

# Dynamic Field Theory: Linking back to motor behavior

Gregor Schöner

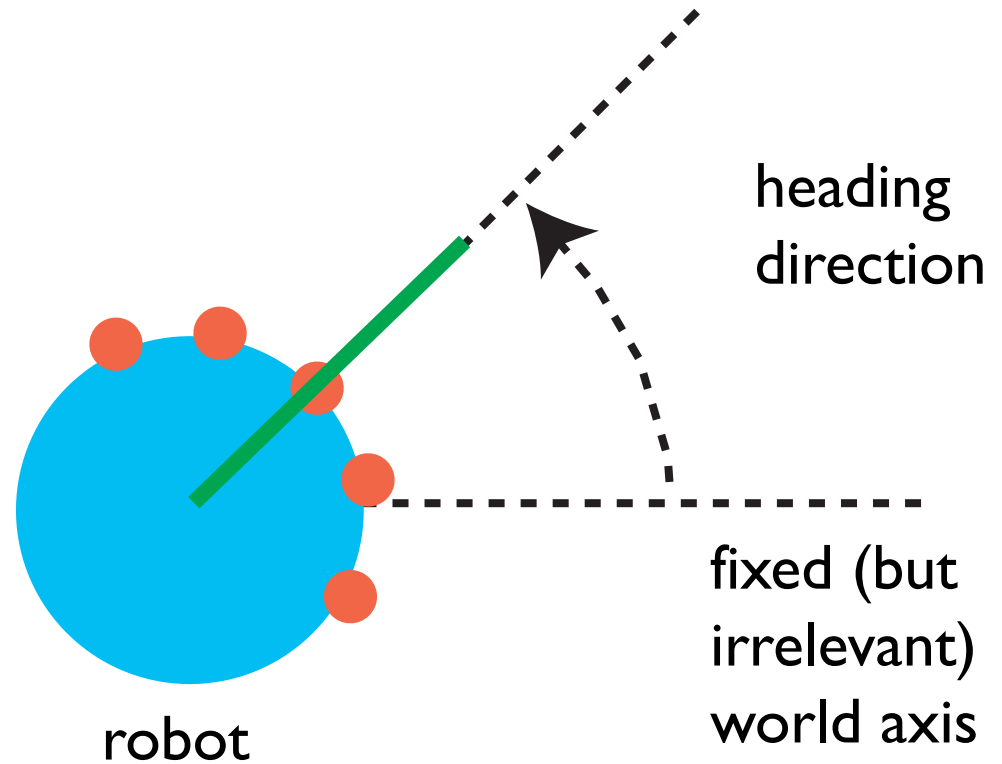
[gregor.schoener@ini.rub.de](mailto:gregor.schoener@ini.rub.de)

# Generating motor behavior

■ > behavioral dynamics

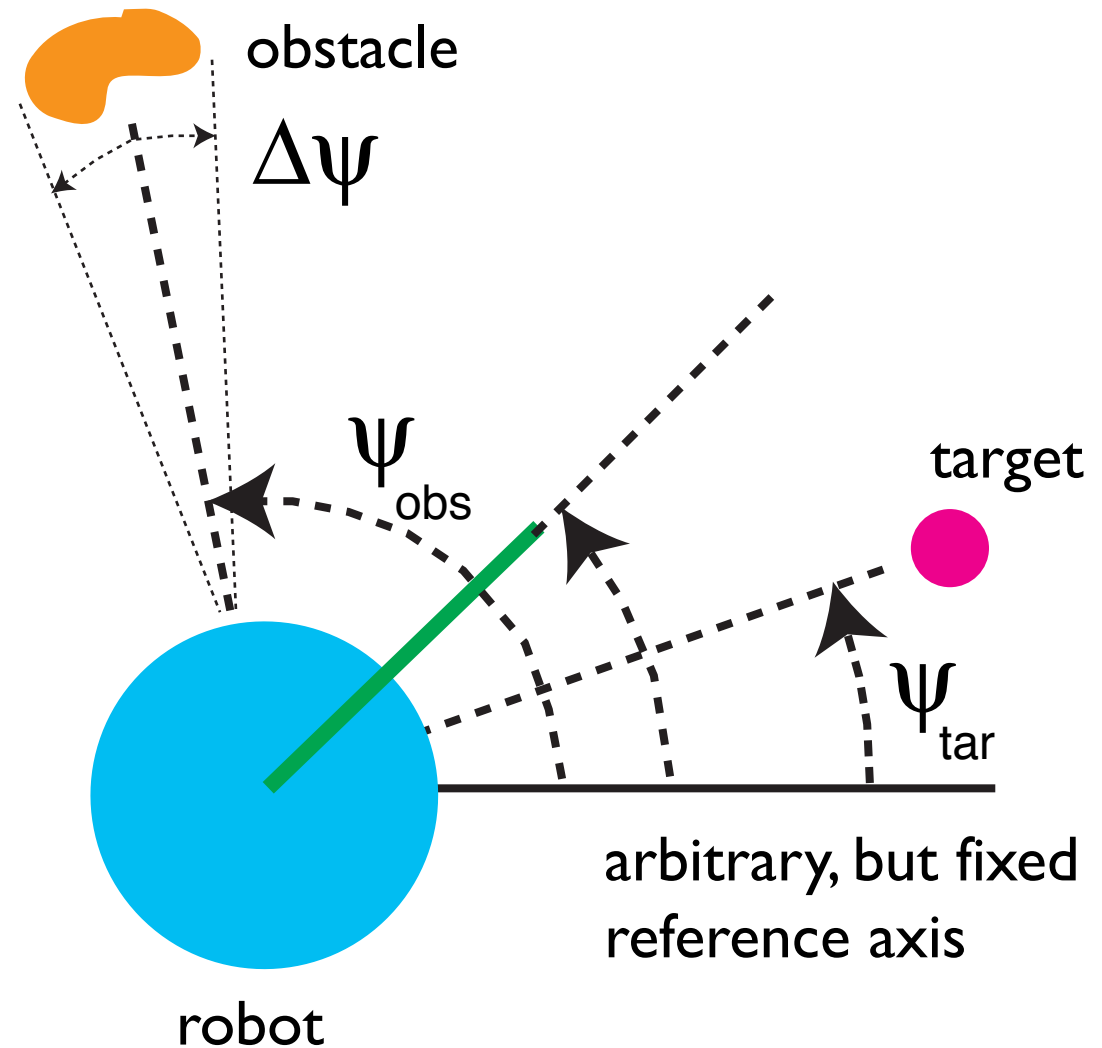
# Behavioral variables: example

■ vehicle moving in  
2D: heading  
direction



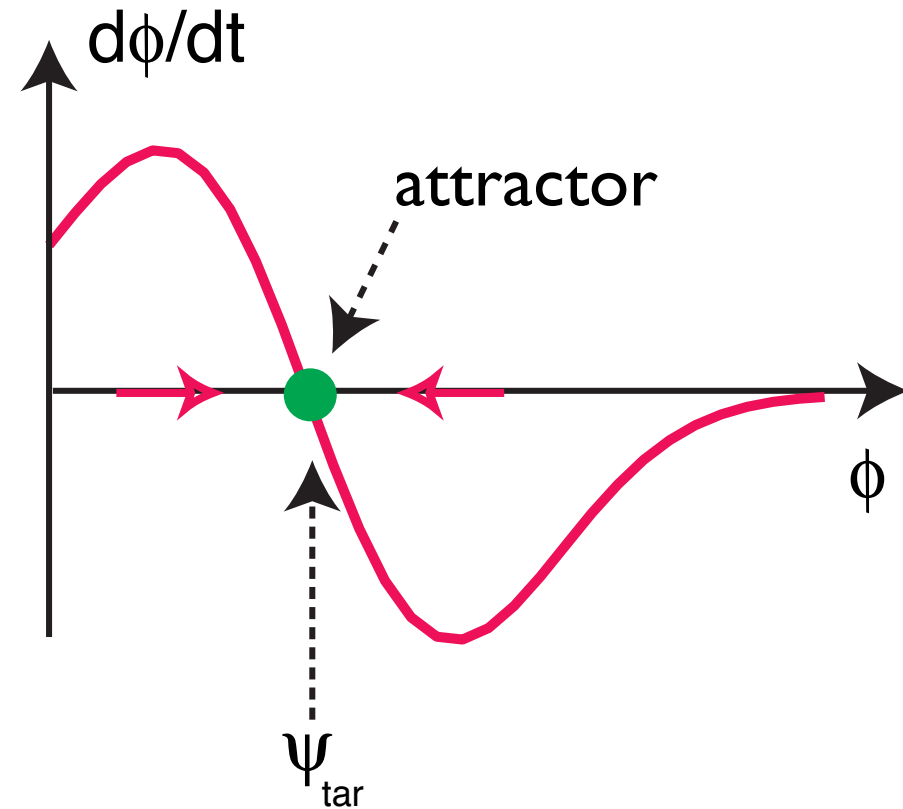
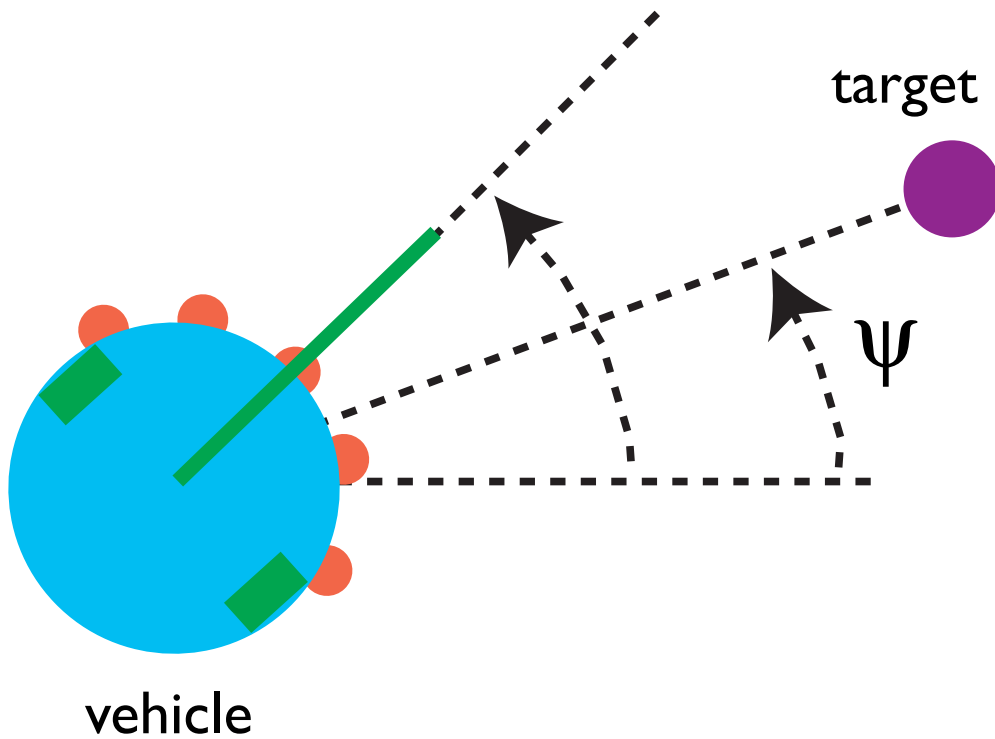
# Behavioral variables: example

- constraints:  
obstacle avoidance  
and target  
acquisition



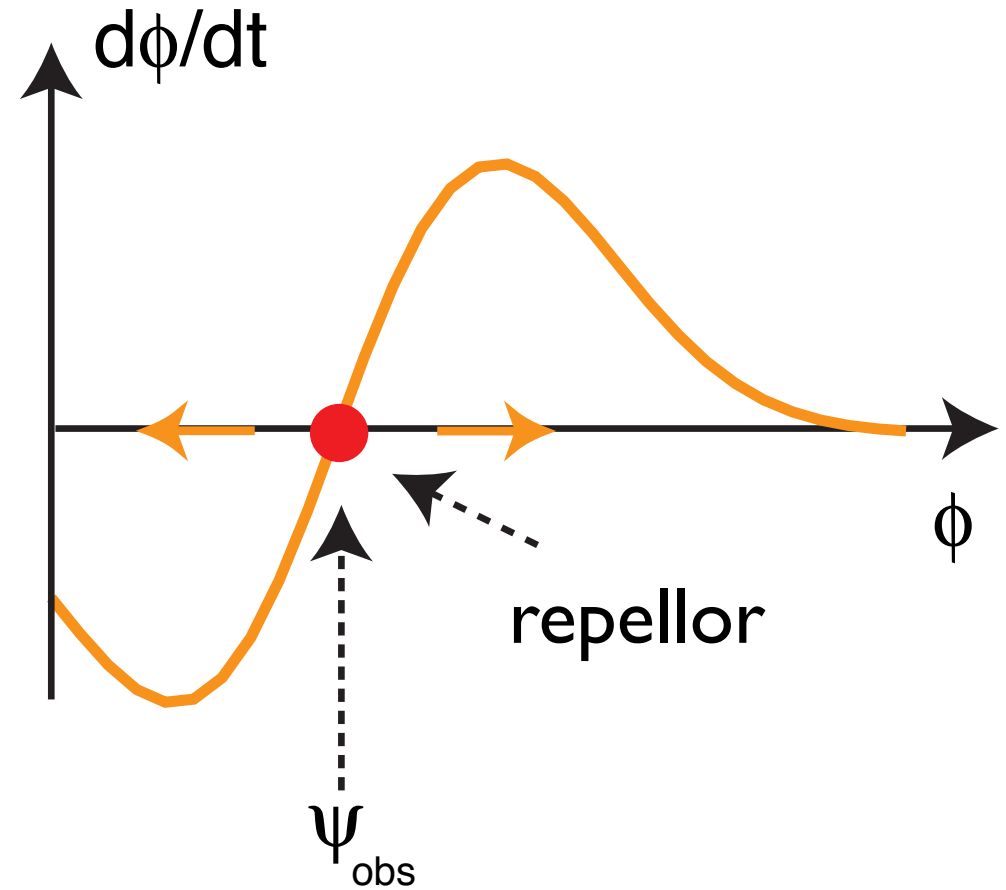
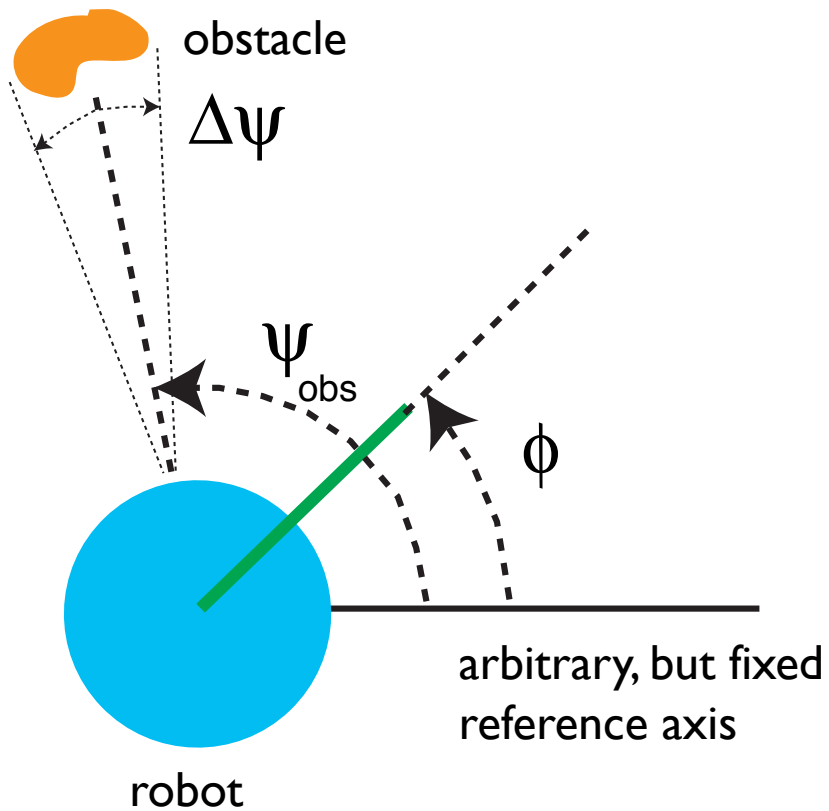
# Behavioral dynamics: example

