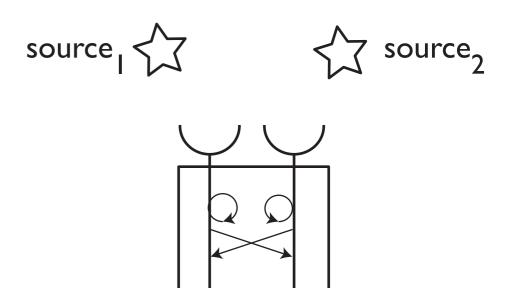
Neural Dynamics

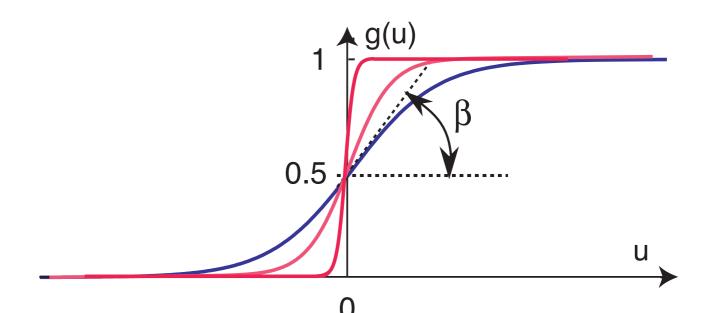
Gregor Schöner gregor.schoener@ini.rub.de

- how to represent the inner state of the Central Nervous System?
- => activation concept



- neural state variables
 - membrane potential of neurons?
 - spiking rate?
 - ... population activation...

- activation as a real number, abstracting from biophysical details
 - low levels of activation: not transmitted to other systems (e.g., to motor systems)
 - high levels of activation: transmitted to other systems
 - as described by sigmoidal threshold function
 - zero activation defined as threshold of that function



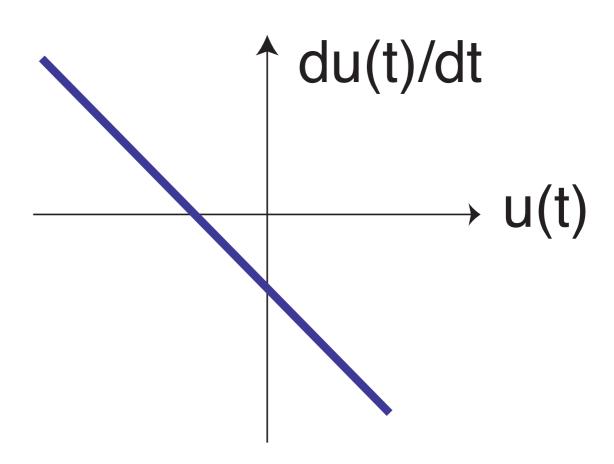
- compare to connectionist notion of activation:
 - same idea, but tied to individual neurons
- compare to abstract activation of production systems (ACT-R, SOAR)
 - quite different... really a function that measures how far a module is from emitting its output...

Activation dynamics

activation variables u(t) as time continuous functions...

$$\tau \dot{u}(t) = f(u)$$

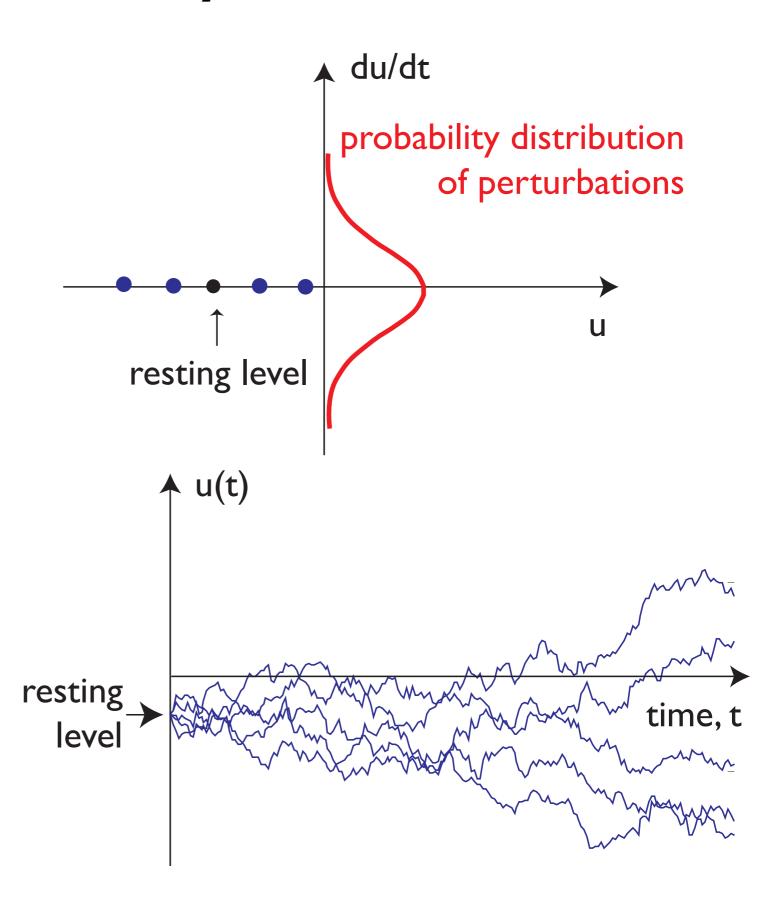
what function f?



