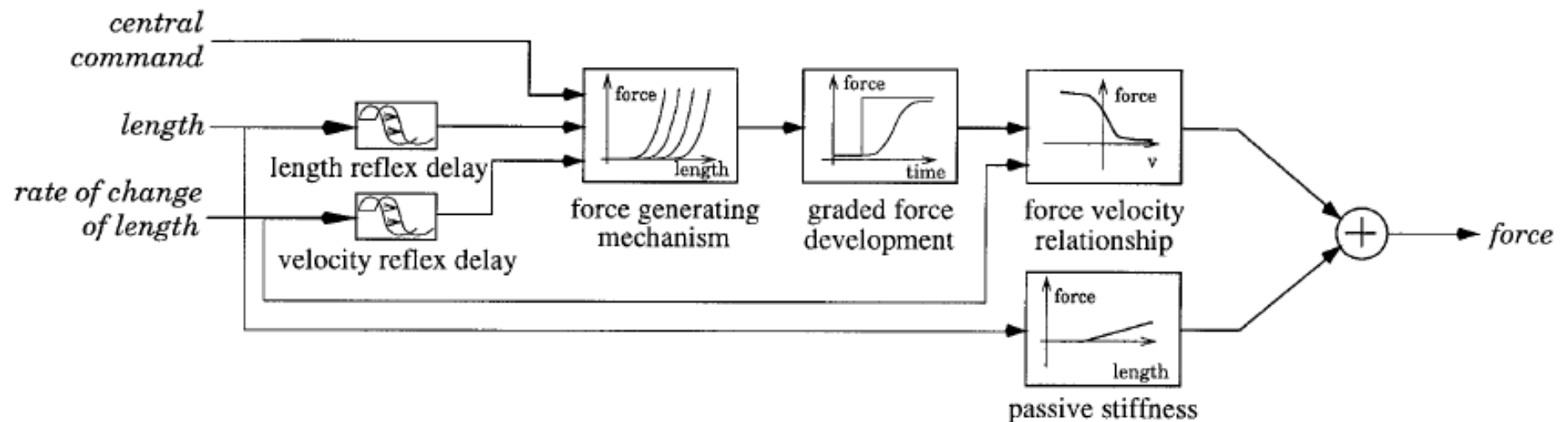
■ Neuro-muscular model based on Gribble, Ostry et al., 98... consistent with EP hypothesis

$$A_i = [l_i - \lambda_i + \mu \cdot \dot{l}_i]^+ \quad [x]^+ = \begin{cases} x, & \text{if } x > 0 \\ 0, & \text{if } x \leq 0 \end{cases}$$

$$\tilde{M}_i = \rho_i \cdot (e^{sA_i} - 1).$$

$$\tau^2 \ddot{M} + 2\tau \dot{M} + M = \tilde{M}$$

$$F_i = M_i[(f_1 + f_2 \cdot \arctan(f_3 + f_4 \cdot \dot{l}_i))] + k(l_i - c_i).$$



$$T = -H \cdot F$$

with  $H$  defined as

$$H = \frac{\partial l}{\partial \theta} = \begin{pmatrix} \frac{\partial l}{\partial \theta_1} & \frac{\partial l}{\partial \theta_2} \end{pmatrix}$$

$$\ddot{\theta} = I^{-1}(T - T_{ext} - C\dot{\theta})$$

$$x = \cos(\theta_1) \cdot l_1 + \cos(\theta_1 + \theta_2) \cdot l_2$$

$$y = \sin(\theta_1) \cdot l_1 + \sin(\theta_1 + \theta_2) \cdot l_2$$

■ Biomechanical dynamics...  
standard...

back to muscle:

$$l_i = c_i + c'_{i,s}\theta_s + c'_{i,e}\theta_e$$

- determine the “minimal” motor command that changes all lamda’s the least possible:

$$\min_{\vec{\lambda}} \Psi(\vec{\lambda}) = \int_0^{t_f} \dot{\vec{\lambda}}(t)^2 dt.$$