■ behavioral constraint: target acquisition



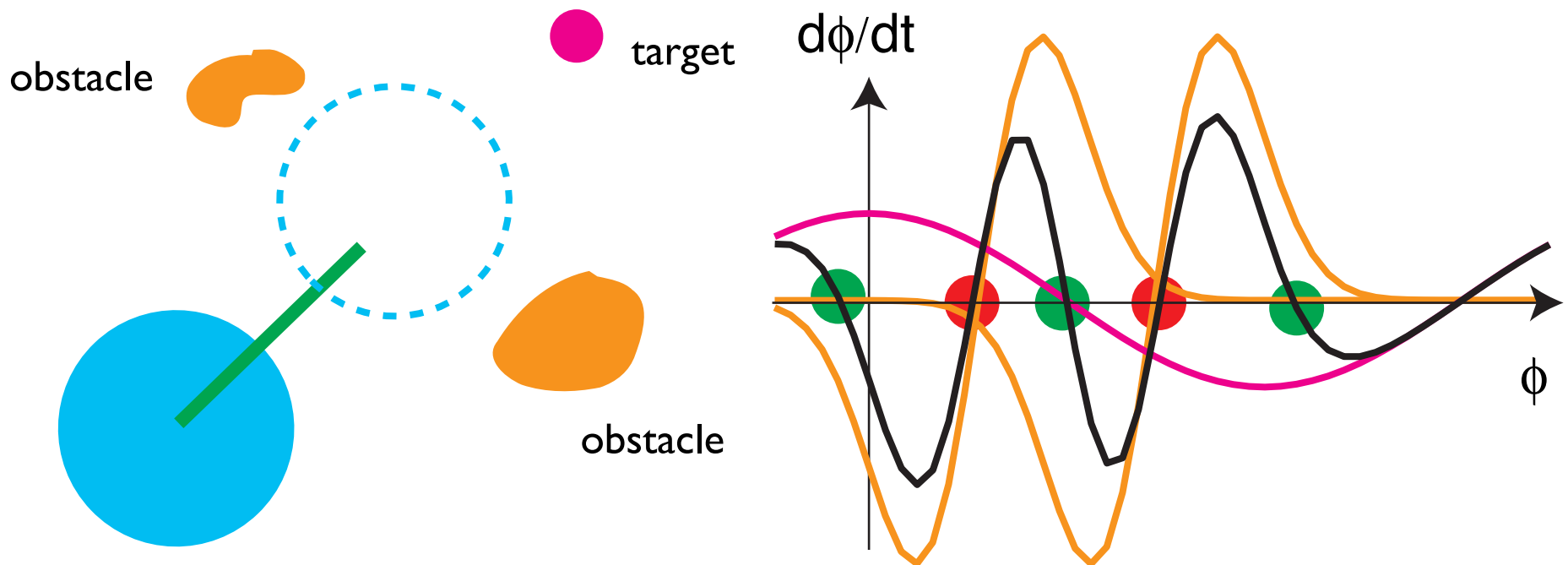
# Behavioral dynamics: example

■ behavioral constraint: obstacle avoidance



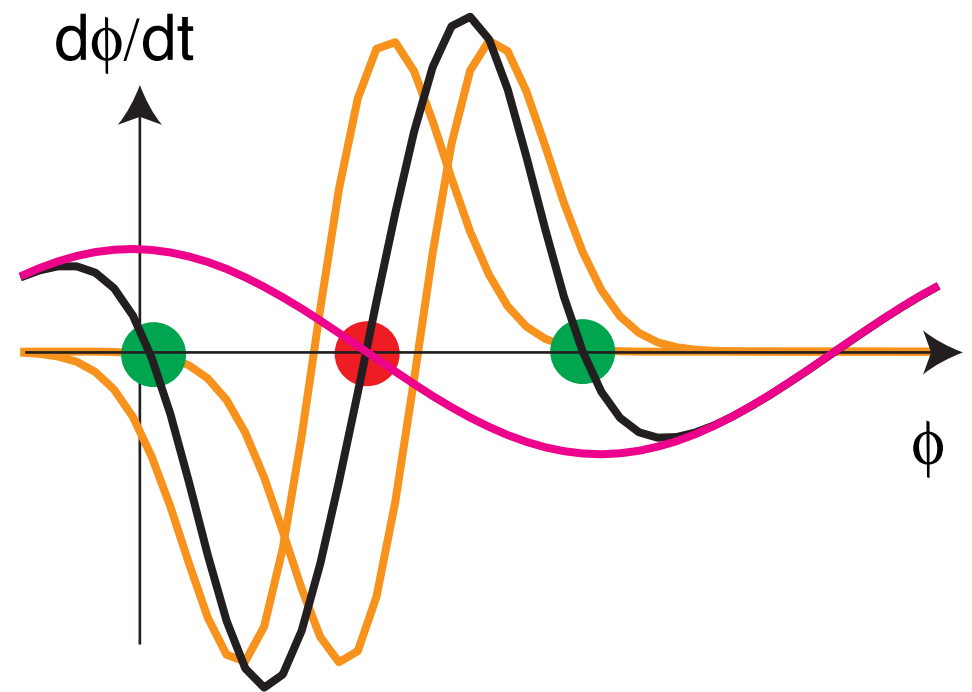
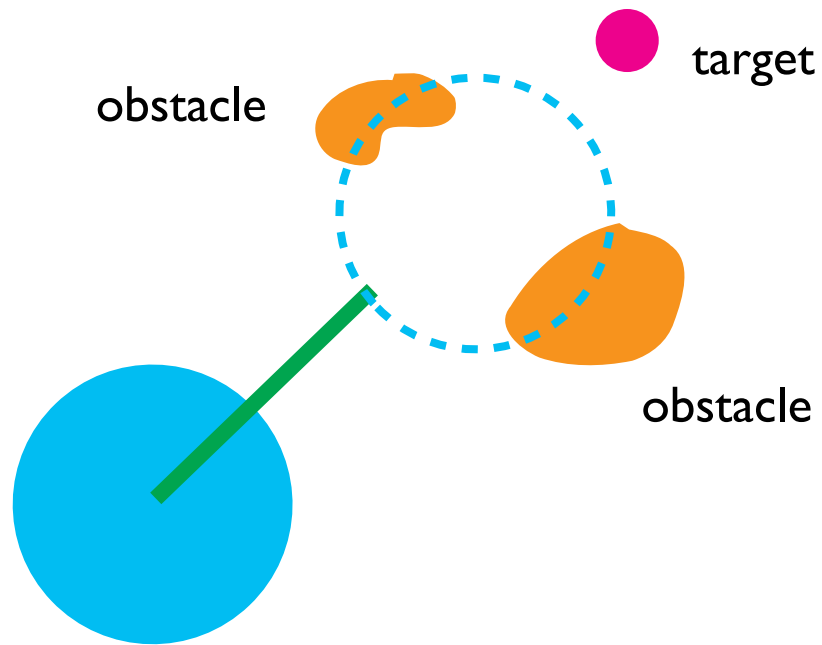
# Behavioral dynamics

- bifurcations in obstacle avoidance and target acquisition
- constraints not in conflict



# Behavioral dynamics

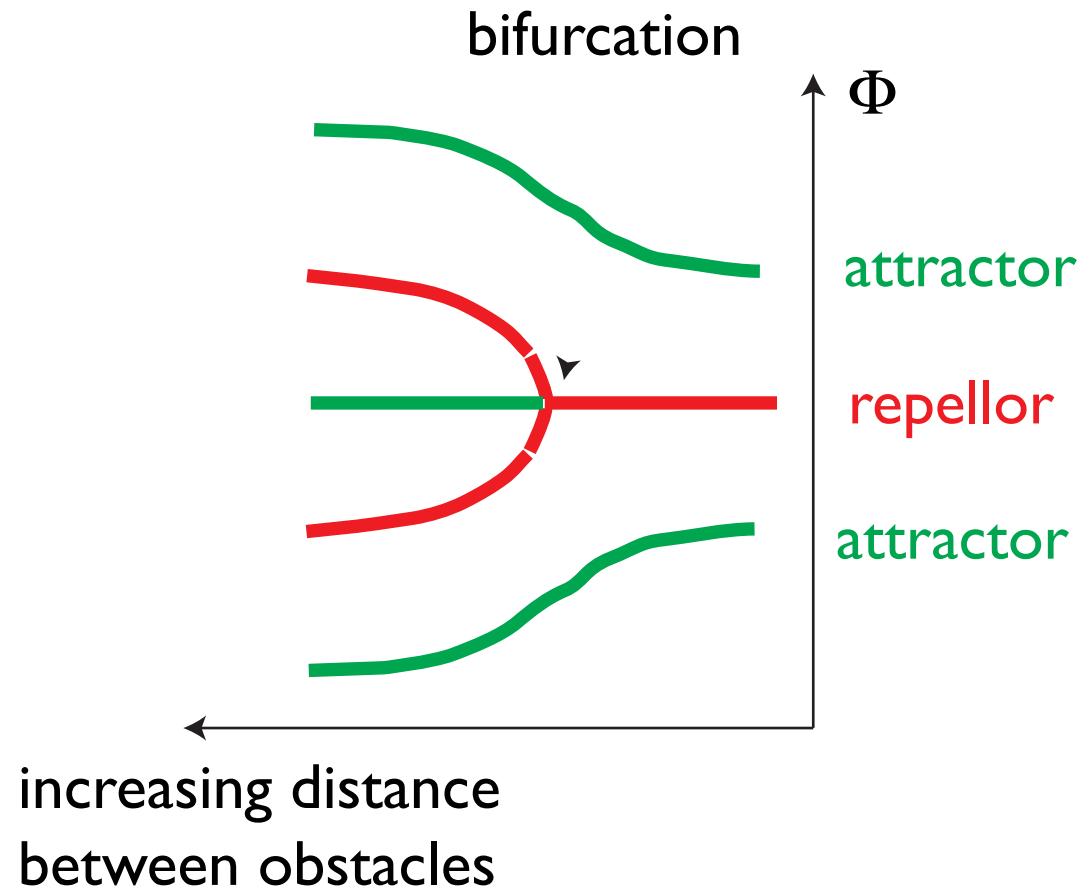
■ constraints in conflict

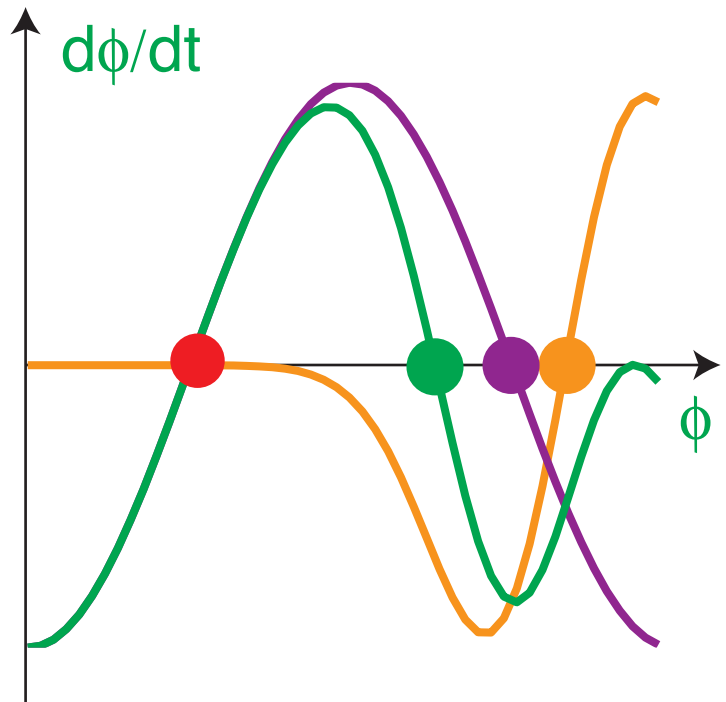
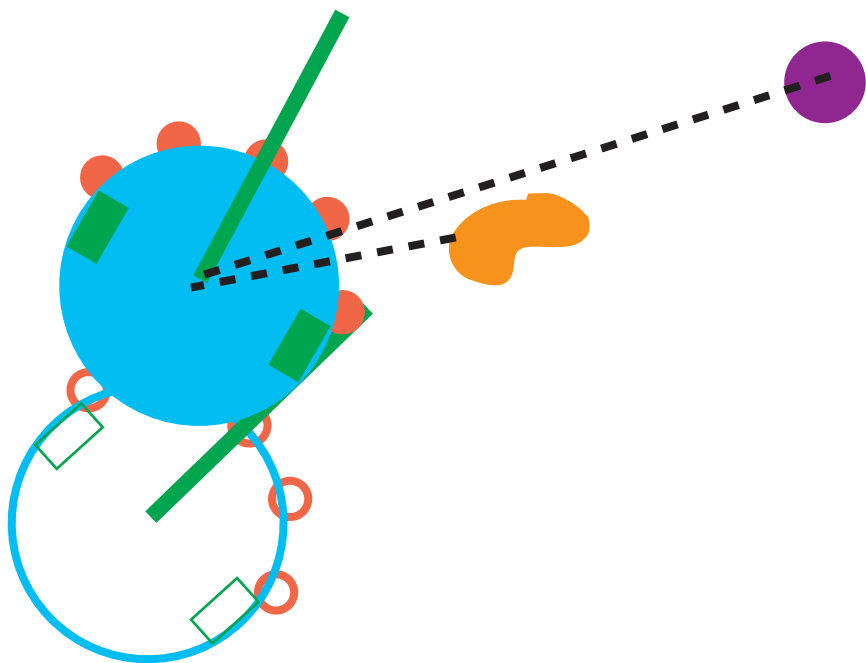
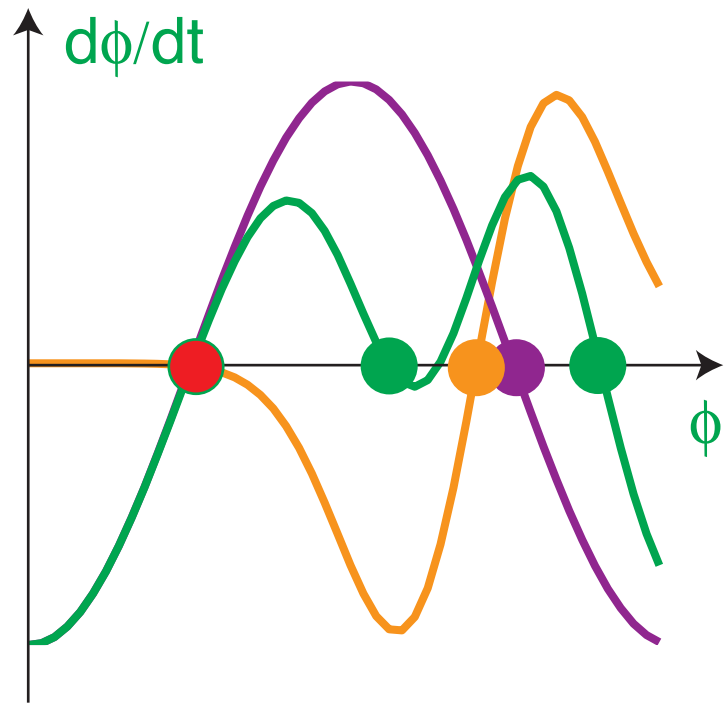
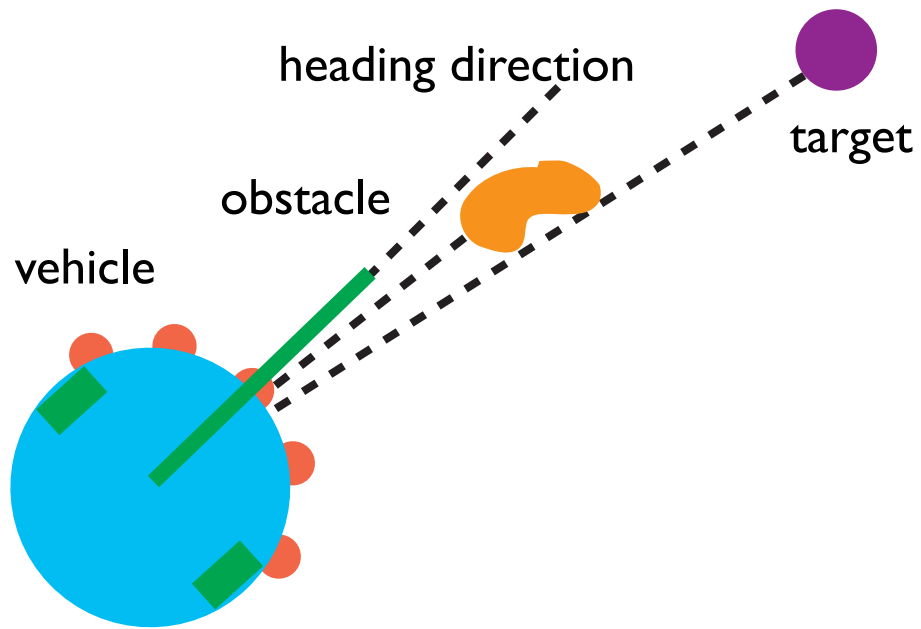