Activation dynamics

start with f=0

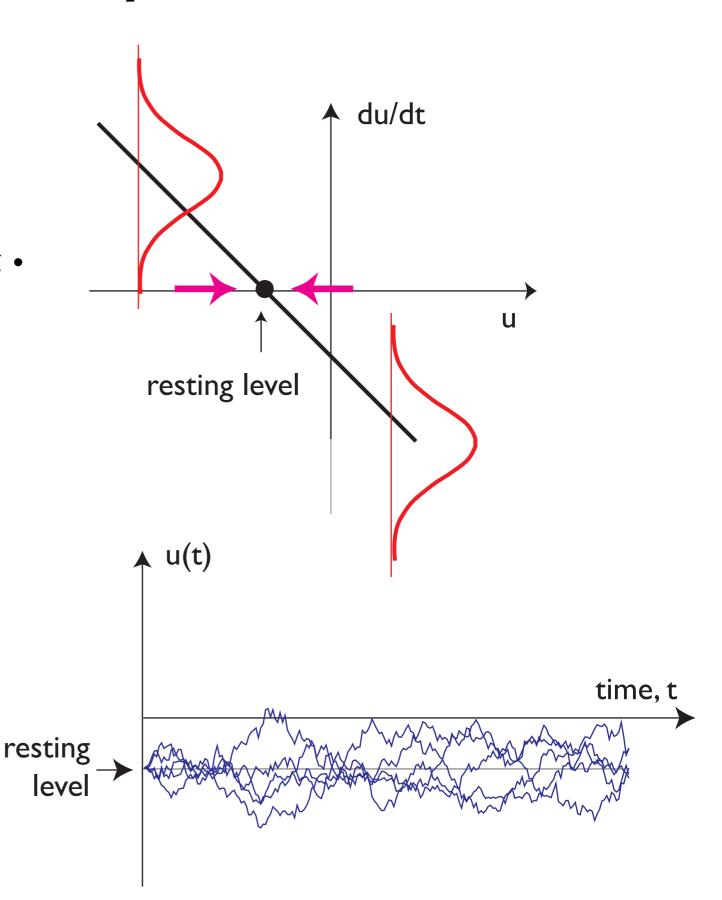
$$\tau \dot{u} = \xi_t$$



Activation dynamics

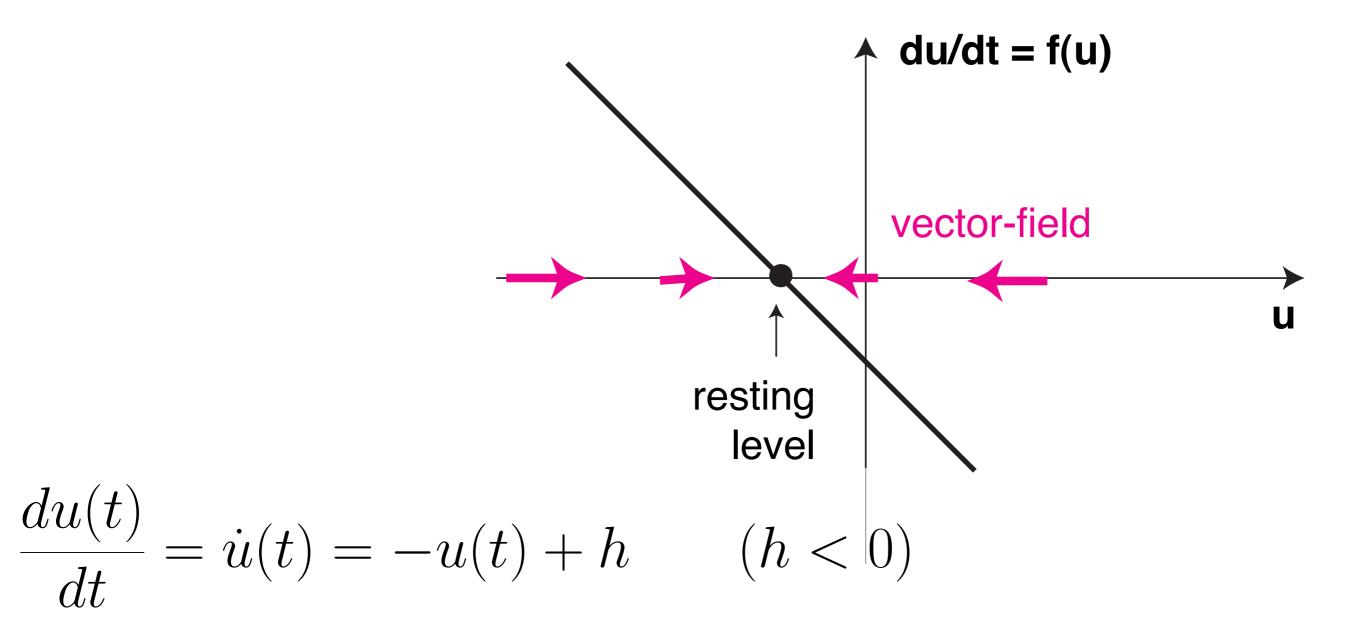
need stabilization

$$\tau \dot{u} = -u + h + \xi_t.$$



Neural dynamics

In a dynamical system, the present predicts the future: given the initial level of activation u(0), the activation at time t: u(t) is uniquely determined