- given that the EP shifts: with boundary conditions

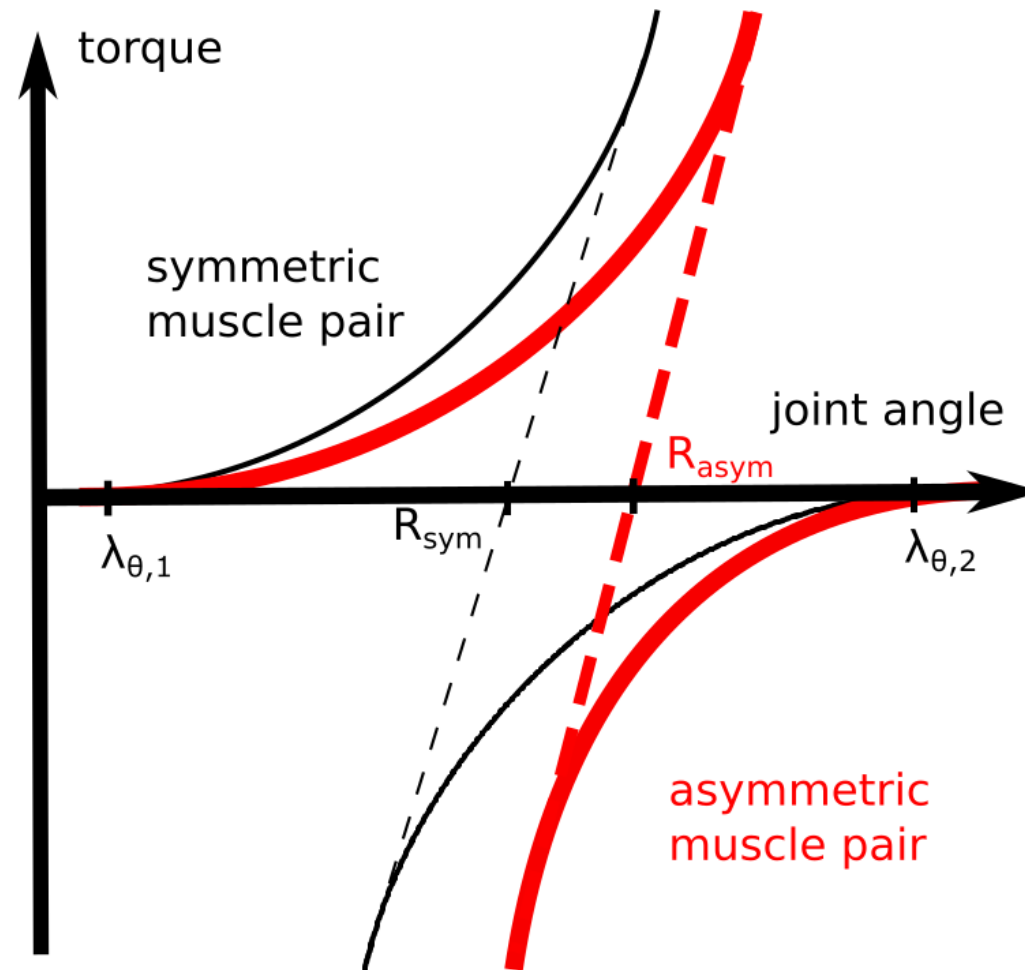
$$\vec{\theta}(t_0) - \vec{\theta}_{\text{start}} = 0, \quad \dot{\vec{\theta}}(t_0) = 0, \quad \ddot{\vec{\theta}}(t_0) = 0,$$

$$\vec{\theta}(t_f) - \vec{\theta}_{\text{final}} = 0. \quad \dot{\vec{\theta}}(t_f) = 0. \quad \ddot{\vec{\theta}}(t_f) = 0.$$

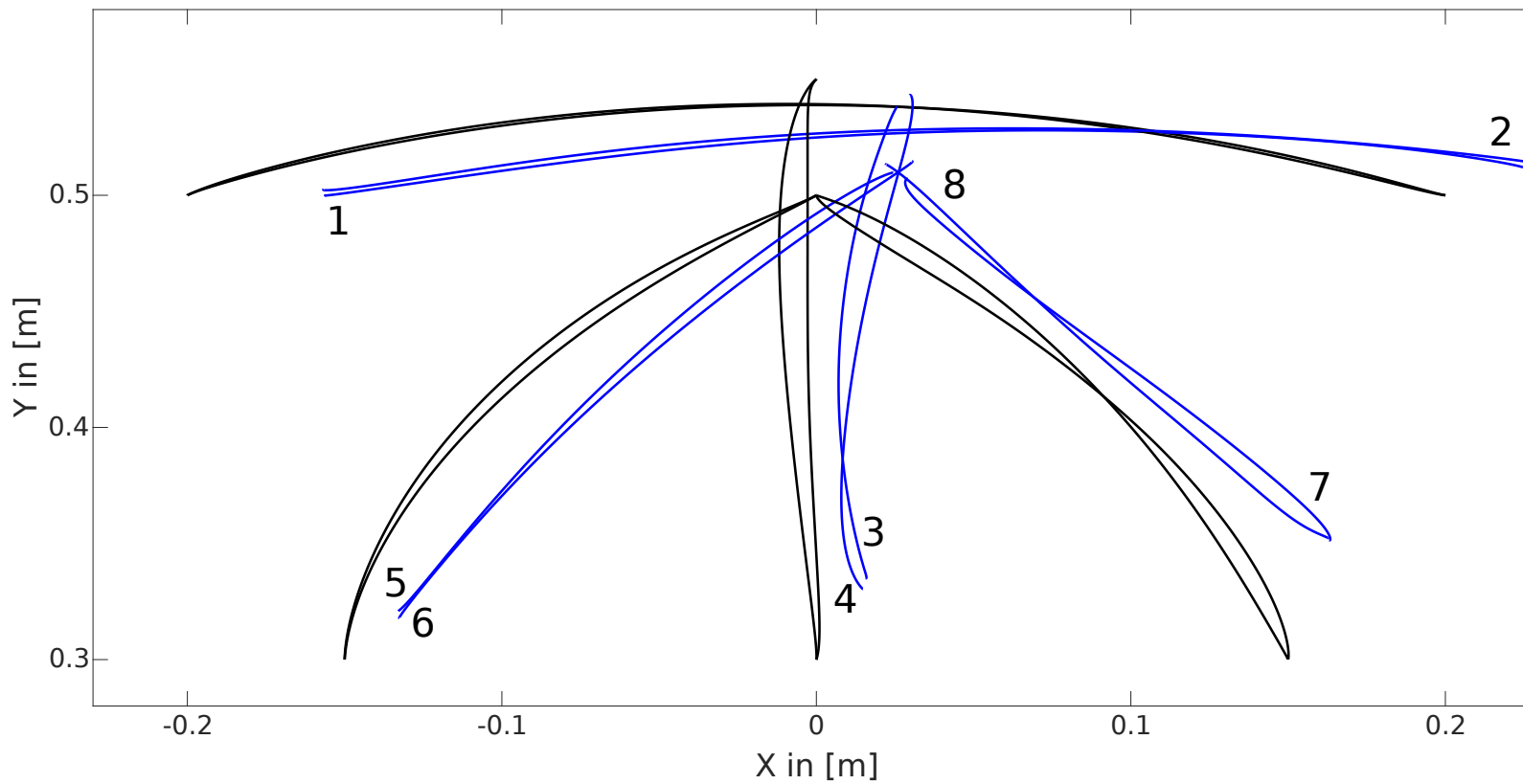
$$\vec{\theta}(t) < \vec{\theta}_{\text{max}}, \quad \lambda_{\text{min}} \leq \vec{\lambda}(t) \leq \lambda_{\text{max}} \quad t \in [t_0, t_f].$$