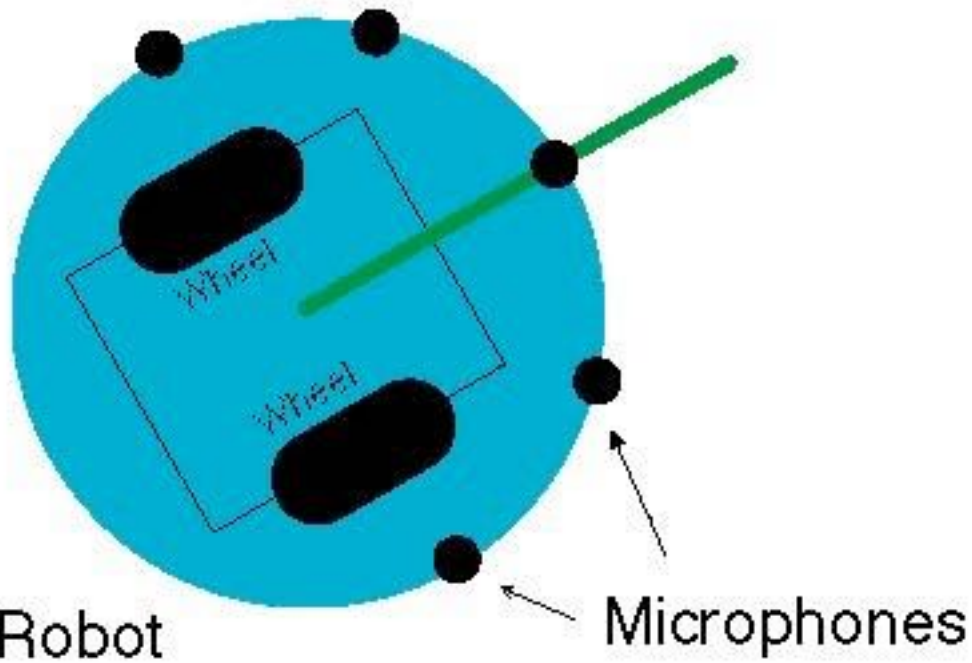
# Behavioral dynamics

- transition from “constraints not in conflict” to “constraints in conflict” is a bifurcation





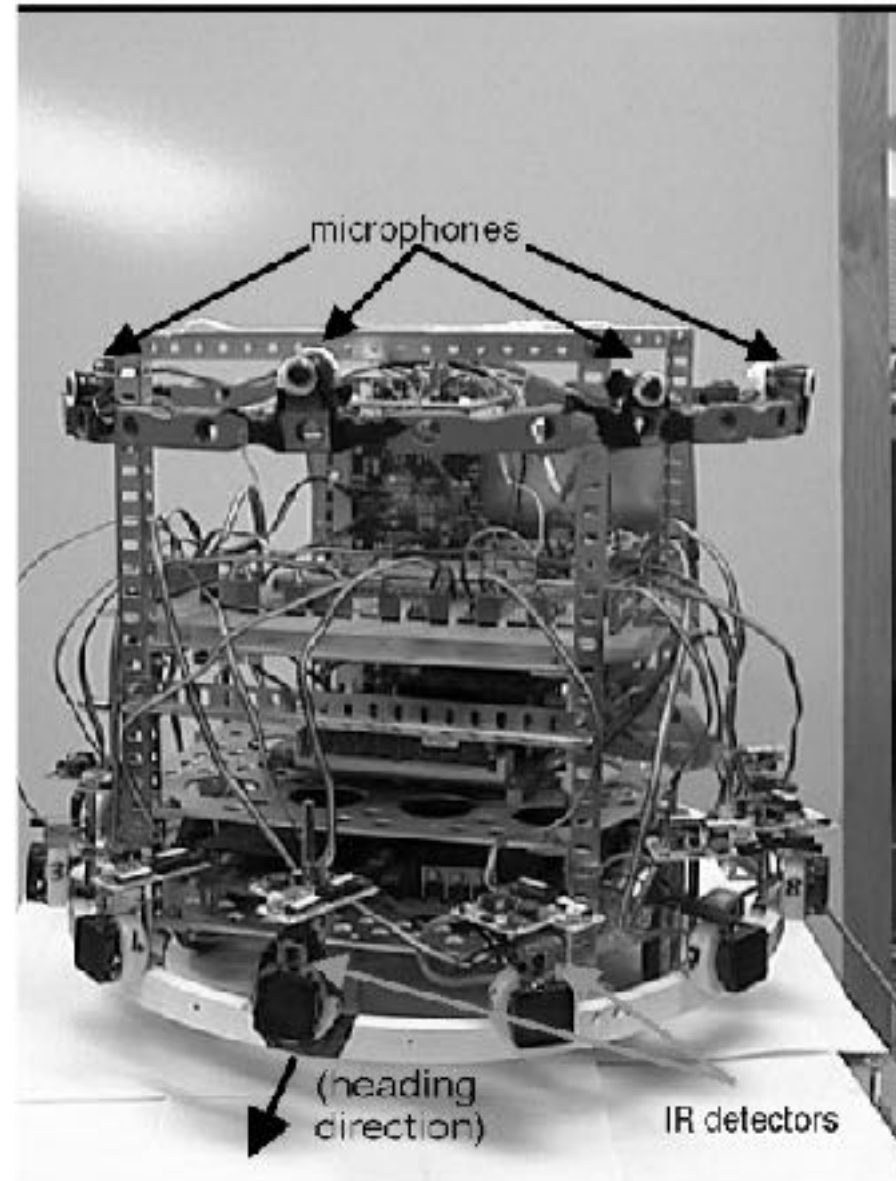
# Vehicle



Robot

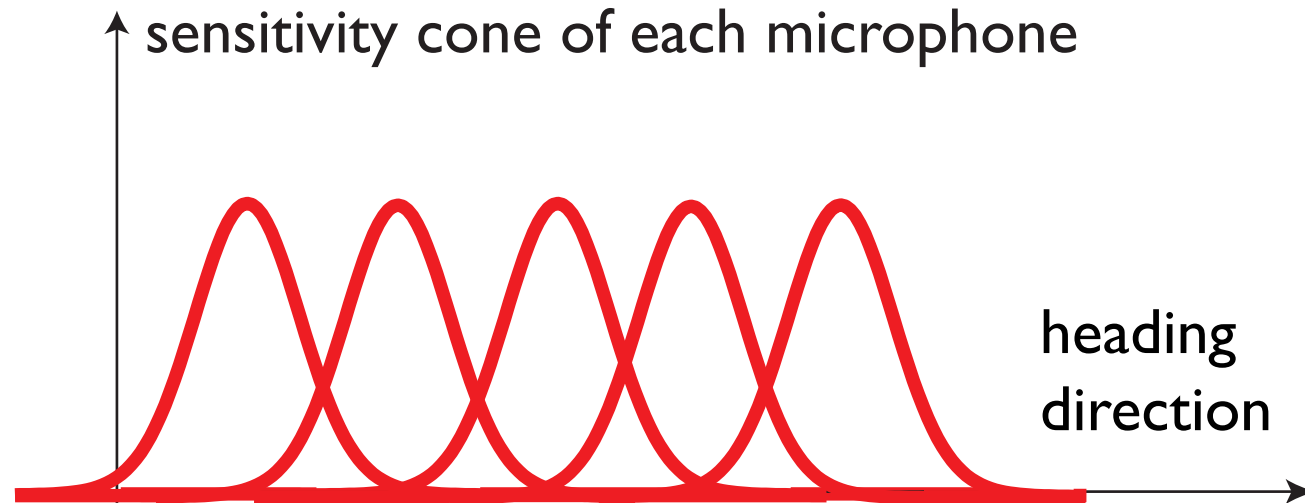
Microphones

[from Bicho, Mallet, Schöner, Int J Rob Res, 2000]

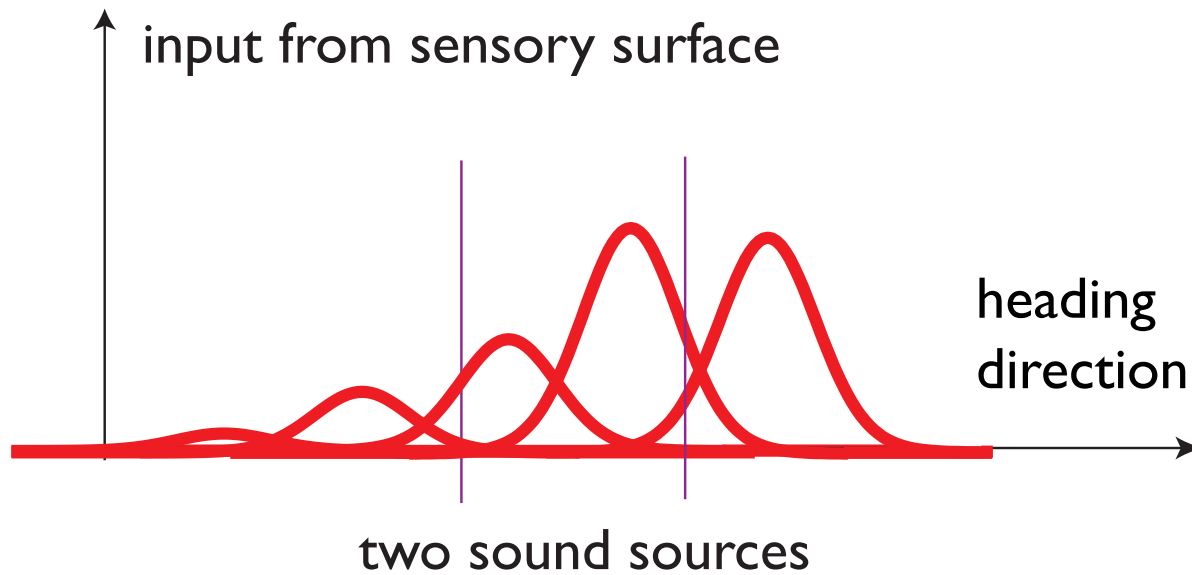
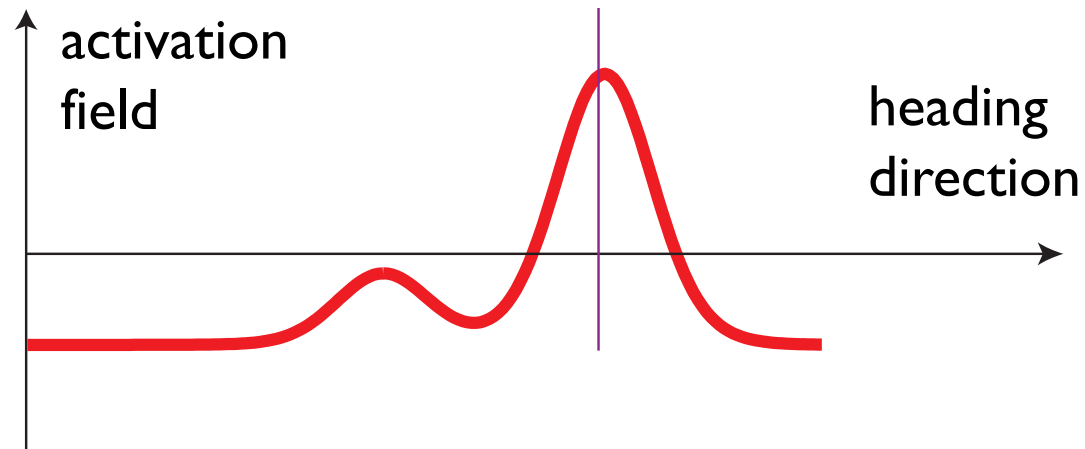