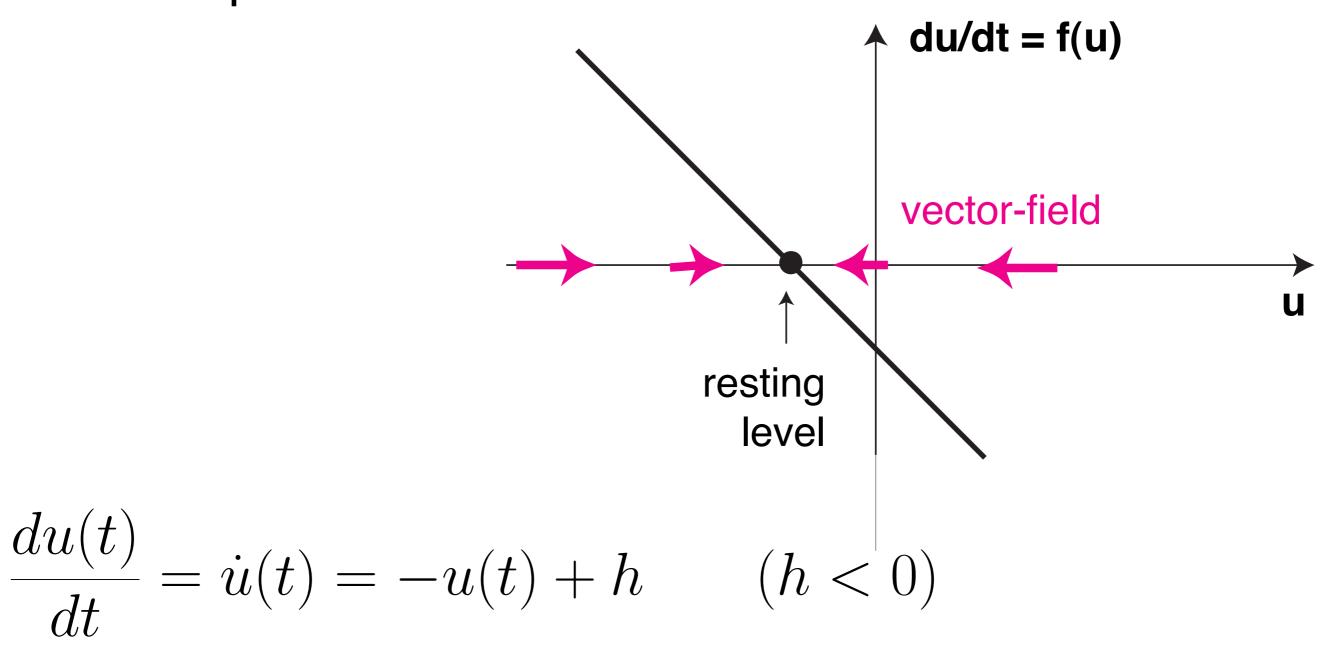


mental simulation

=> dynamical systems tutorial Mathis Richter

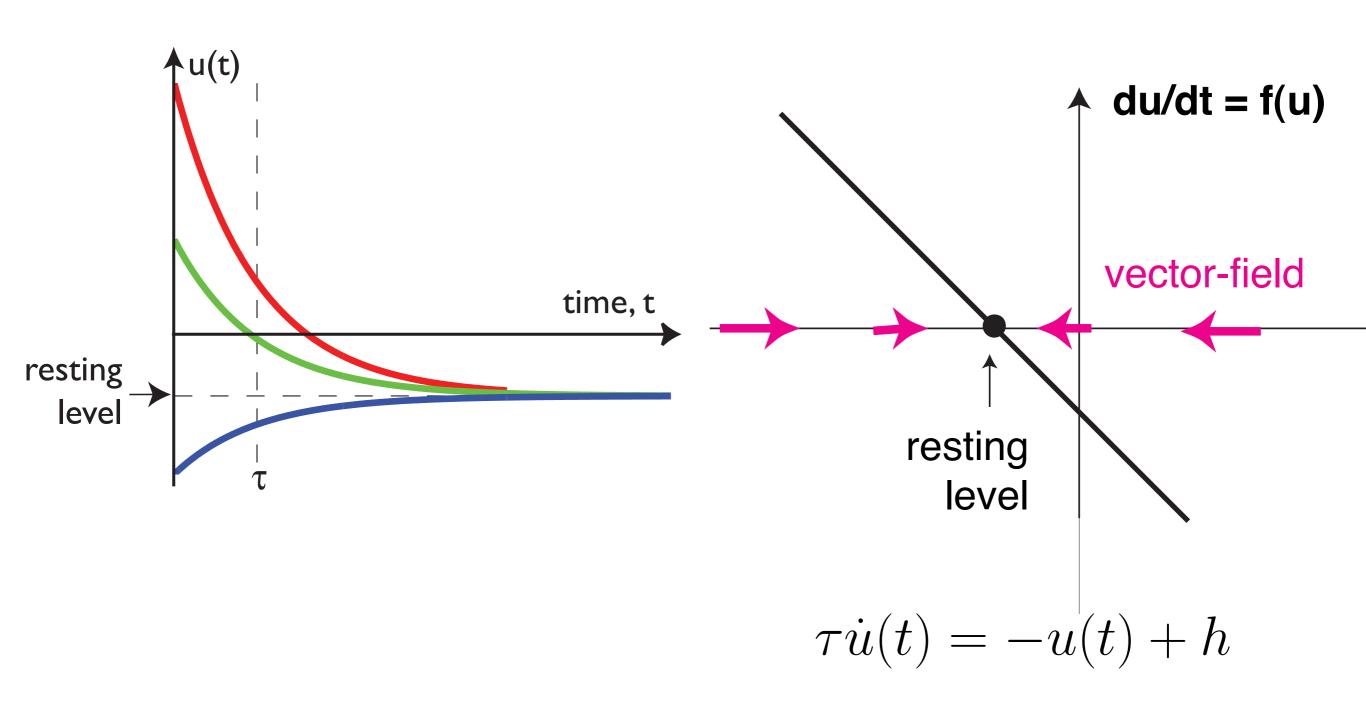
Neural dynamics

- stationary state=fixed point= constant solution
- stable fixed point: nearby solutions converge to the fixed point=attractor



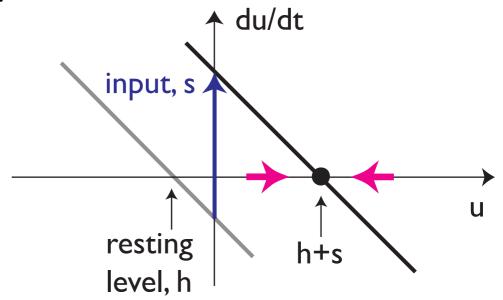
Neural dynamics

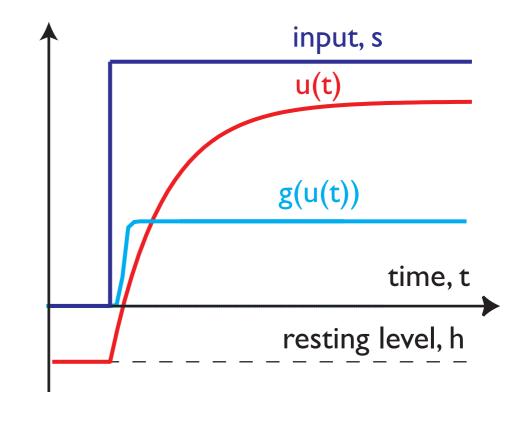
attractor structures ensemble of solutions=flow



Neuronal dynamics

- inputs=contributions to the rate of change
 - positive: excitatory
 - negative: inhibitory
- => shifts the attractor
- activation tracks this shift (stability)





$$\tau \dot{u}(t) = -u(t) + h + inputs(t)$$

=> simulation

tutorial on numerics

=

dynamical system continuous time

$$\dot{u} = f(u)$$
.

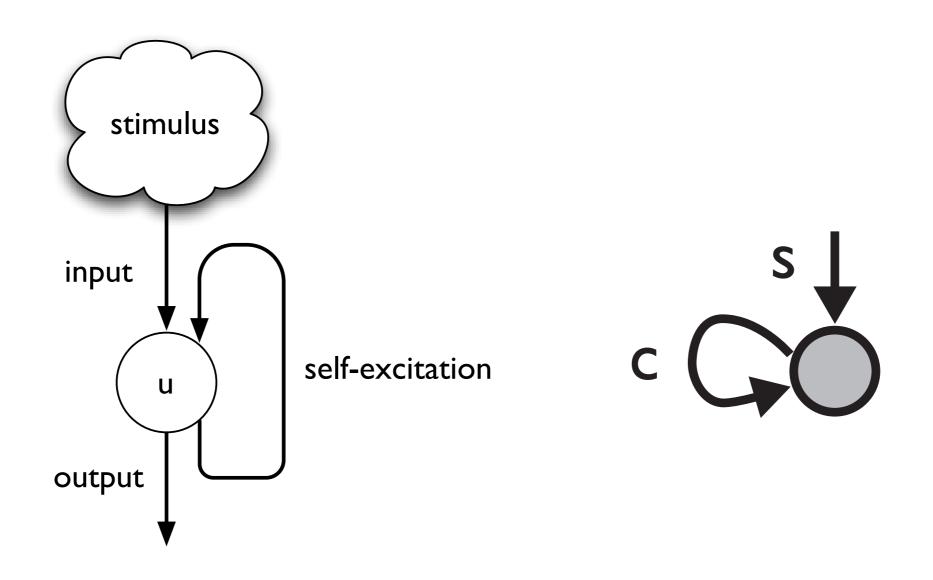
differential
 quotient
 approximates the
 derivative in
 discrete.time