$$\dot{\vec{\theta}}(t) < \dot{\vec{\theta}}_{\text{max}}.$$

# Why “lambda” rather than R?



# Paths exp-model



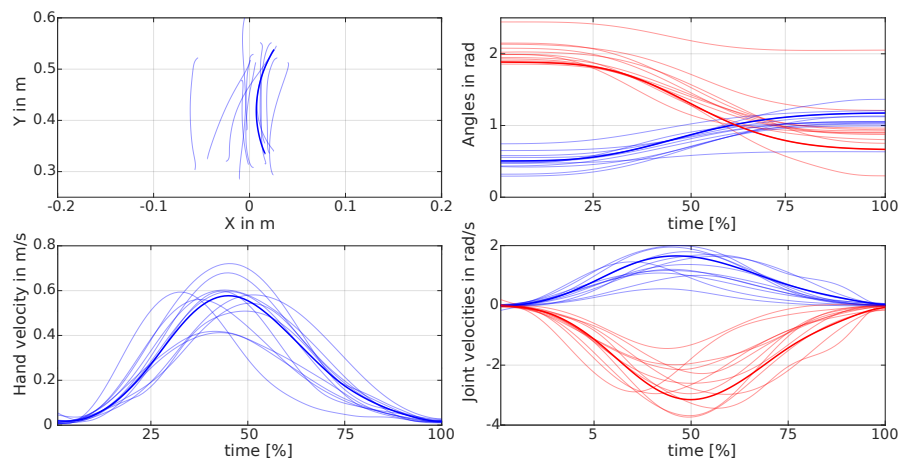
blue: experiment  
black: model



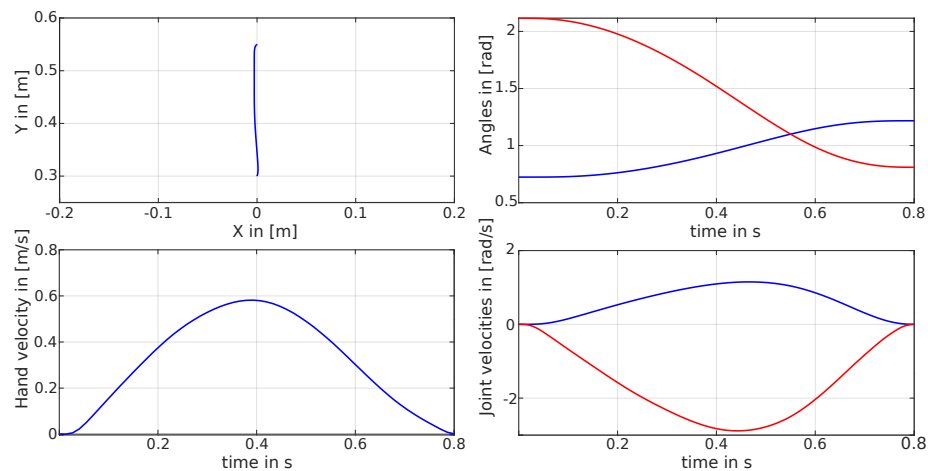
# Trajectories exp-data

slow

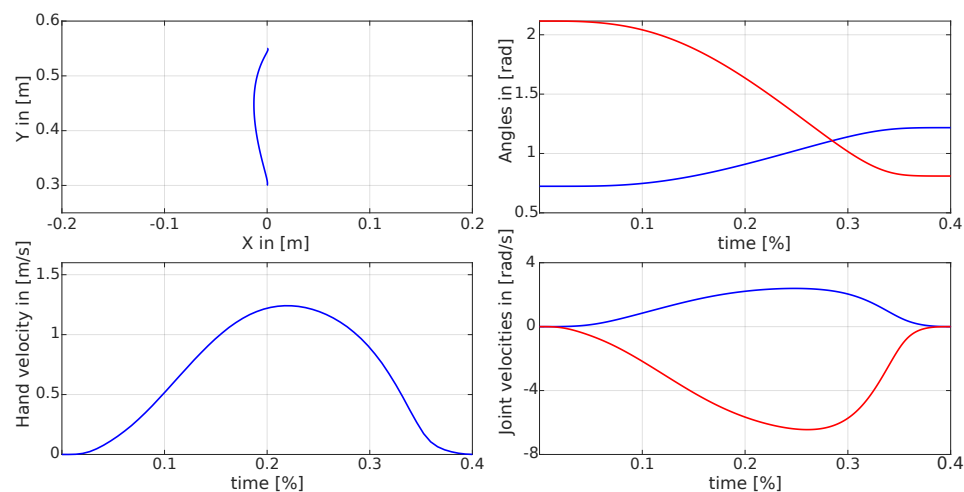
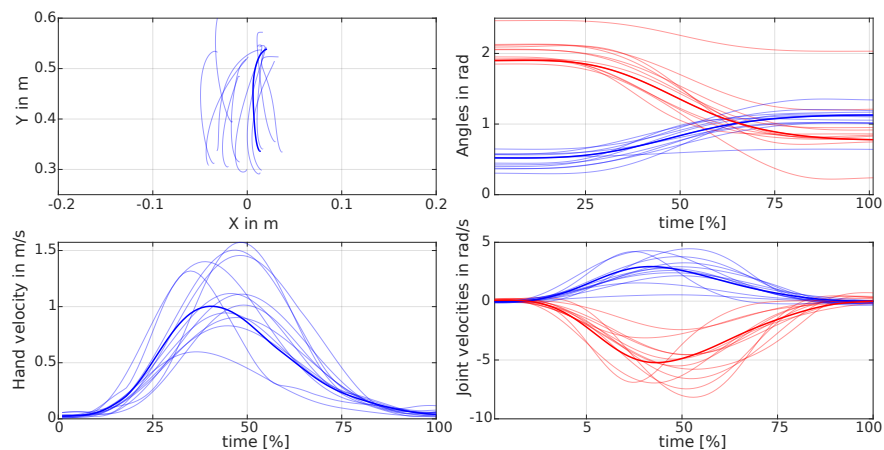
experiment