# sensory surface

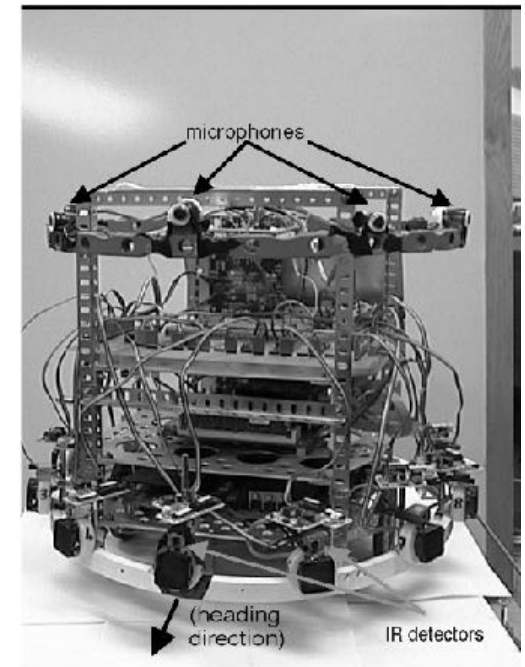
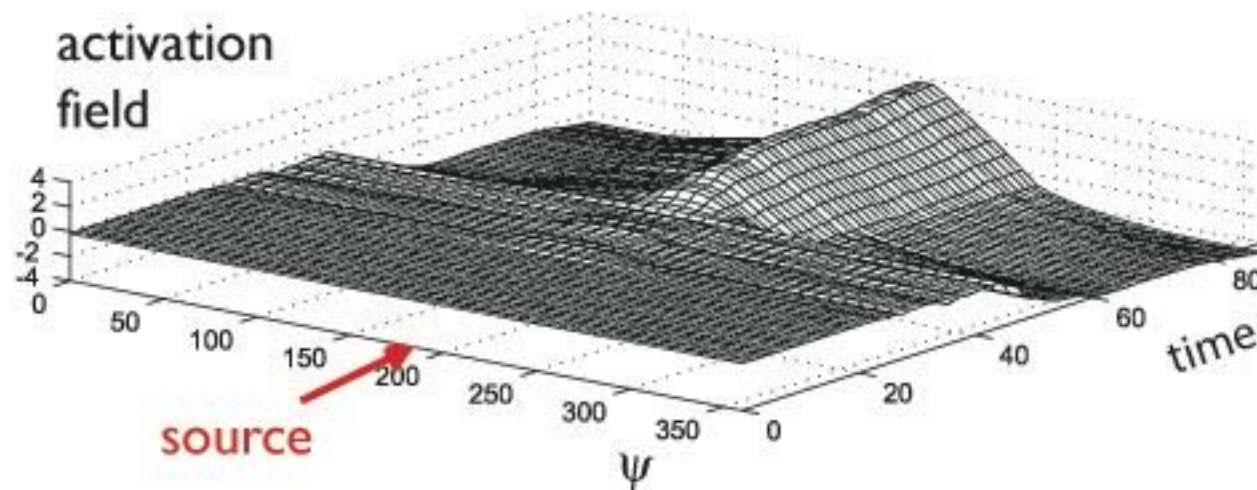
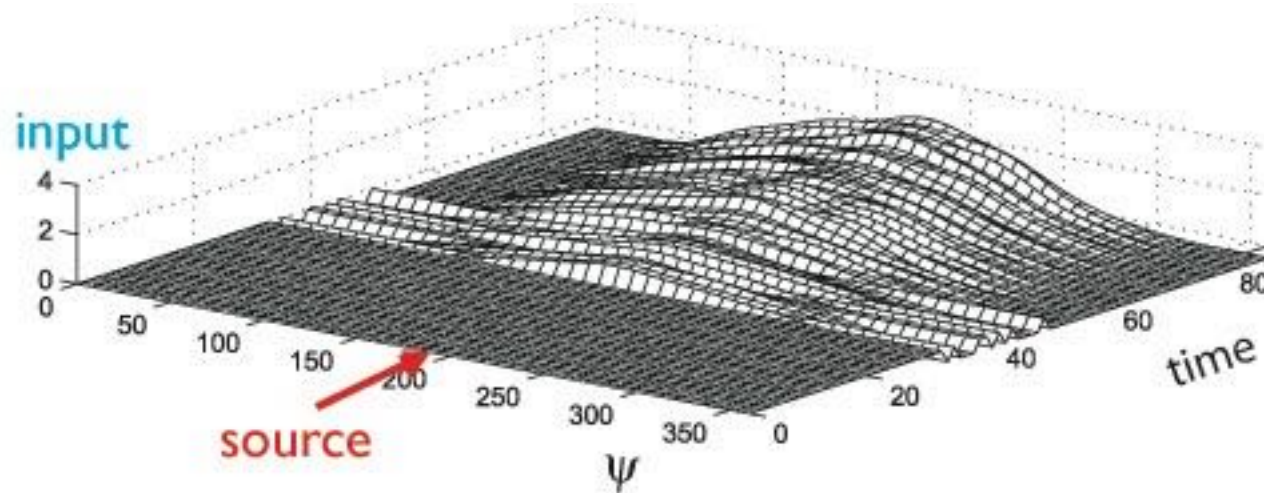
- each microphone samples heading direction



# and provides input to the field



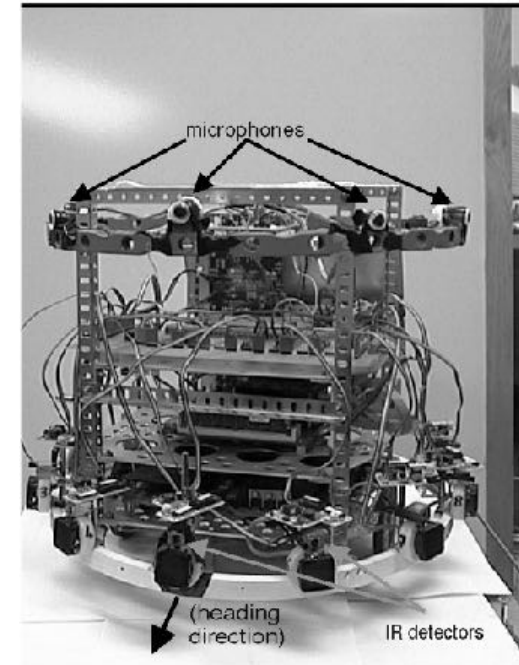
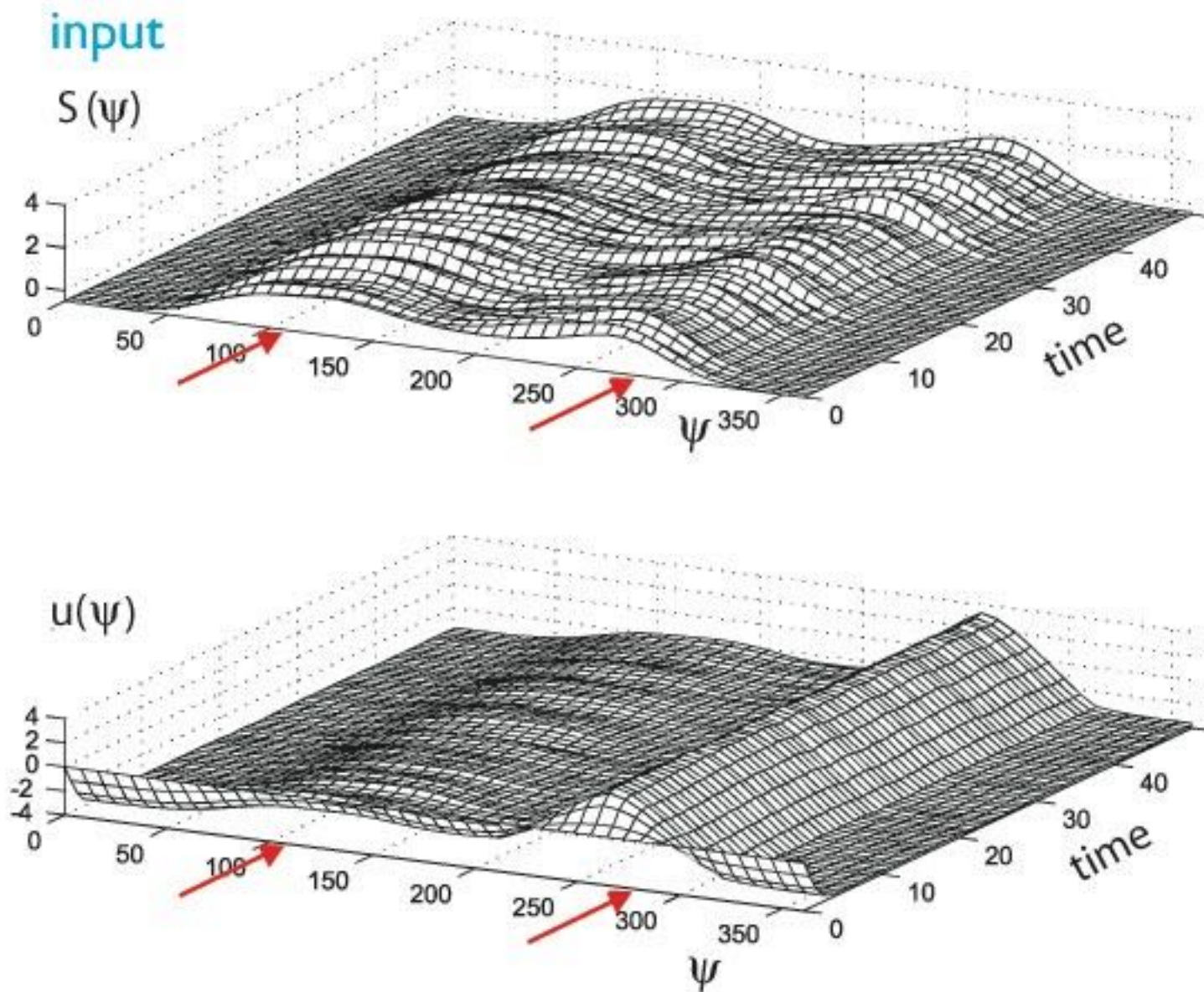
# detection instability on a phonotaxis robot



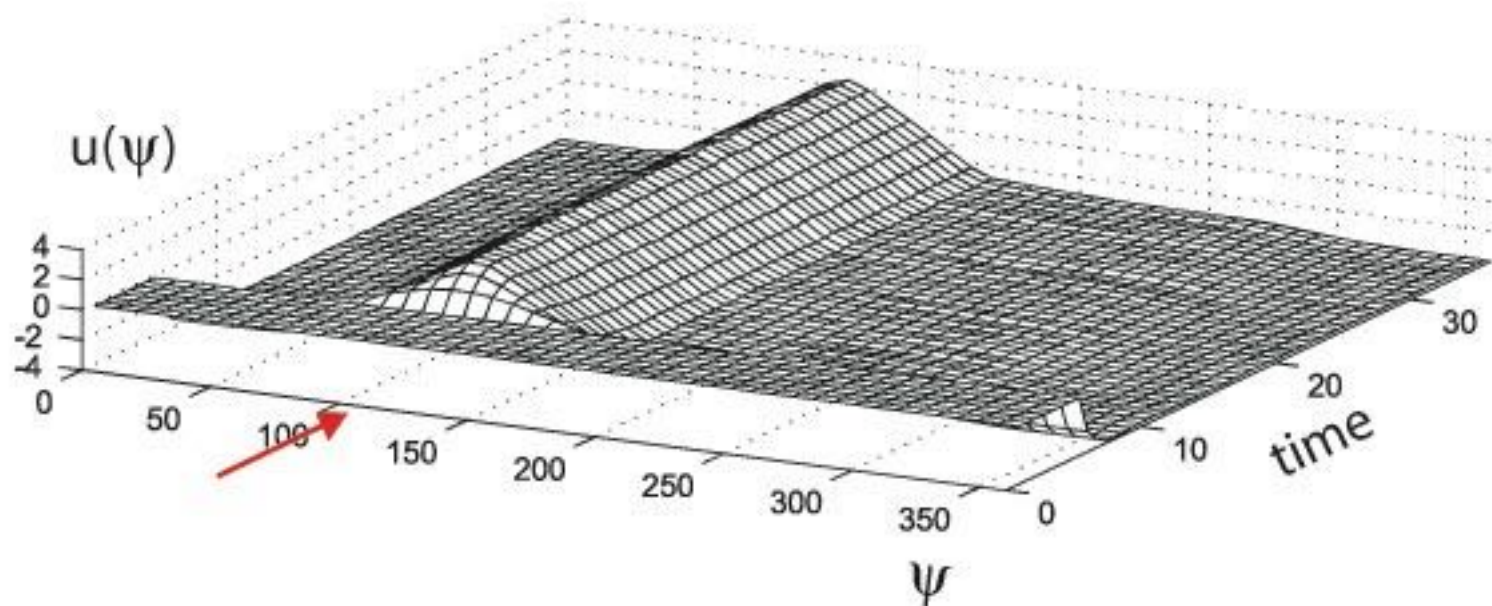
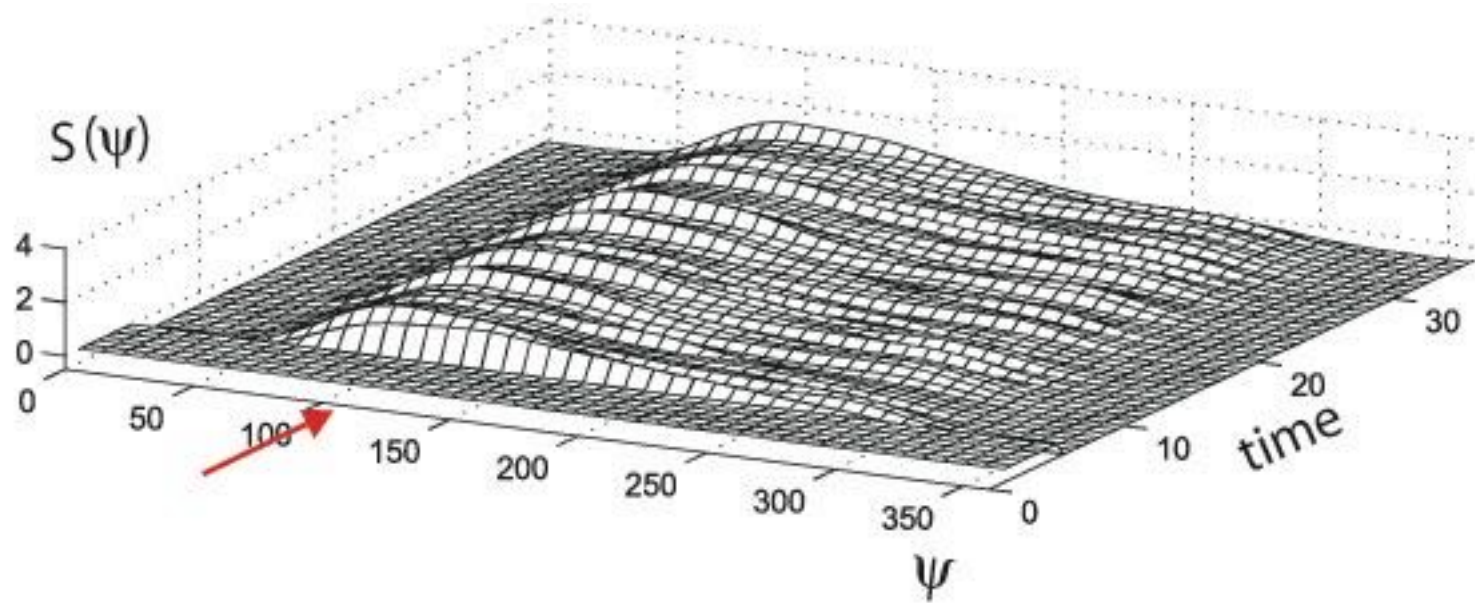
[from Bicho, Mallet, Schöner: Int. J. Rob. Res., 2000]