$$\dot{u}(t_i) \approx \frac{u(t_i) - u(t_{i-1})}{\sqrt{t}} \Delta$$

Euler iteration equation in discrete time

$$u(t_i) = u(t_{i-1}) + \Delta t f(u(t_{i-1})).$$

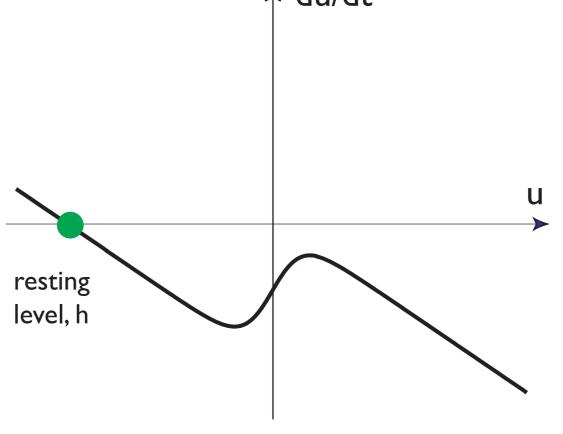
Matlab code



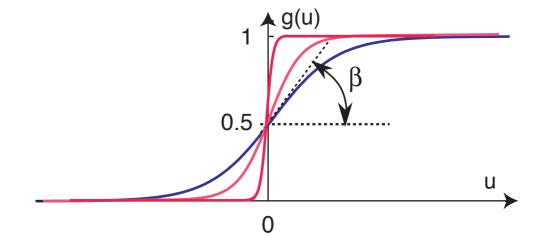
$$\tau \dot{u}(t) = -u(t) + h + S(t) + c\sigma(u(t))$$

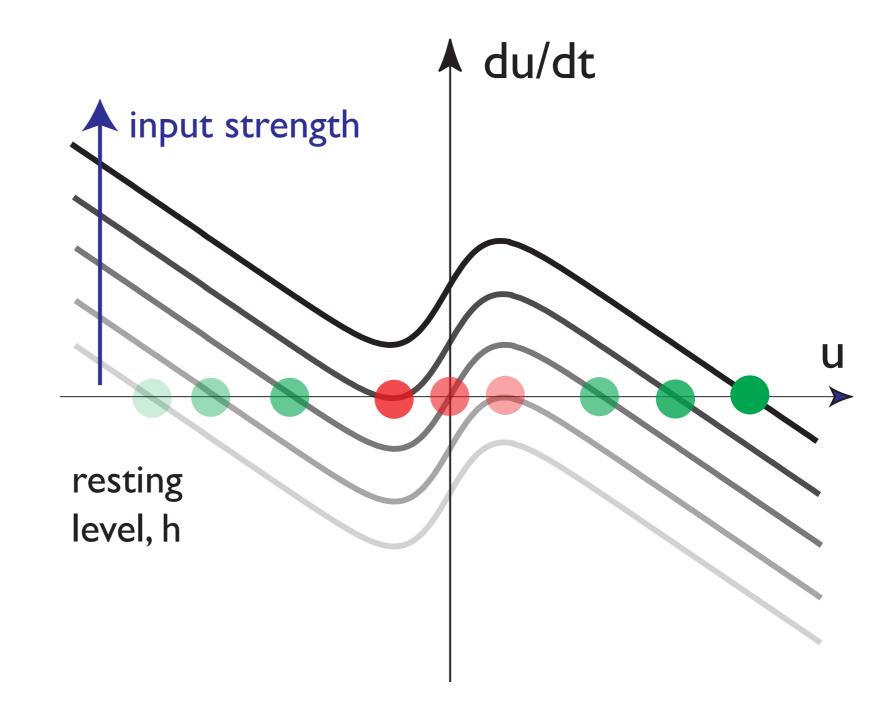
$$\tau \dot{u}(t) = -u(t) + h + S(t) + c\sigma(u(t))$$

$$\uparrow \text{ du/dt}$$



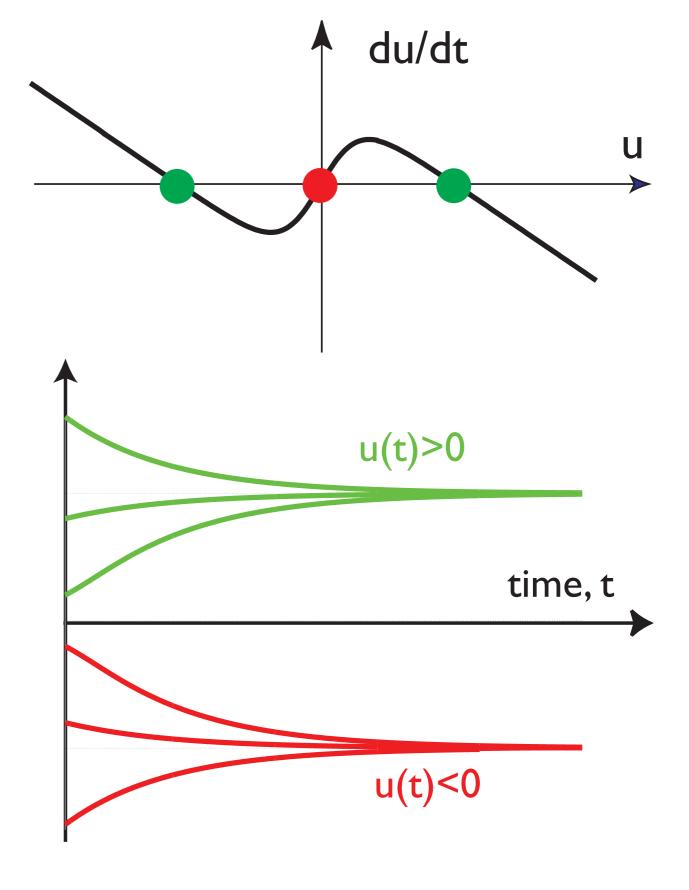
=> nonlinear dynamics!