model



fast



# Minimal lambda trajectories

flexors

Shoulder lambda

Elbow lambda

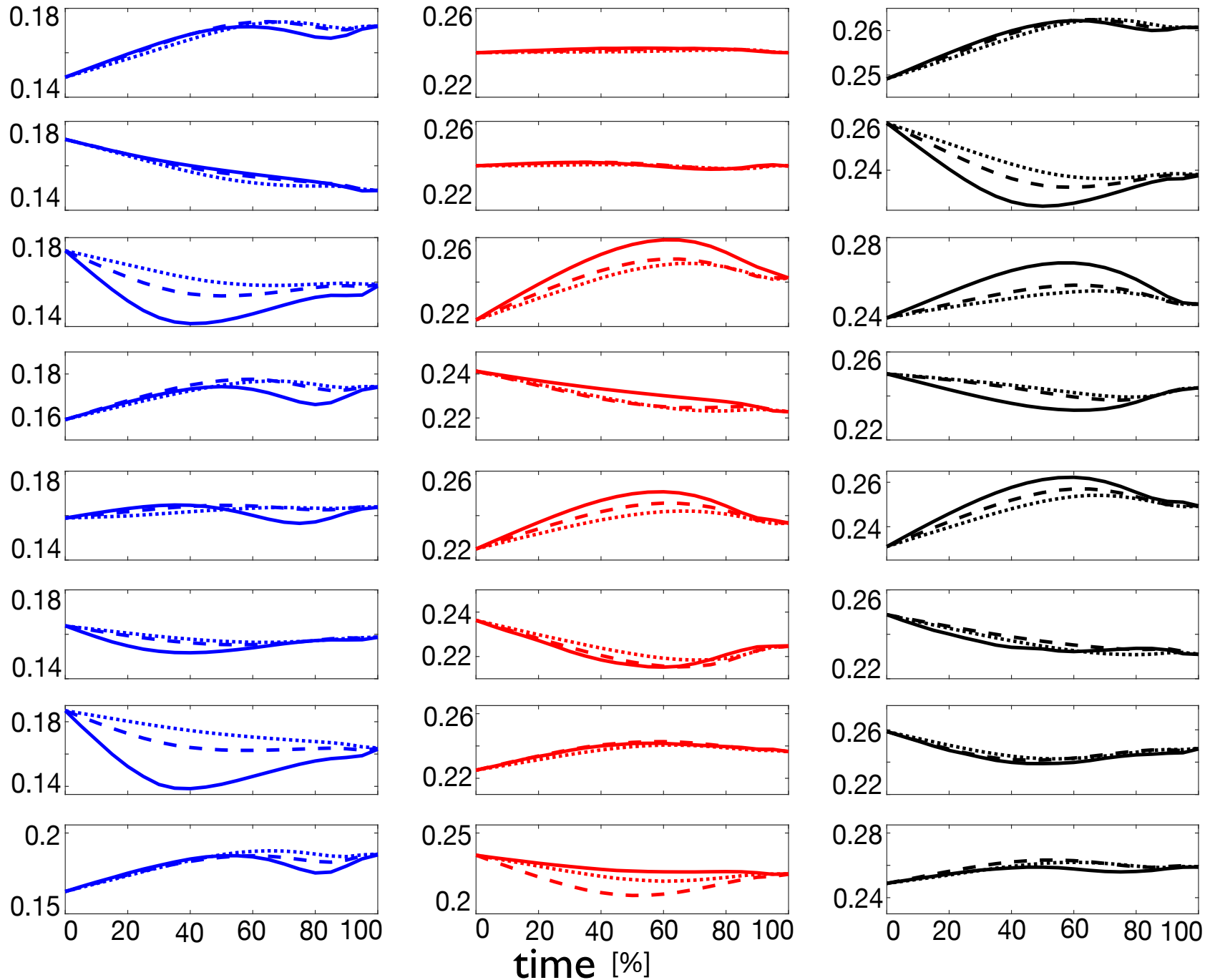
Biarticular lambda

[m]