# target selection on phonotaxis vehicle

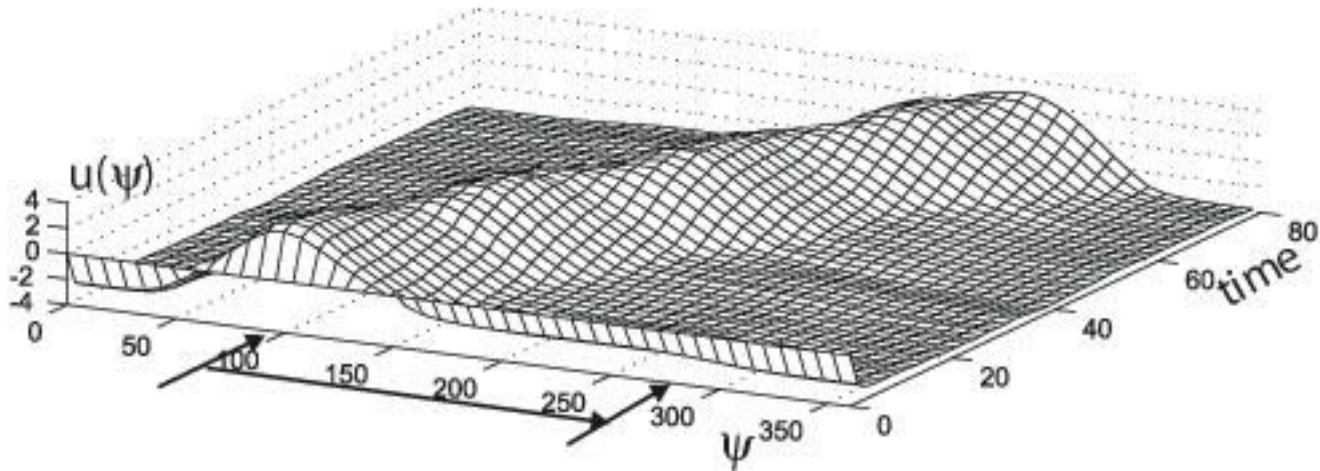
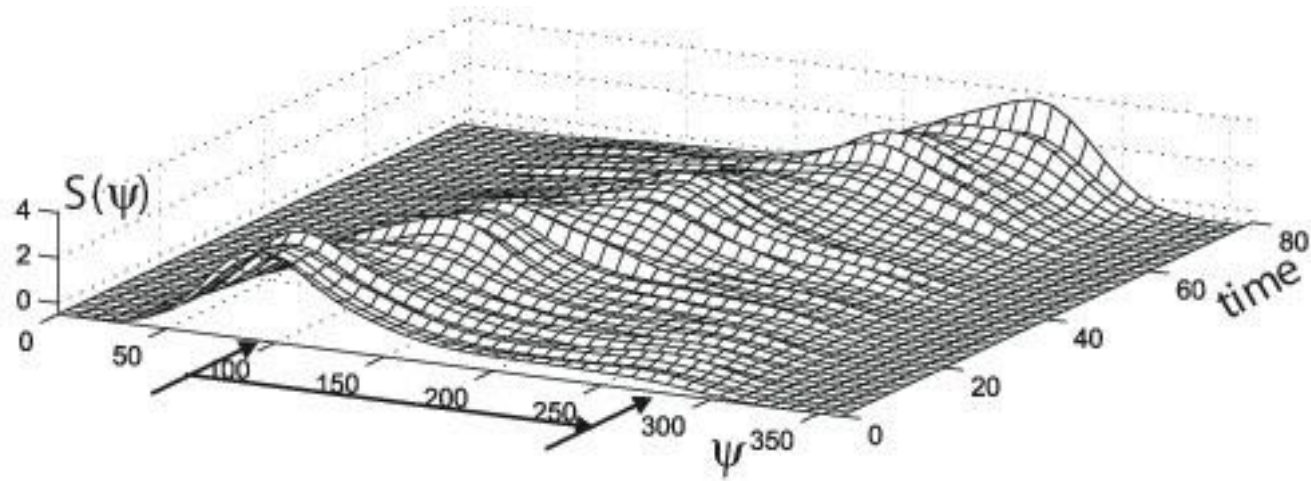


# robust estimation

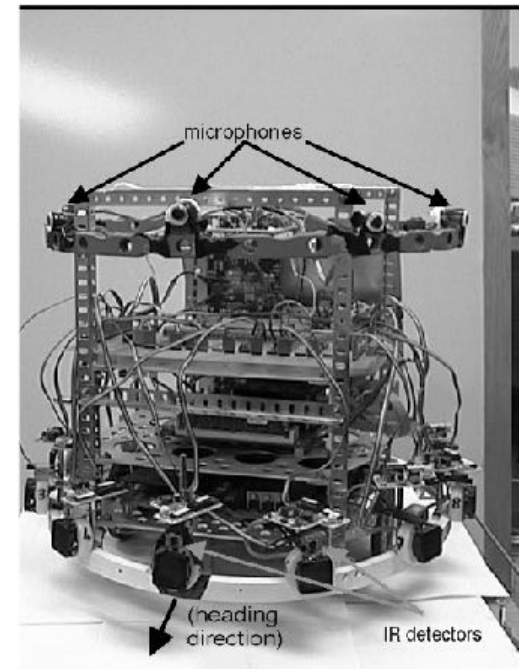
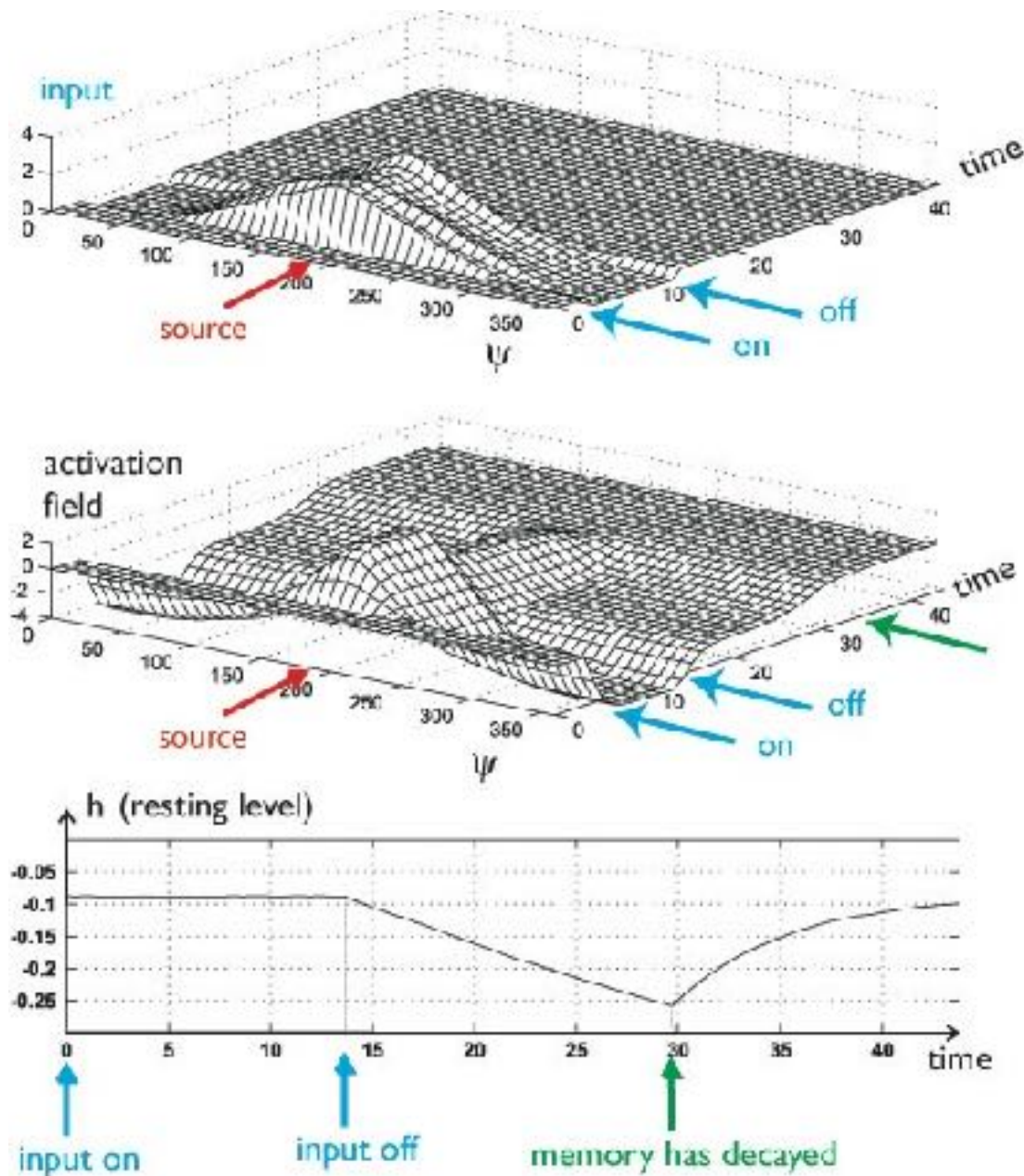




# tracking



# memory & forgetting on phonotaxis vehicle

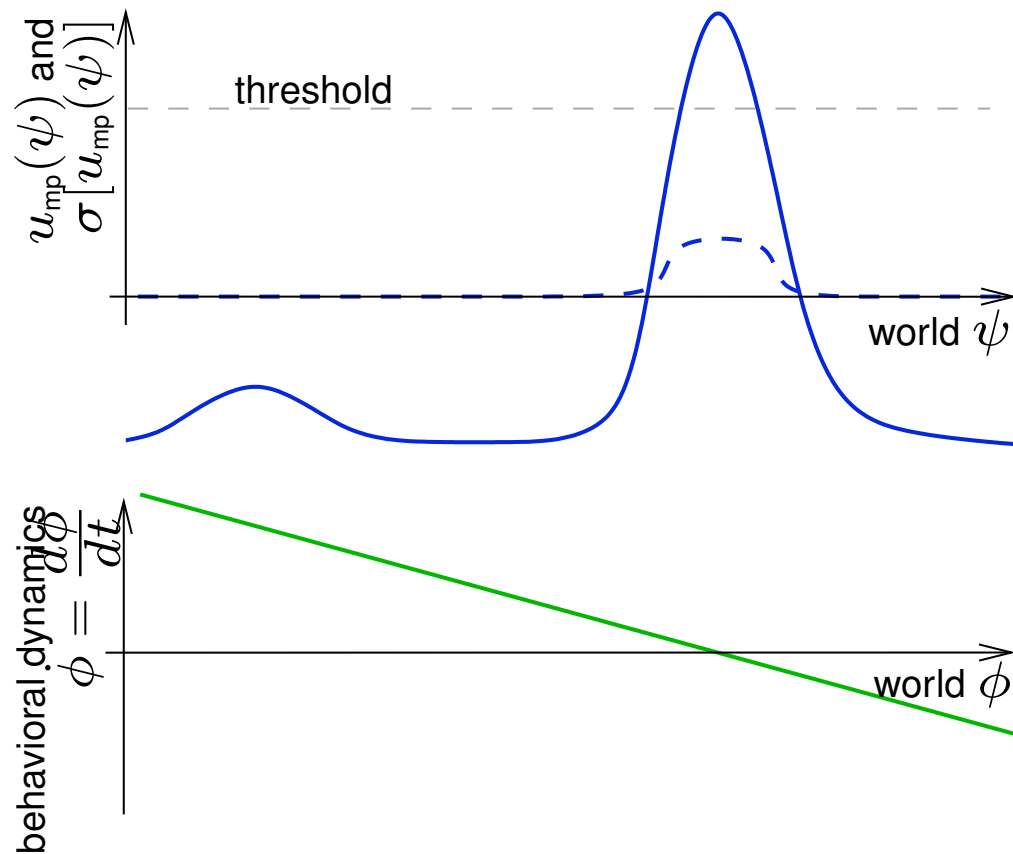


a robotic demo of all of instabilities



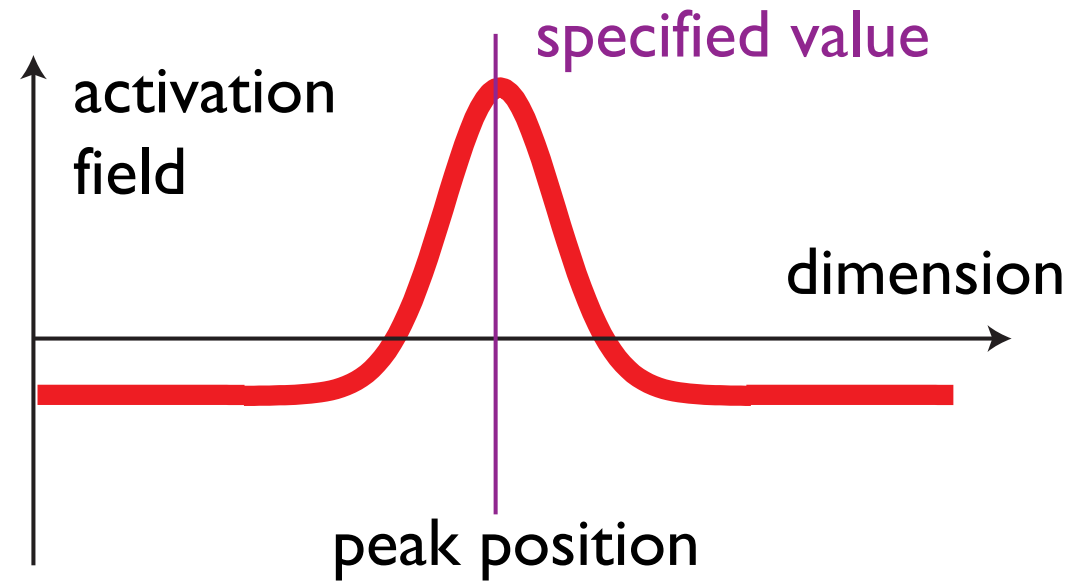
# back to attractor dynamics of heading

- couple peak in direction field into dynamics of heading direction as an attractor



# => transition from DFT to DST

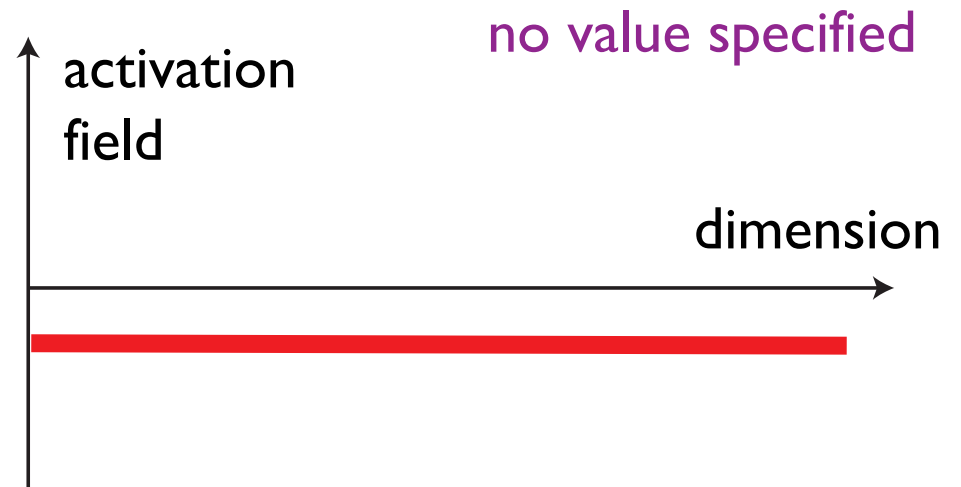
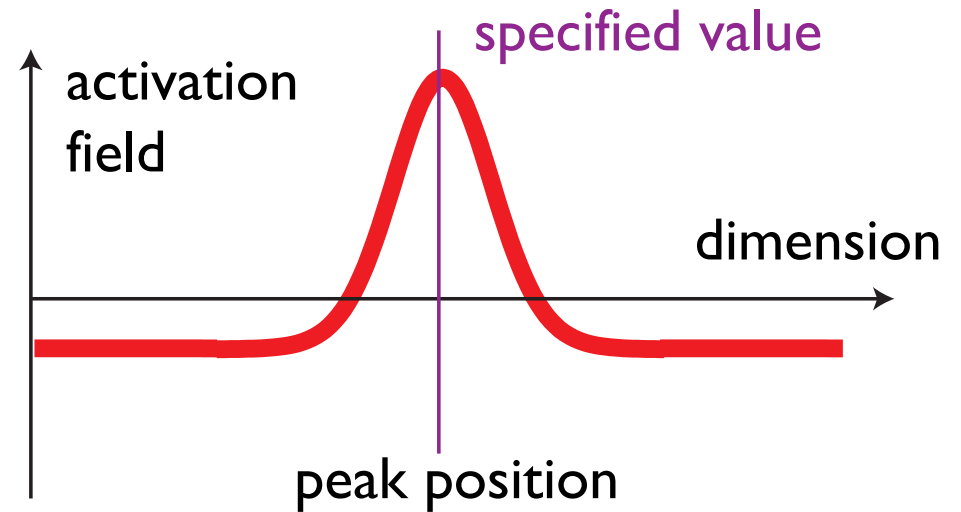
- peak specifies value for a dynamical variable that is congruent to the field dimension



# from DFT to DST

■ treating sigmoided field as probability: need to normalize

■ => problem when there is no peak: divide by zero!