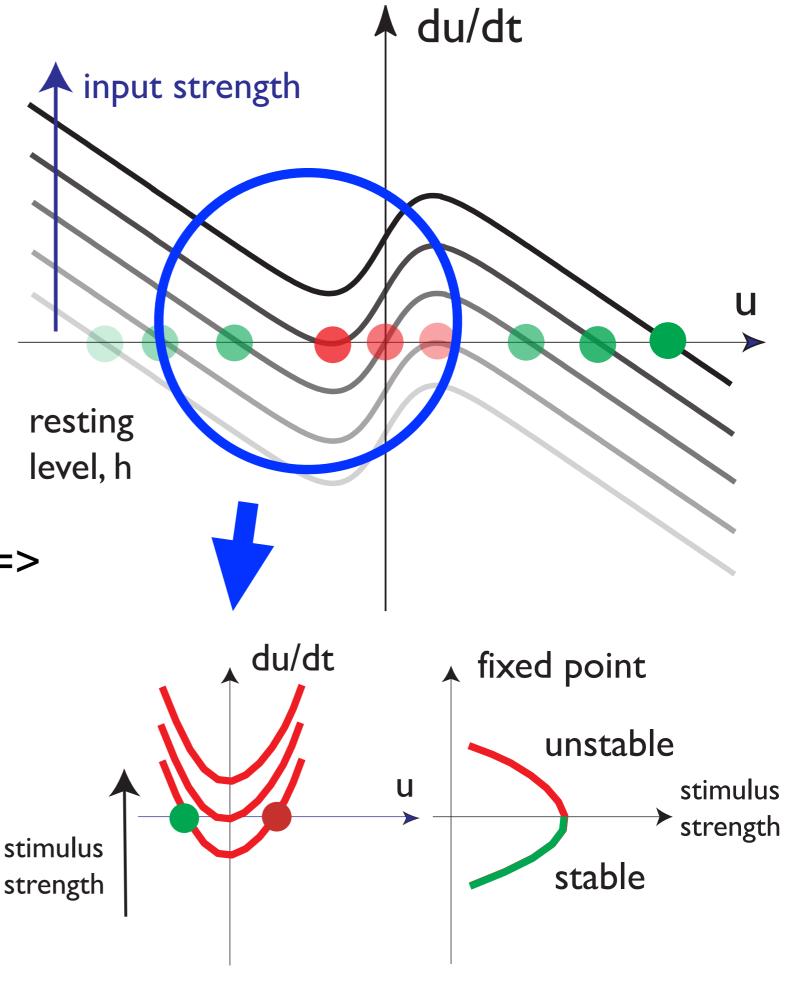
$$\tau \dot{u}(t) = -u(t) + h + S(t) + c\sigma(u(t))$$

- at intermediate stimulus strength: bistable
- "on" vs "off" state

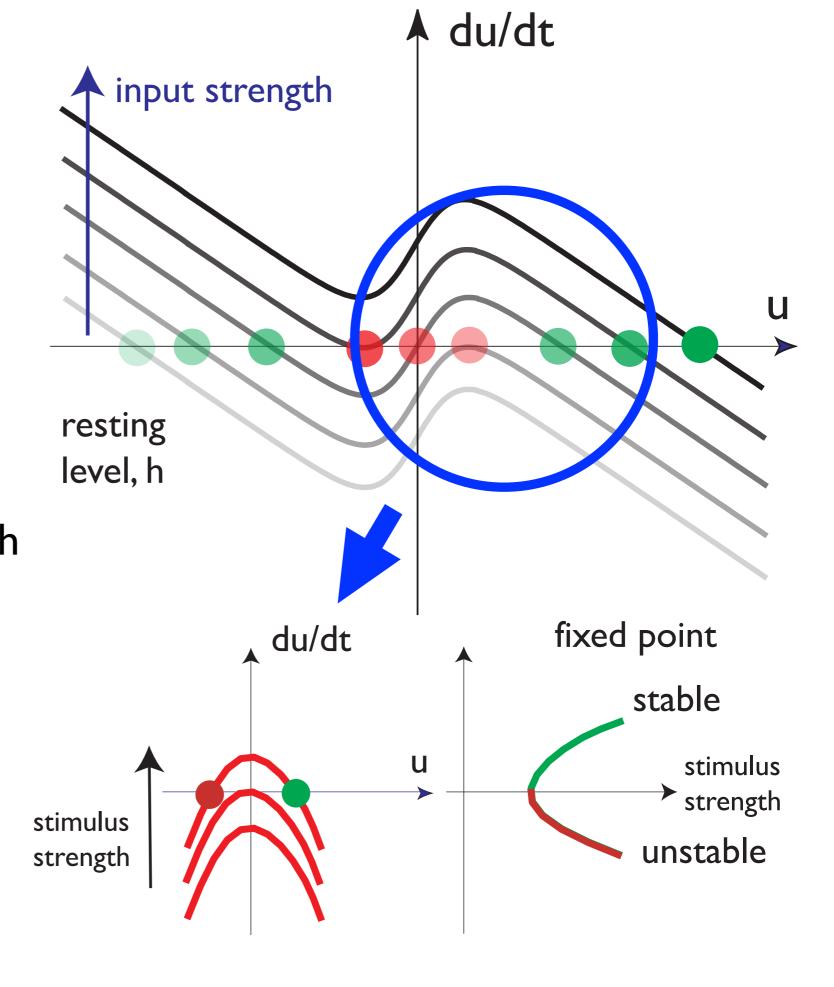


$$\tau \dot{u}(t) = -u(t) + h + S(t) + c\sigma(u(t))$$

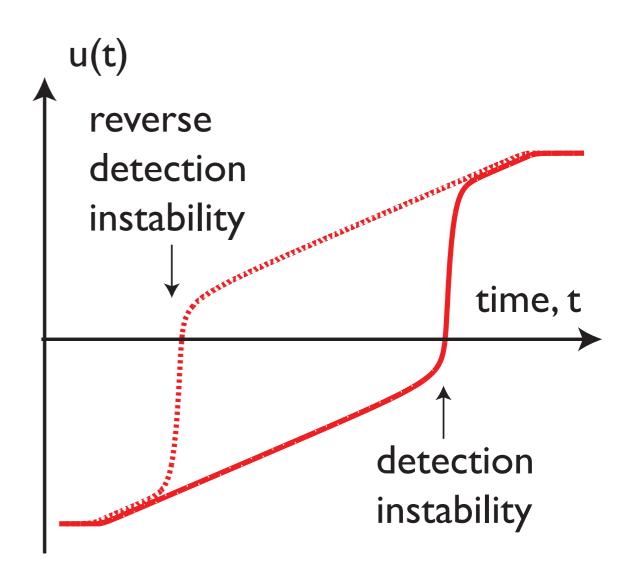
increasing input strength =>
detection instability



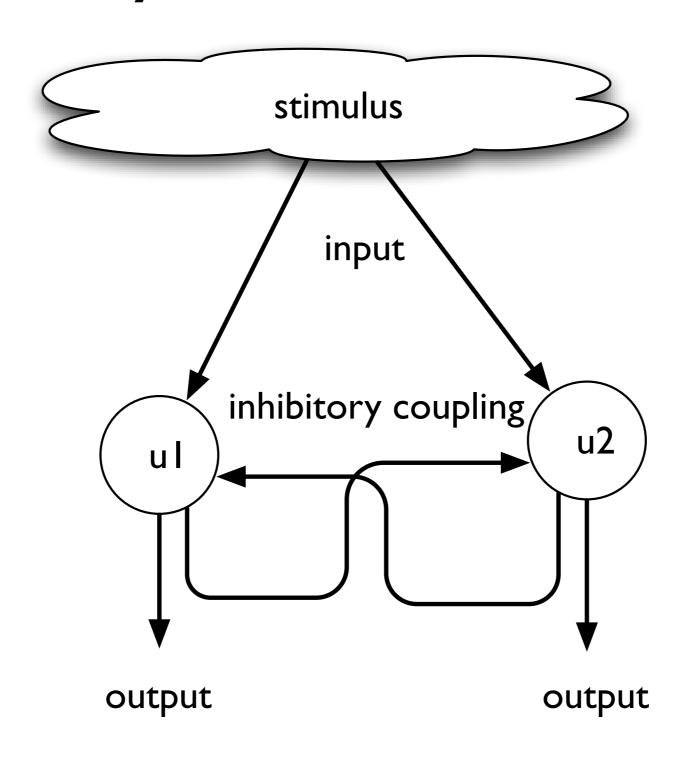
decreasing input strength
=> reverse detection
instability