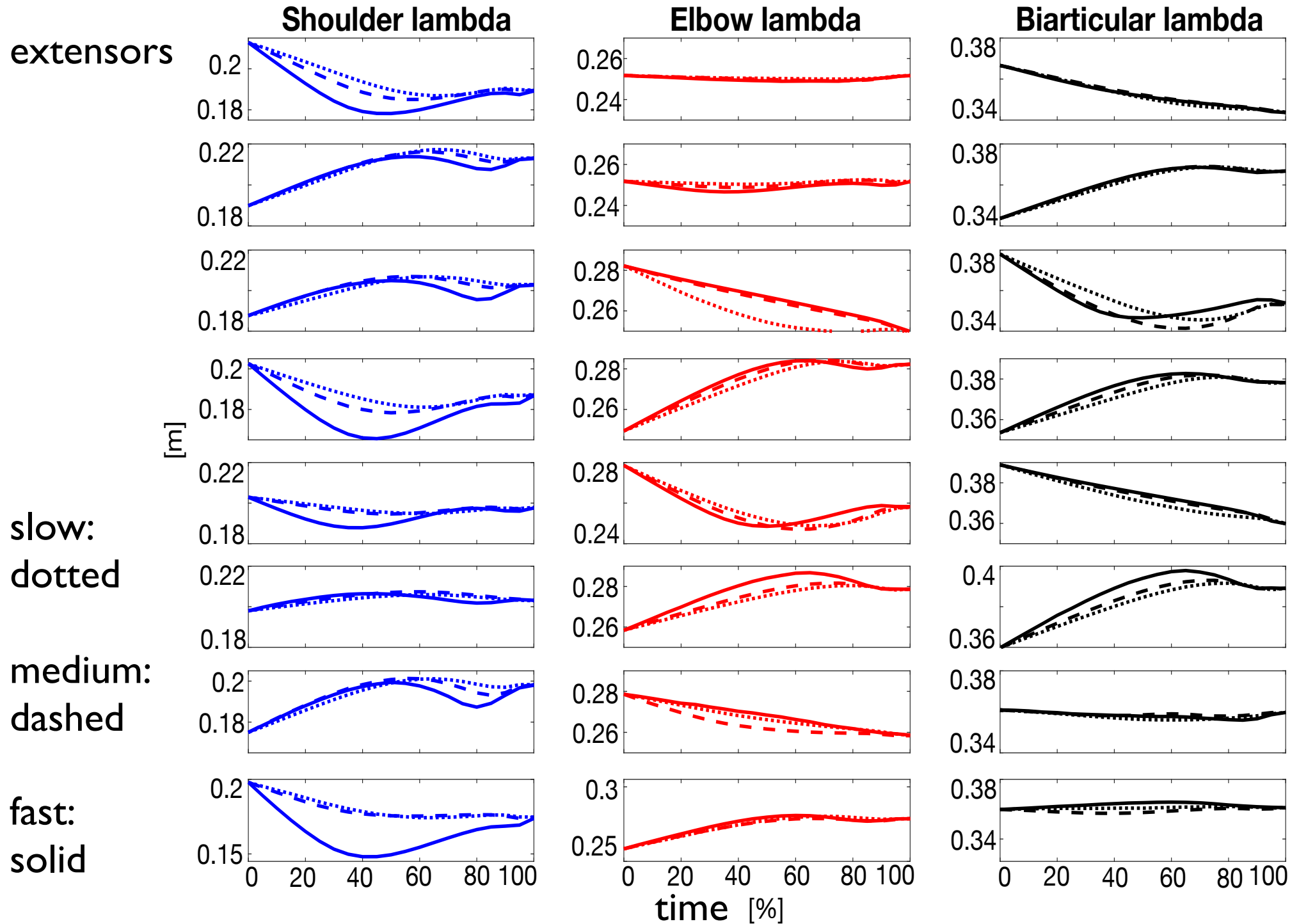
slow:  
dotted

medium:  
dashed

fast:  
solid