# from DFT to DST

## ■ solution: peak sets attractor

■ location of attractor: peak location

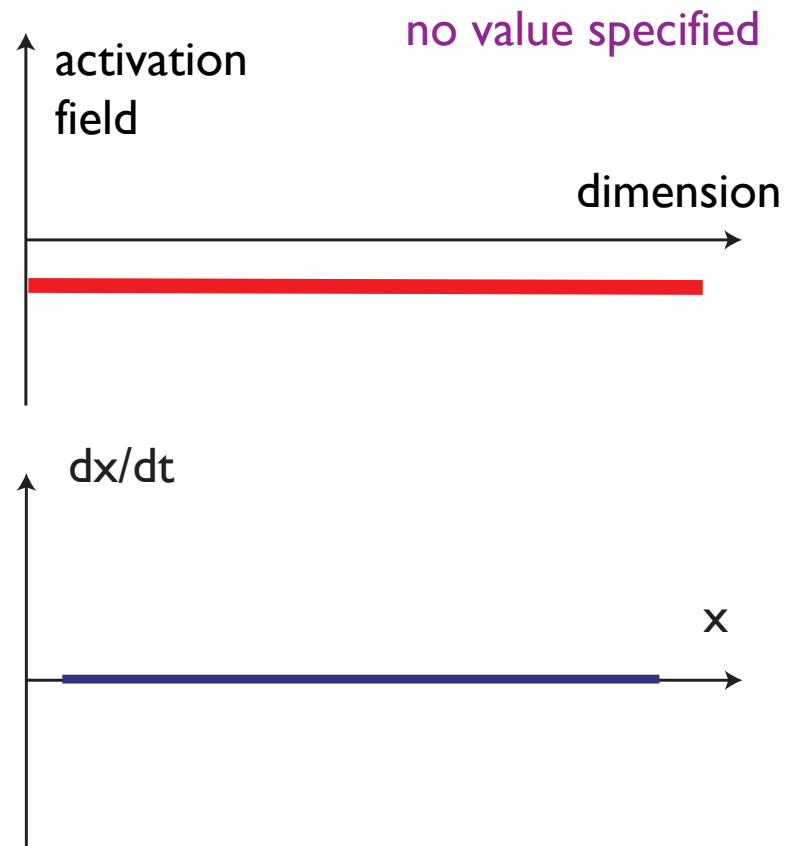
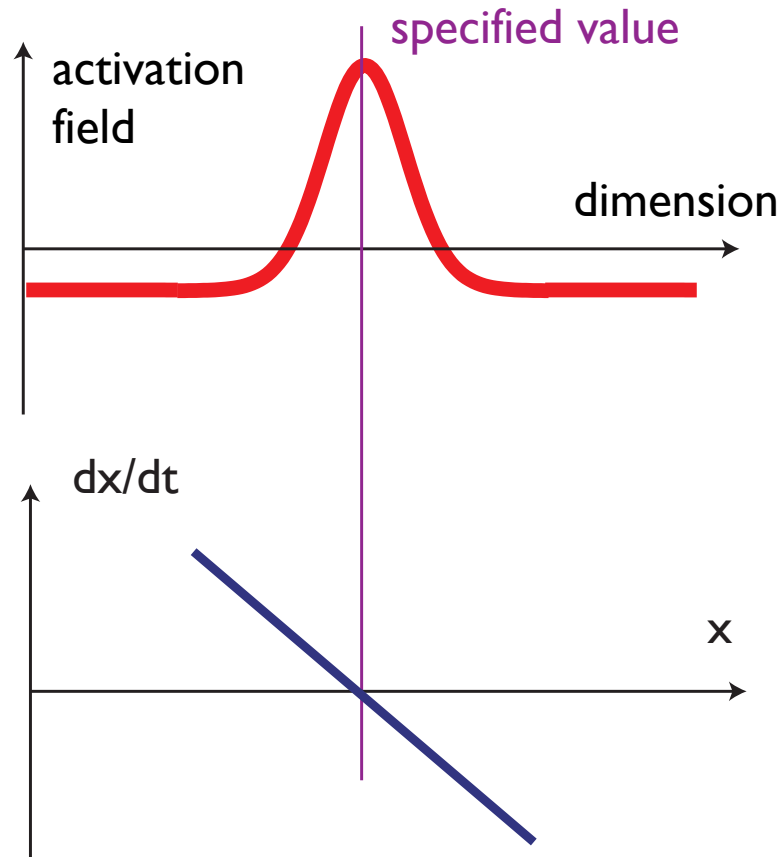
■ strength of attractor: summed supra-threshold activation

$$x_{\text{peak}} = \frac{\int dx x \sigma(u(x, t))}{\int dx \sigma(u(x, t))}$$

$$\dot{x} = - \left[ \int dx \sigma(u(x, t)) \right] (x - x_{\text{peak}})$$

$$\Rightarrow \dot{x} = - \left[ \int dx \sigma(u(x, t)) \right] x + \left[ \int dx x \sigma(u(x, t)) \right]$$

# from DFT to DST



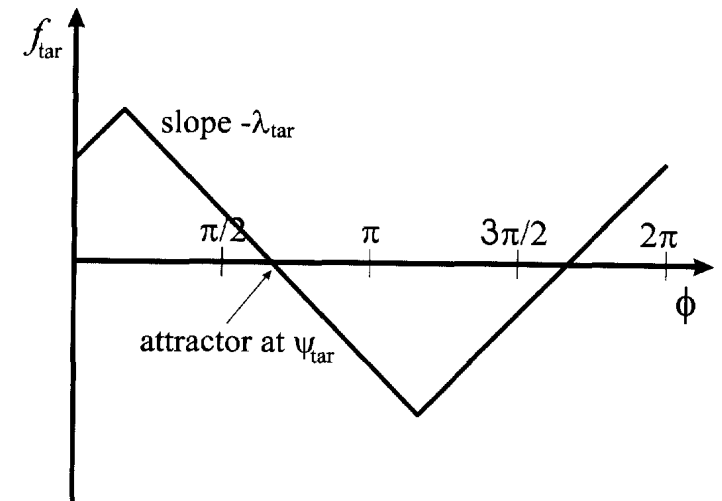


# => Bicho, Mallet, Schöner (2000)

- this is how target acquisition is integrated into obstacle avoidance on the robot

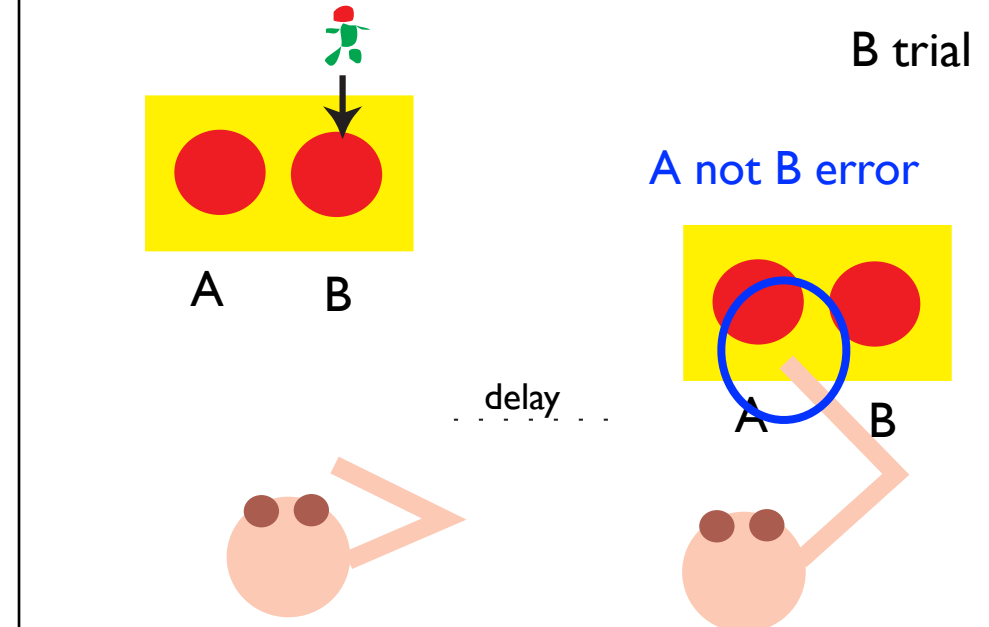
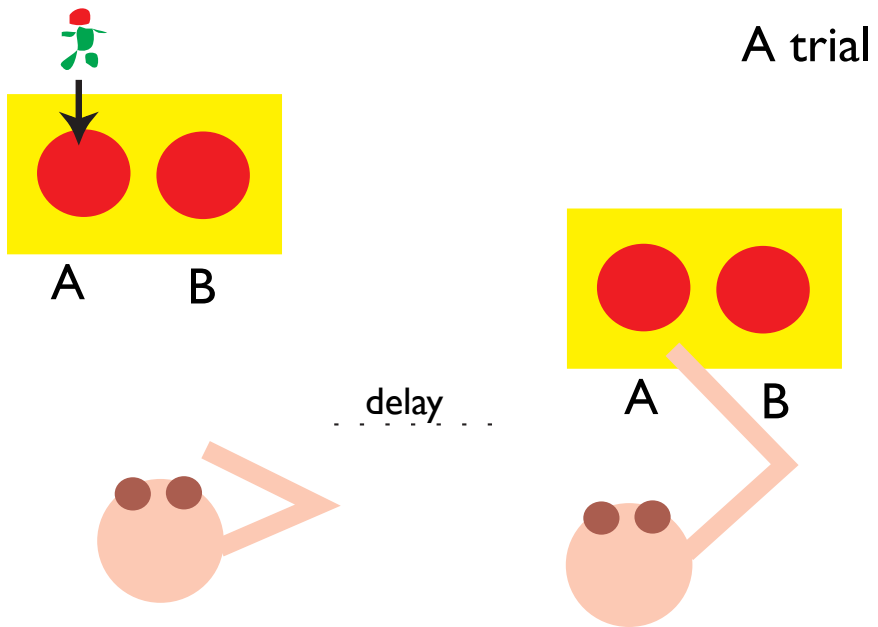
$$\frac{d\phi}{dt} = \sum_{i=1}^7 f_{\text{obs},i} + f_{\text{tar}}$$

$$\psi_{\text{tar}} = \int_0^{2\pi} \psi H(u(\psi)) d\psi / N_u$$



$$f_{\text{tar}} = \begin{cases} -\lambda'_{\text{tar}}(N_u\phi - \int_0^{2\pi} (H(u(\psi))\psi) d\psi) \\ \text{for } \psi_{\text{tar}} - \pi/2 < \phi \leq \psi_{\text{tar}} + \pi/2 \\ \lambda'_{\text{tar}}(N_u(\phi - \pi) - \int_0^{2\pi} (H(u(\psi))\psi) d\psi) \\ \text{for } \psi_{\text{tar}} + \pi/2 < \phi \leq \psi_{\text{tar}} + 3\pi/2 \end{cases}$$

# Piaget's A not B paradigm: "out-of-sight -- out of mind"

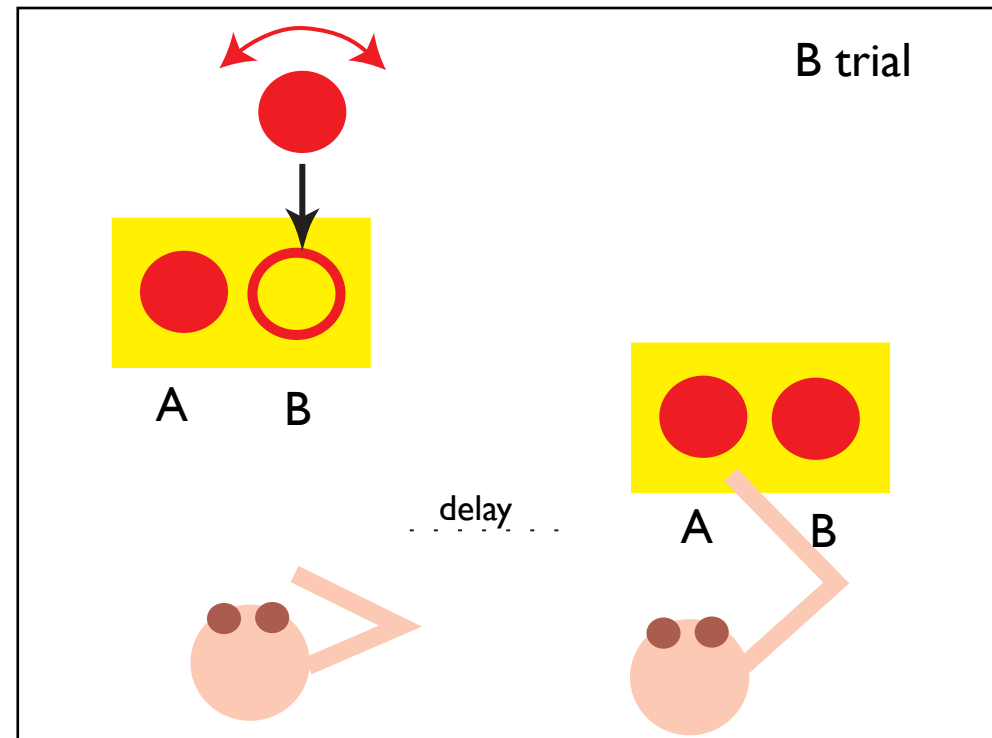
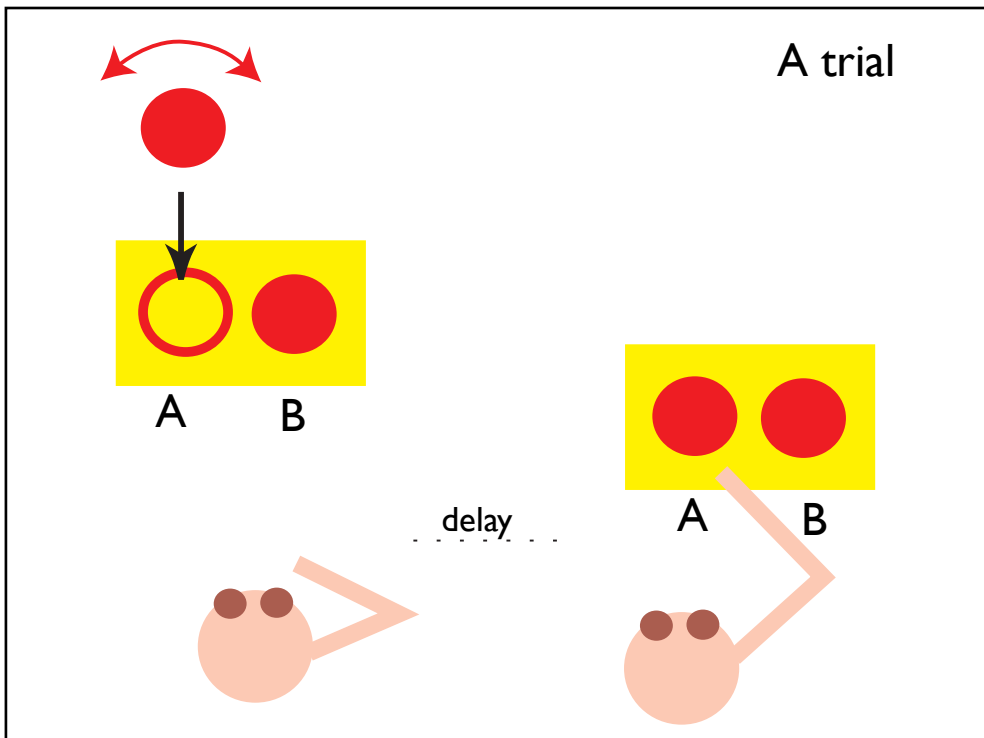