the detection and the reverse detection instability create discrete events out of input that changes continuously in time







$$\tau \dot{u}_1(t) = -u_1(t) + h - \sigma(u_2(t)) + S_1$$

$$\tau \dot{u}_2(t) = -u_2(t) + h - \sigma(u_1(t)) + S_2$$

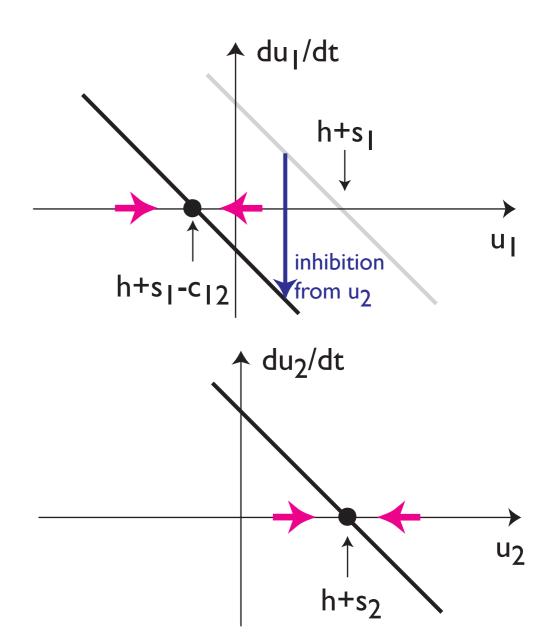
- the rate of change of activation at one site depends on the level of activation at the other site
- mutual inhibition

$$\tau \dot{u}_1(t) = -u_1(t) + h - \sigma(u_2(t)) + S_1$$

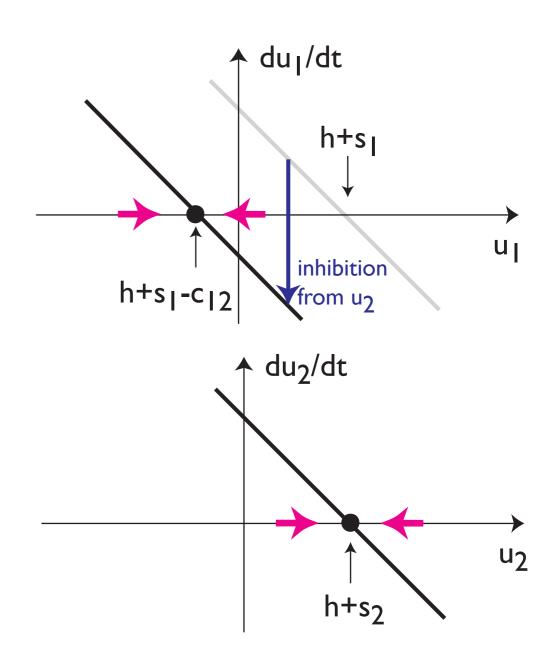
$$\tau \dot{u}_2(t) = -u_2(t) + h - \sigma(u_1(t)) + S_2$$



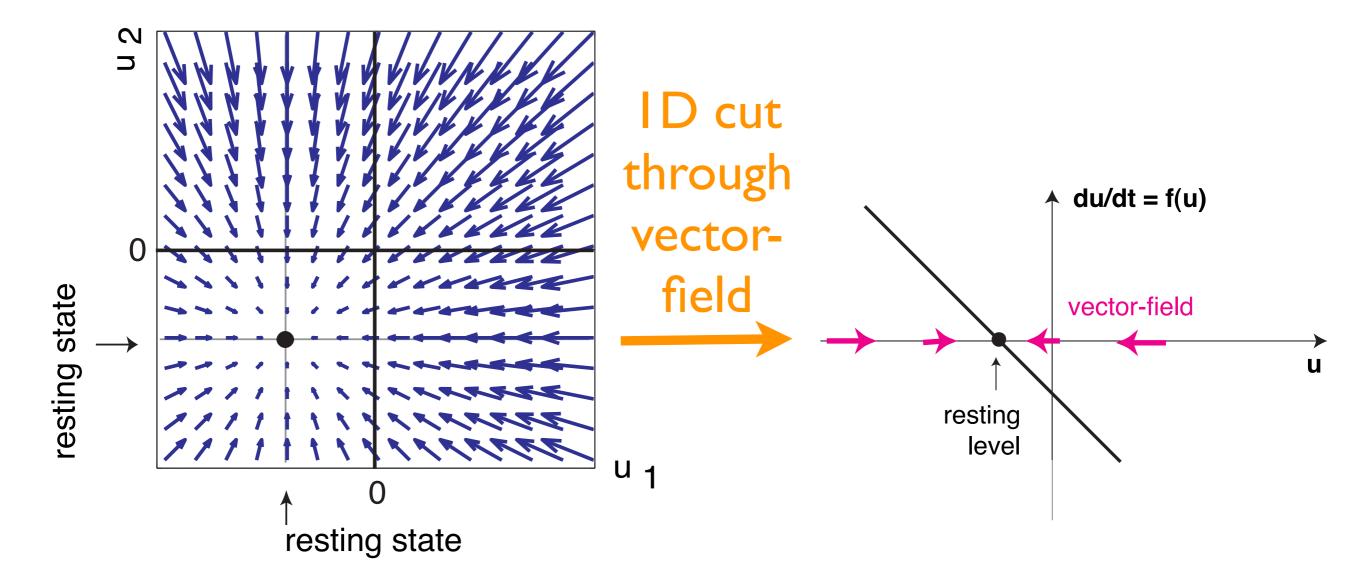
- to visualize, assume that u_2 has been activated by input to positive level
- => then u_l is suppressed