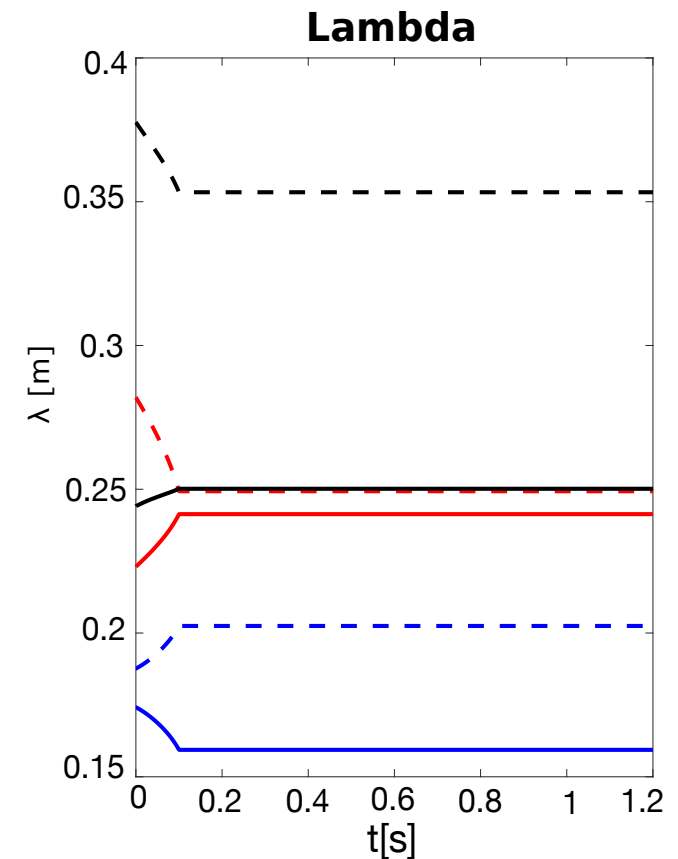
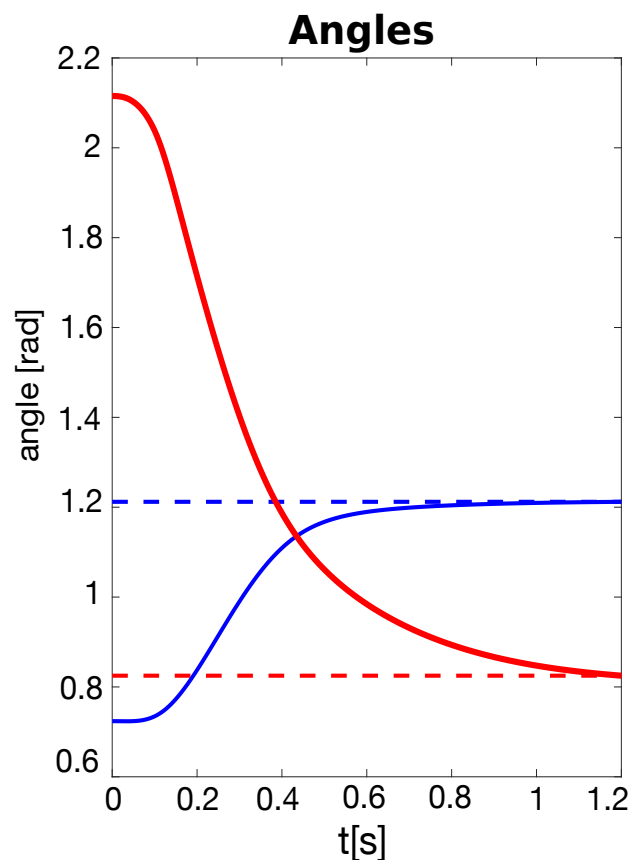
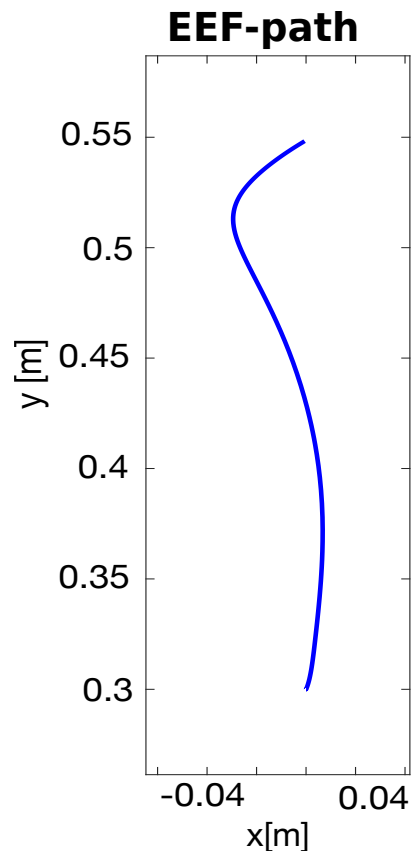