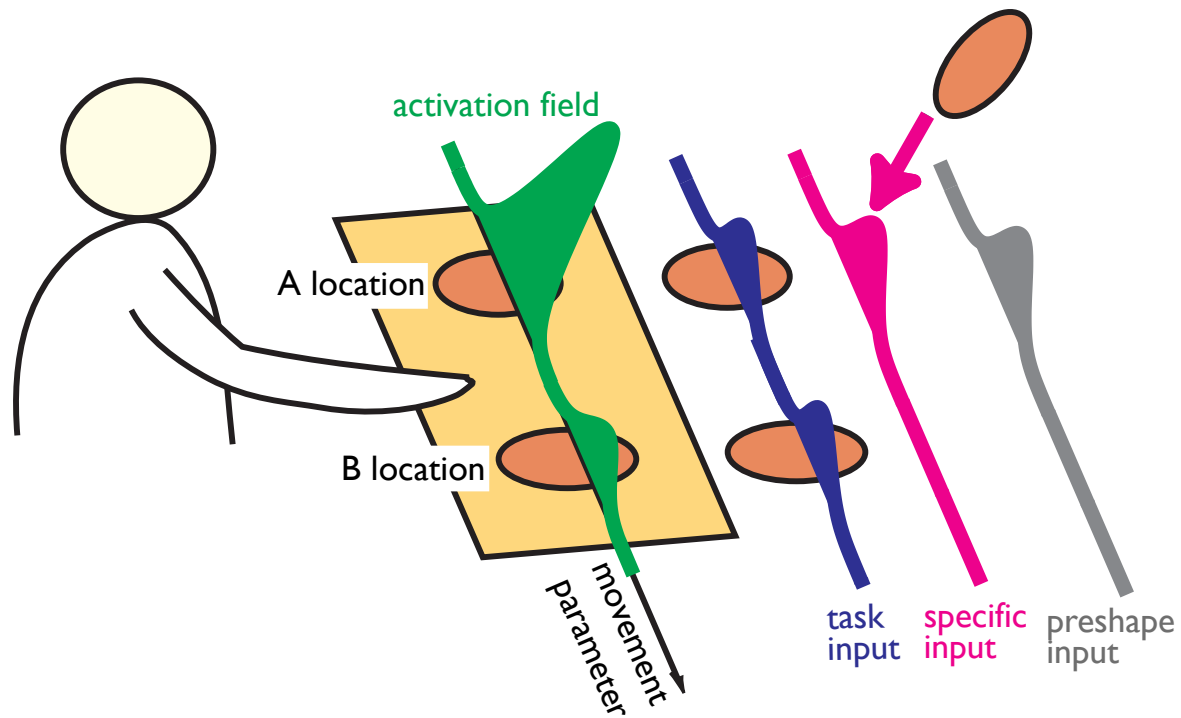
# Toyleless variant of A not B task



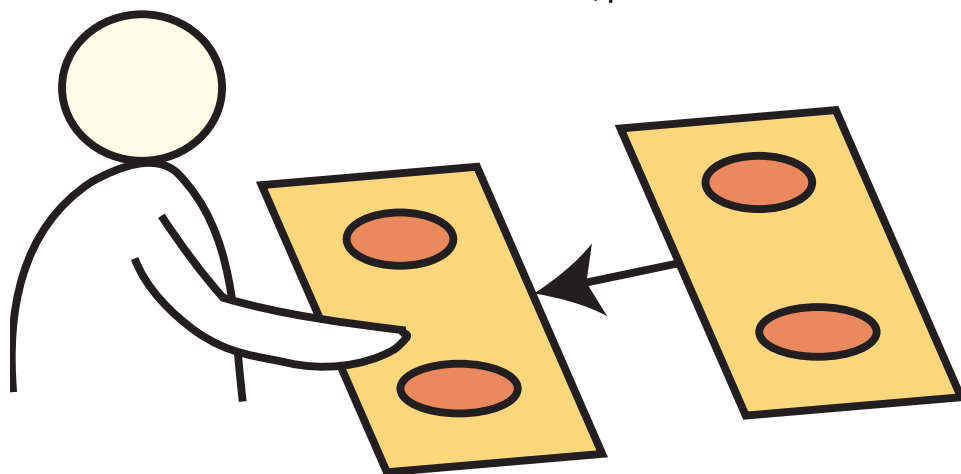
[Smith, Thelen et al.: Psychological Review (1999)]

# Toyleless variant of A not B task reveals that A not B is essentially a decision task!





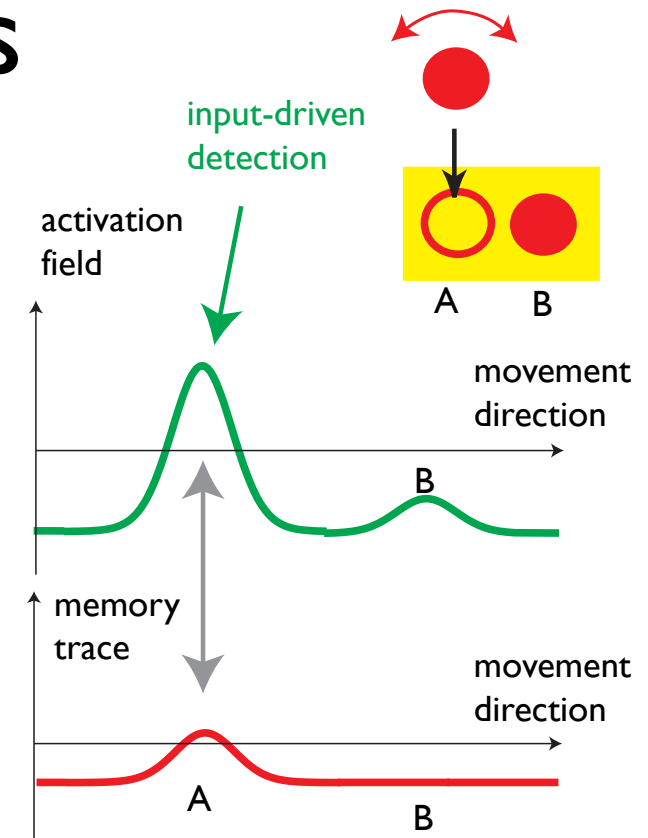
[Thelen, et al., BBS (2001)]



[Dinveva, Schöner, Dev. Science 2007]

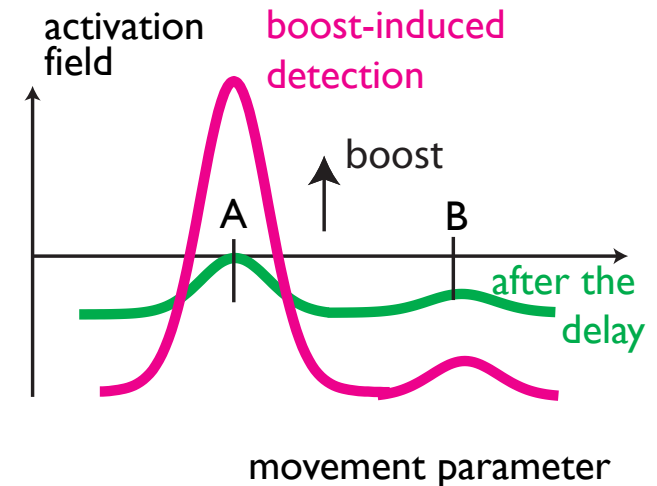
# Instabilities

- detection: forming and initiating a movement goal
- selection: making sensori-motor decisions
- (learning: memory trace)
- boost-driven detection: initiating the action
- memory instability: old infants sustain during the delay, young



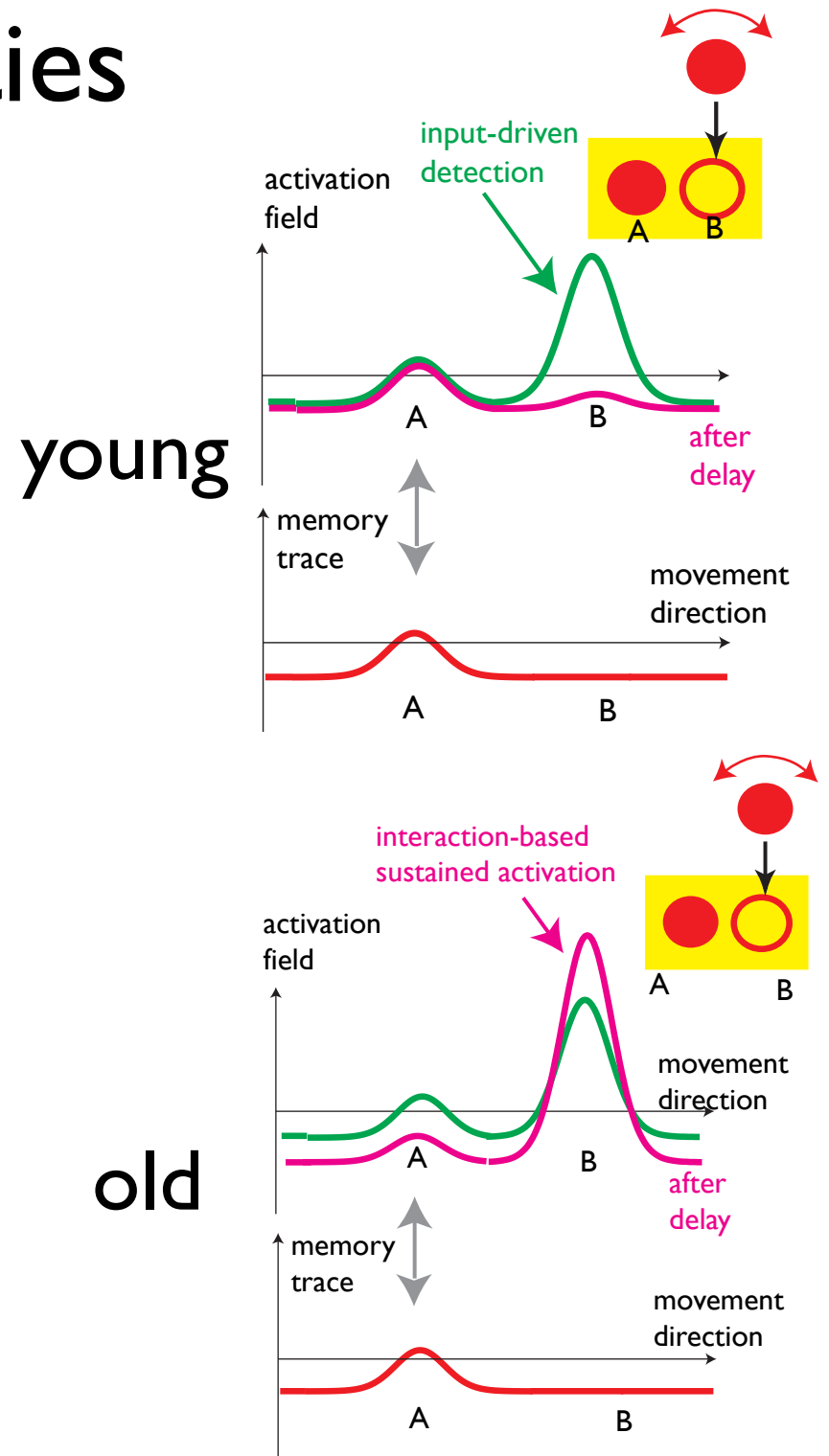
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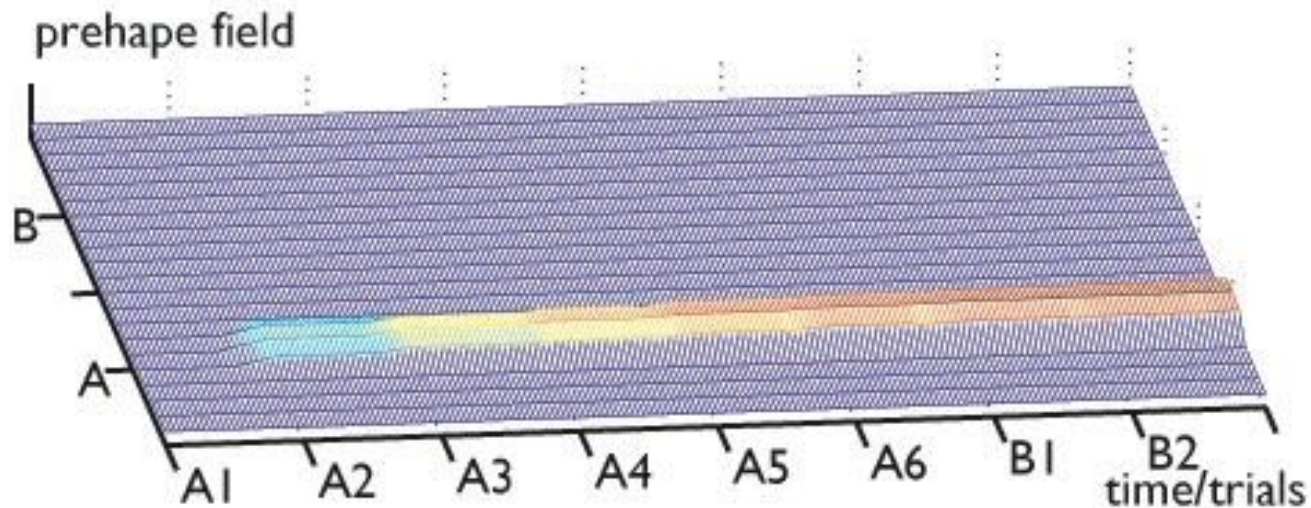
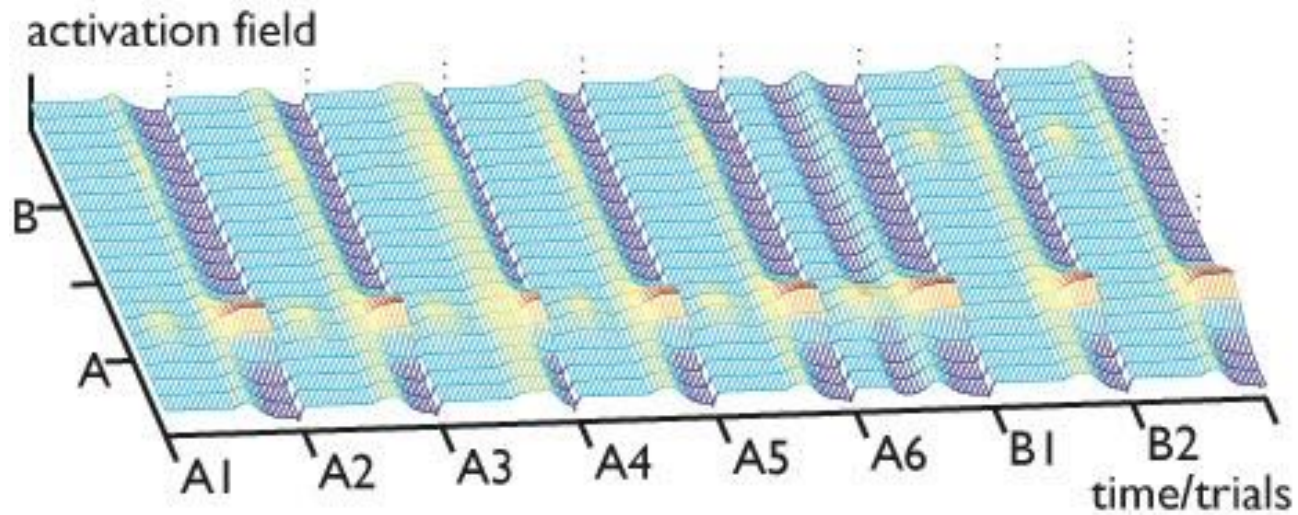
# Instabilities