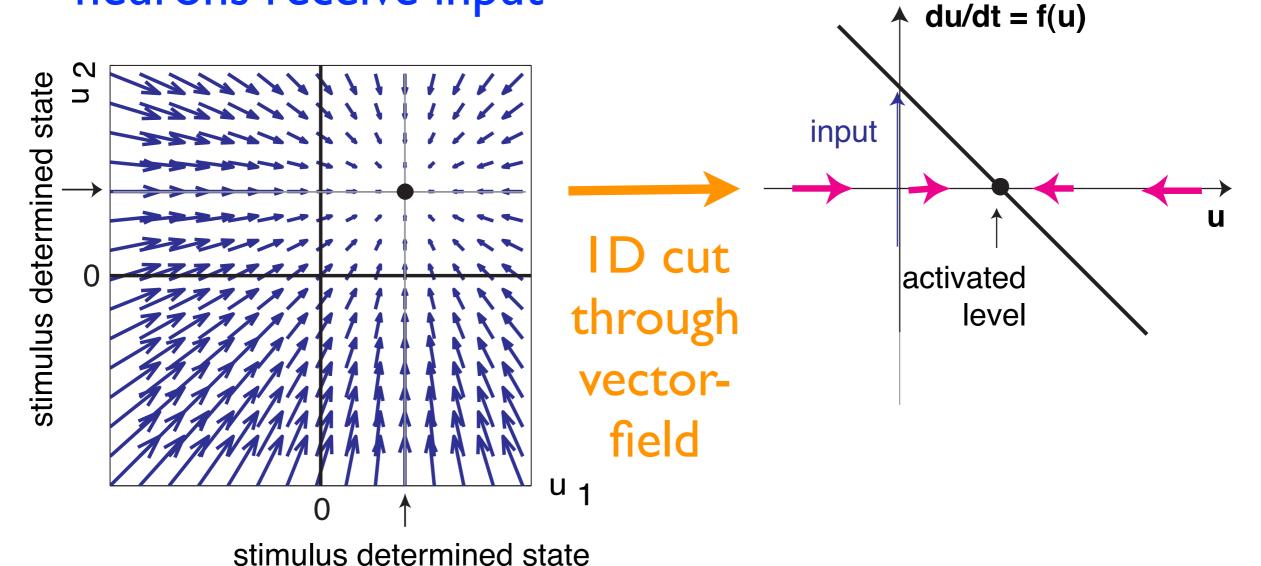
- why would u_2 be positive before u_I is? E.g., it grew faster than u_I because its inputs are stronger/inputs match better
- => input advantage translates into time advantage which translates into competitive advantage



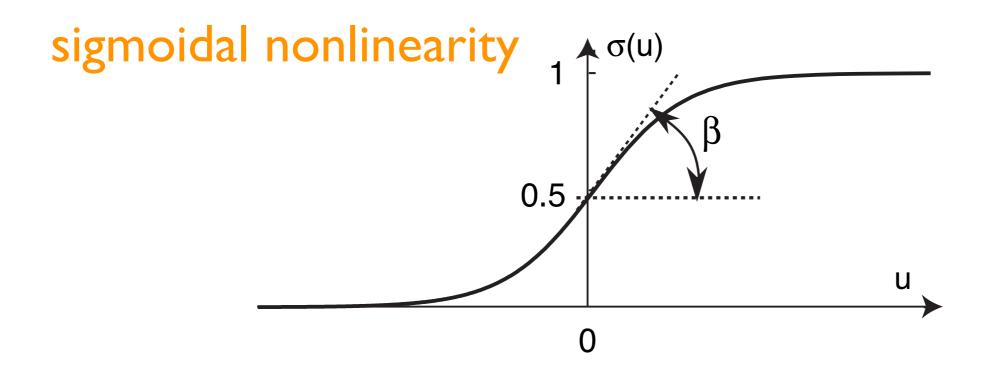
vector-field in the absence of input



vector-field (without interaction) when both neurons receive input



only activated neurons participate in interaction!