# Minimal lambda trajectories



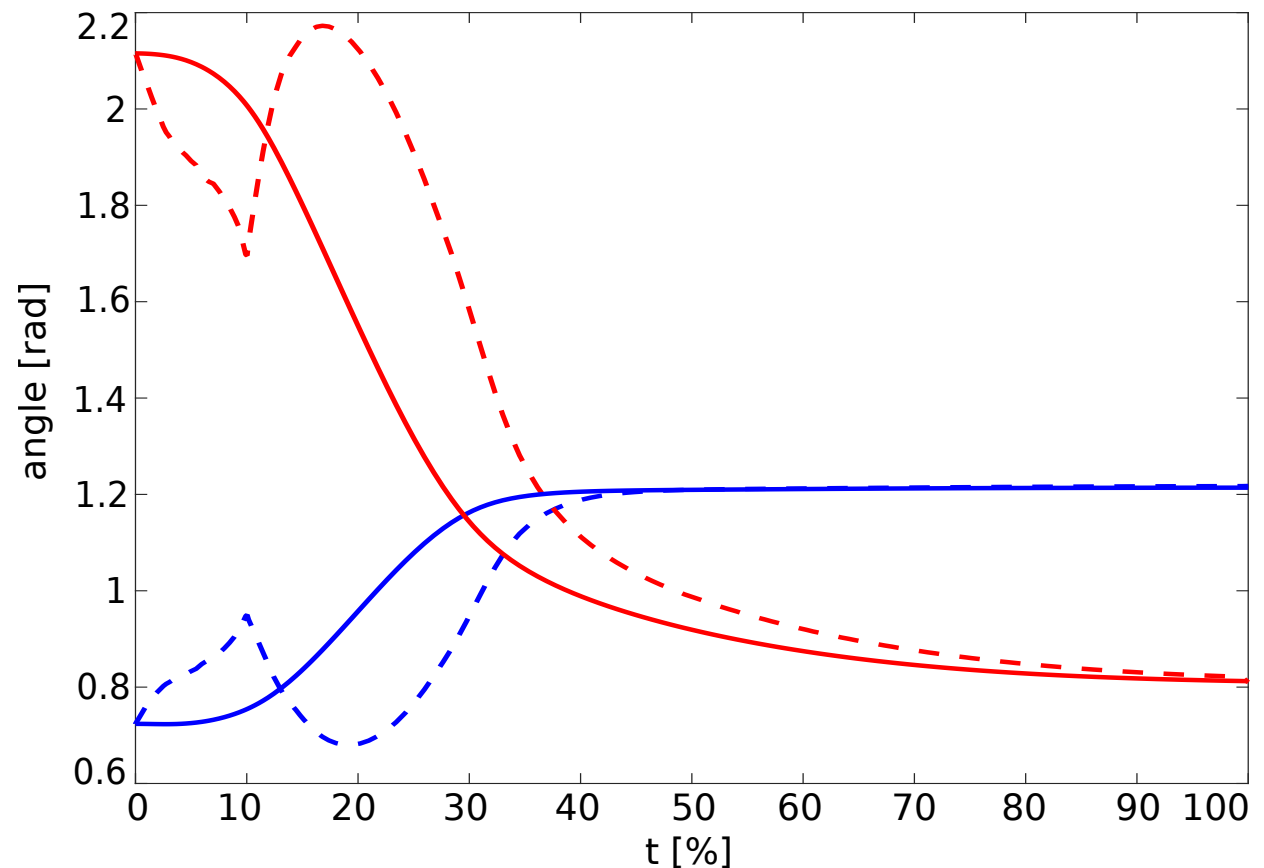
# Do the time courses of lambda matter?