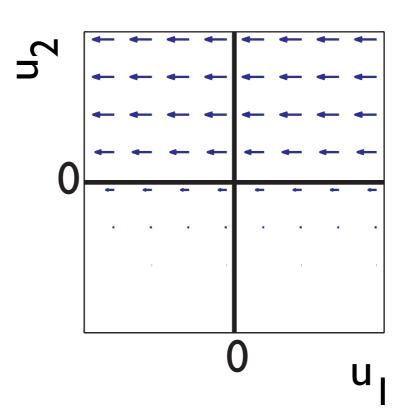


vector-field of mutual inhibition

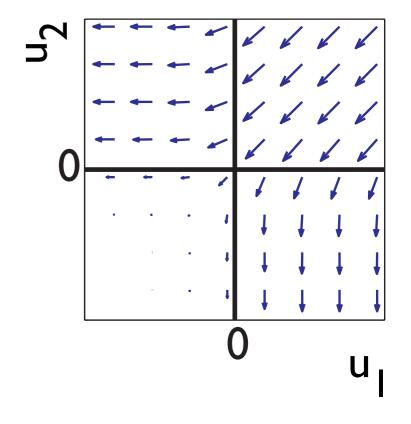
site I inhibits site 2

D U

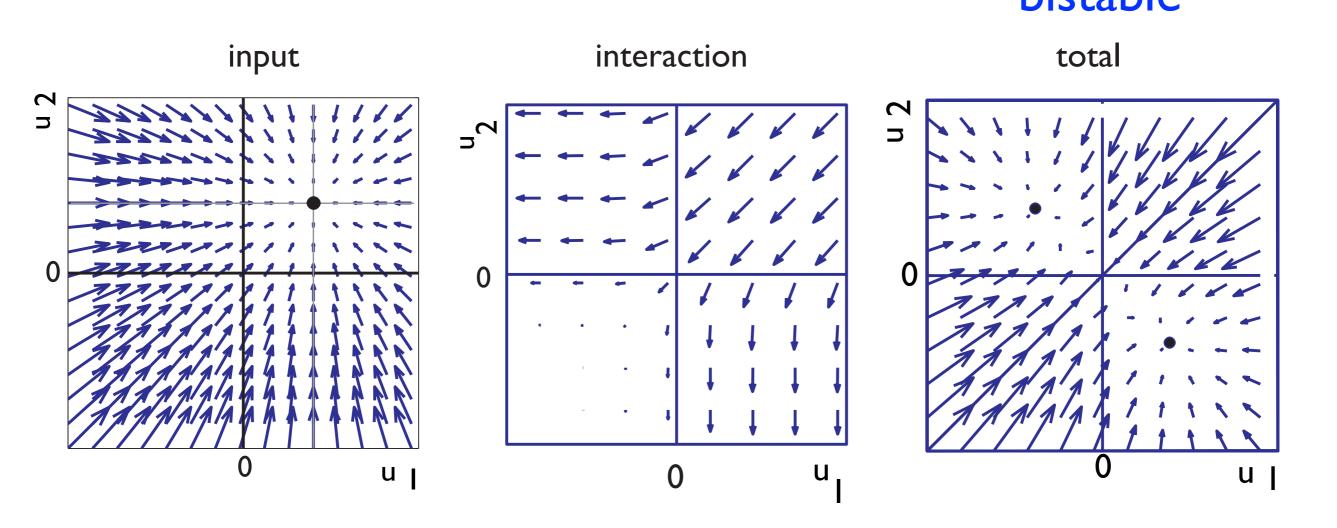
site 2 inhibits site I



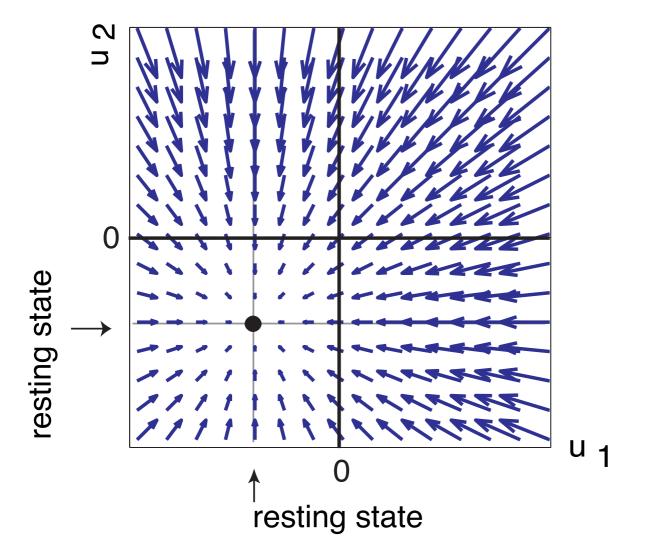
interaction combined



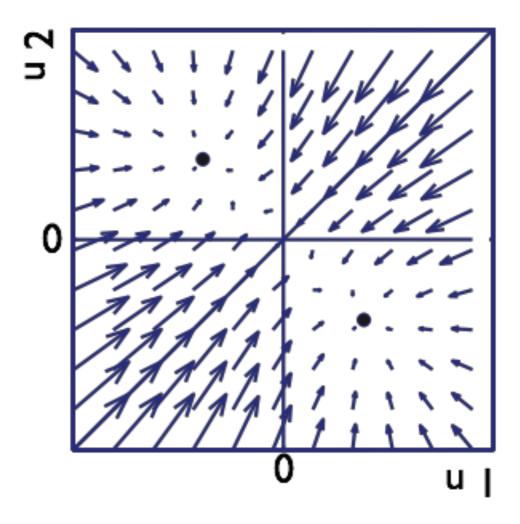
vector-field with strong mutual inhibition:
bistable



before input is presented

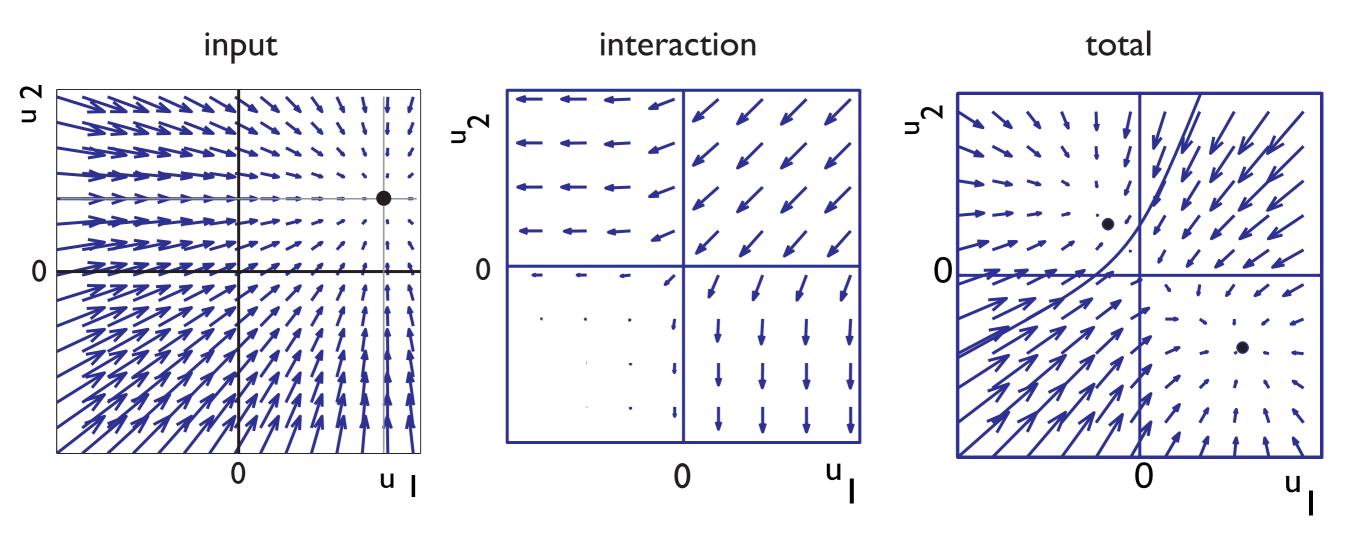


after input is presented



Neuronal dynamics with competition =>biased competition

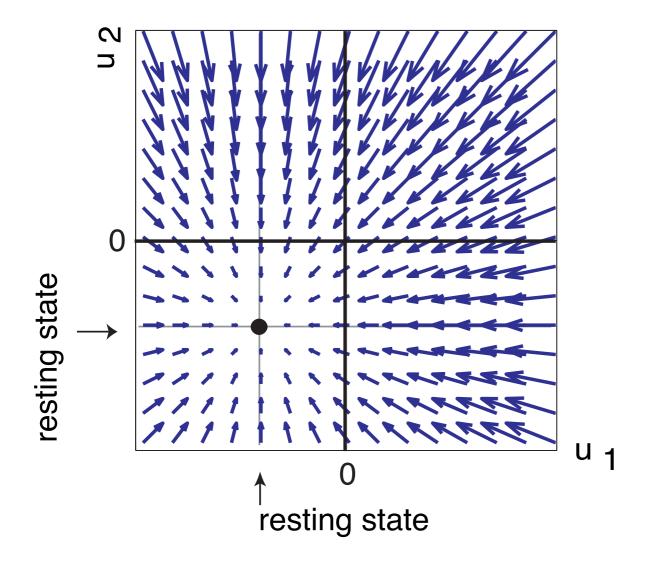
attractor with activated u_l stronger, attractor with activated u_l become unstable

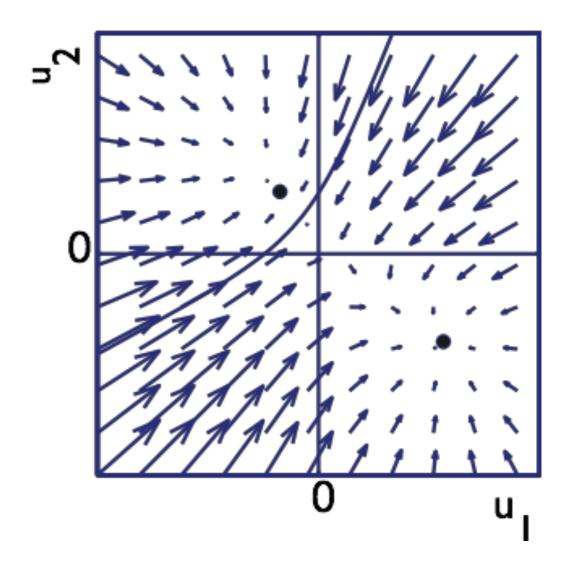


Neuronal dynamics with competition =>biased competition

before input is presented

after input is presented







- => hands-on exercise NOW
- in the robotics lab..

next

- where do activation variables come from?
- => DFT lecture