- making a slow ramp (in hand space) fast



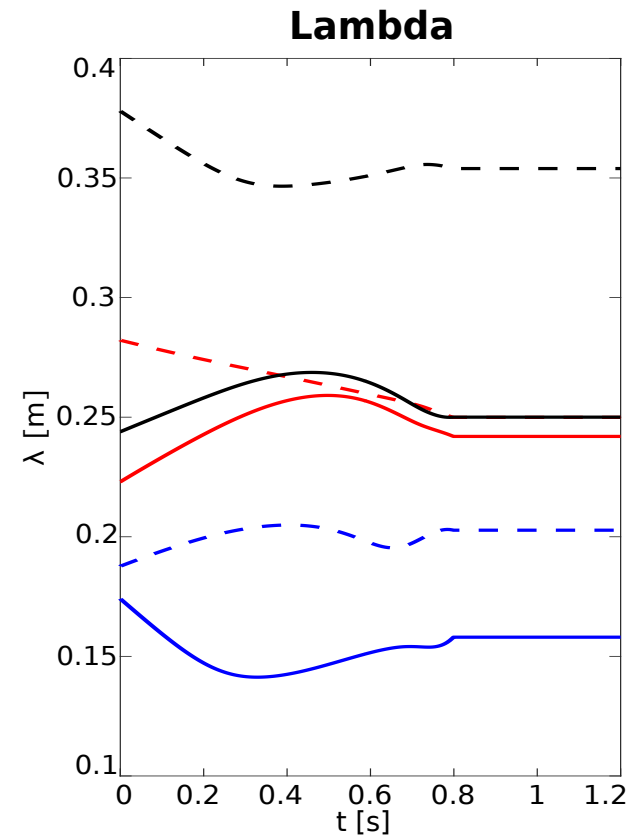
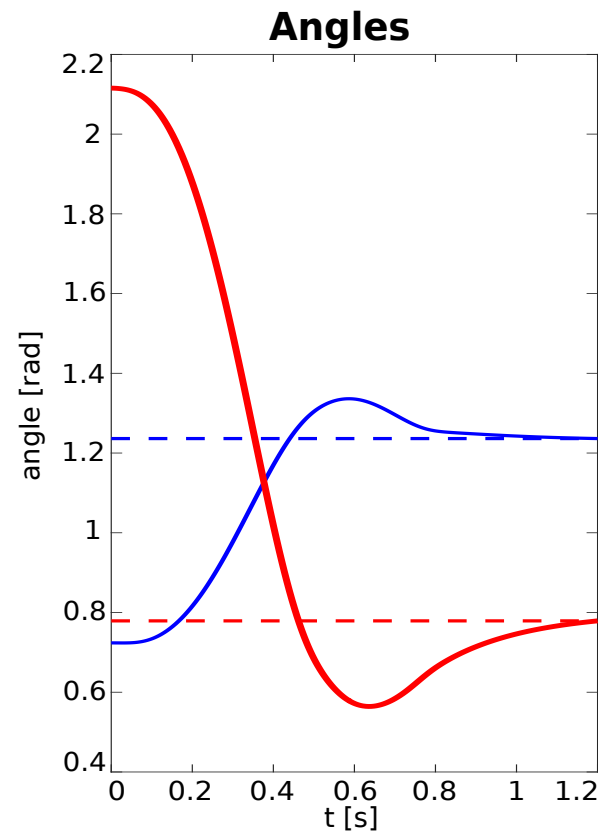
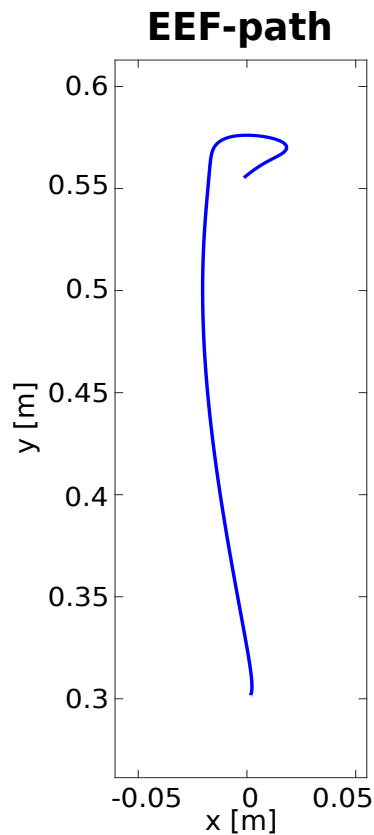
# Do the time courses of lambda matter?

- attractor (dashed) and real (solid) trajectory from fast ramp



# Do the time courses of lambda matter?

- slowing down lambda of a fast movement



# Optimal control

- => CNS needs to solve the “optimal control” problem = generating the right time course of motor commands so that the effector arrives at the target in the desired time with zero velocity (and has some desired smooth temporal shape).