- detection: forming and initiating a movement goal
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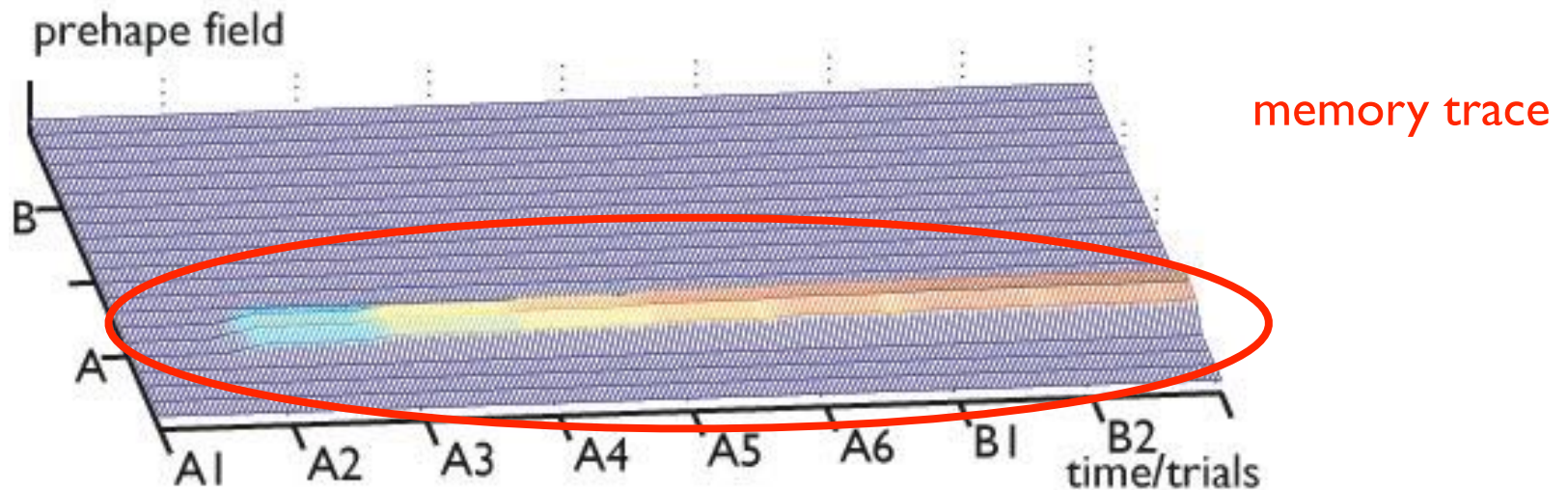
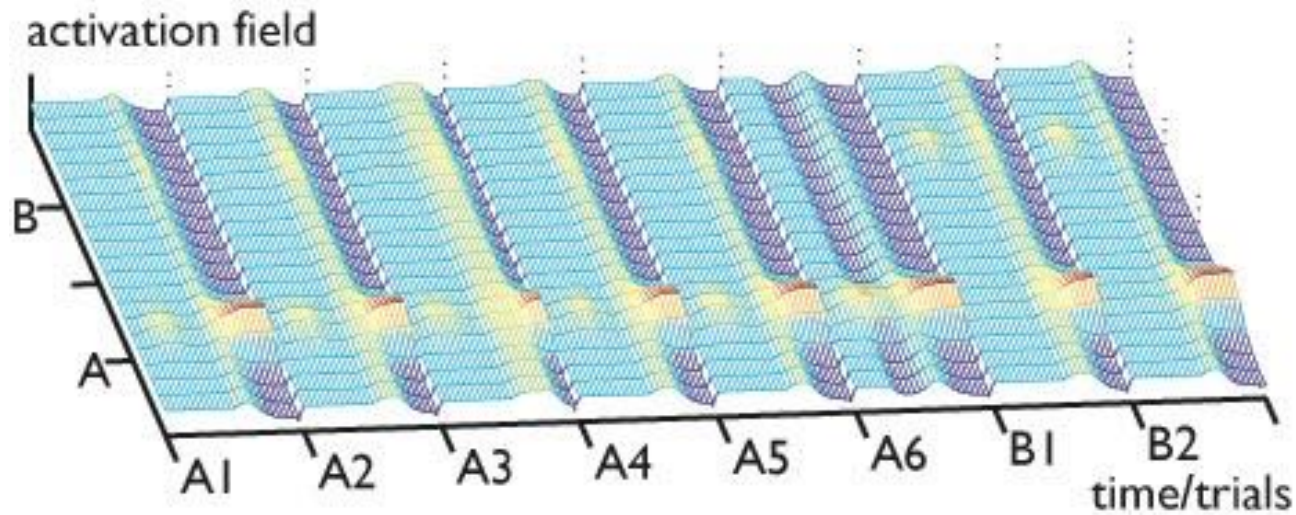




# DFT of infant perseverative reaching

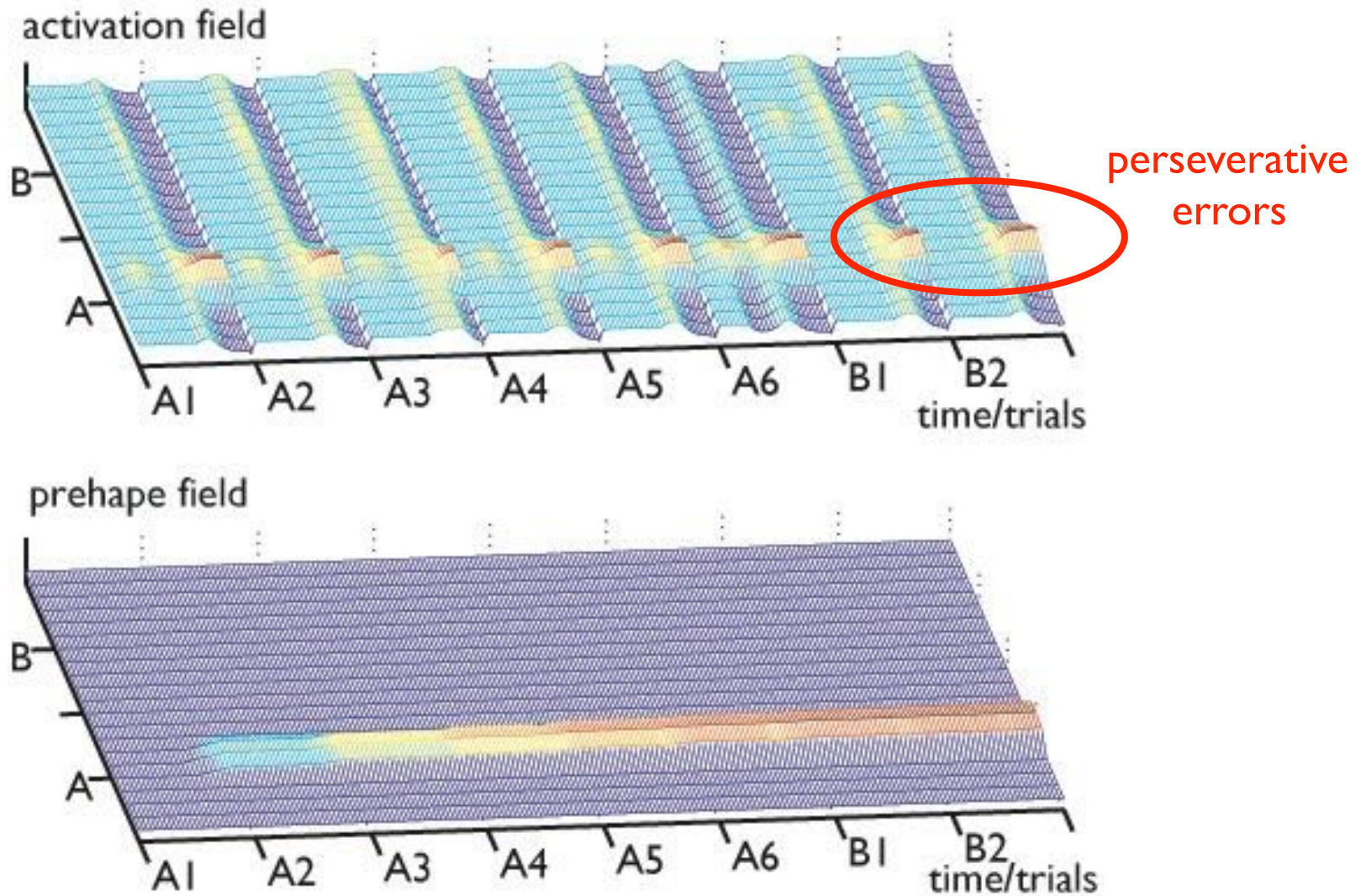


# DFT of infant perseverative reaching





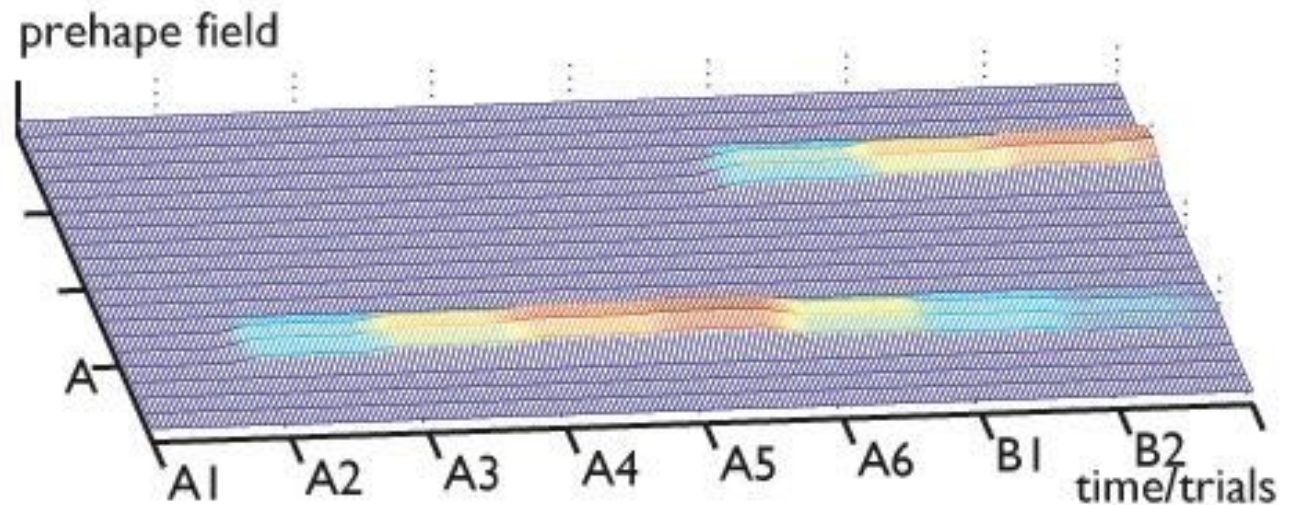
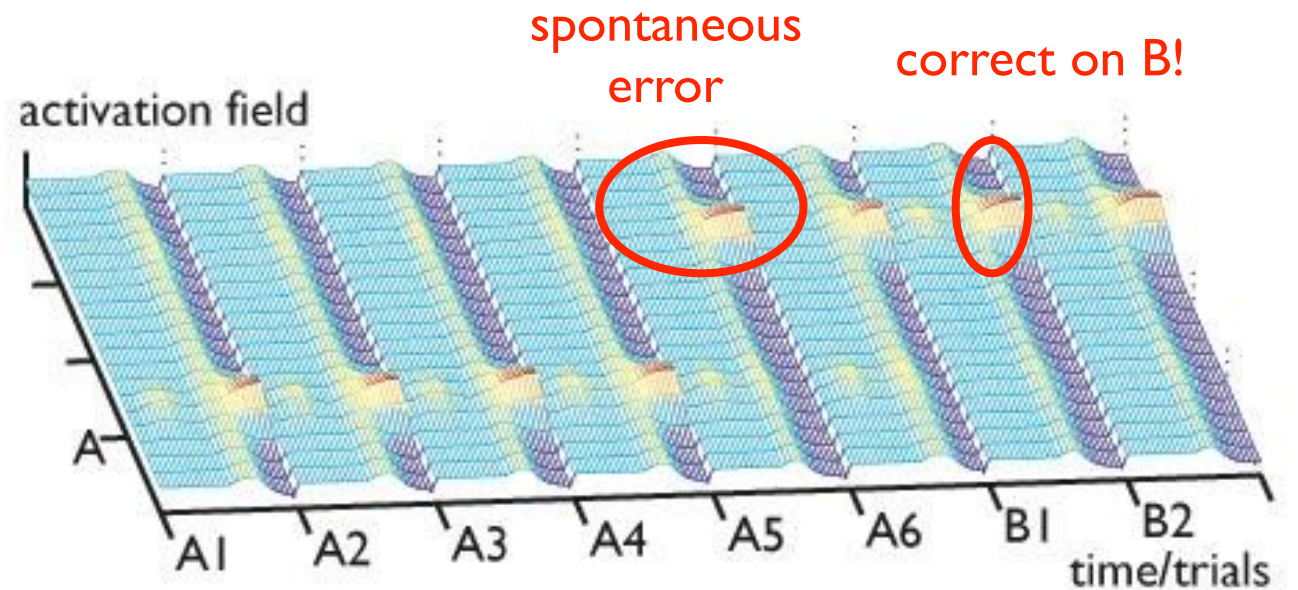
# DFT of infant perseverative reaching



# DFT of infant perseverative reaching

■ in spontaneous errors, activation arises at B on an A trial

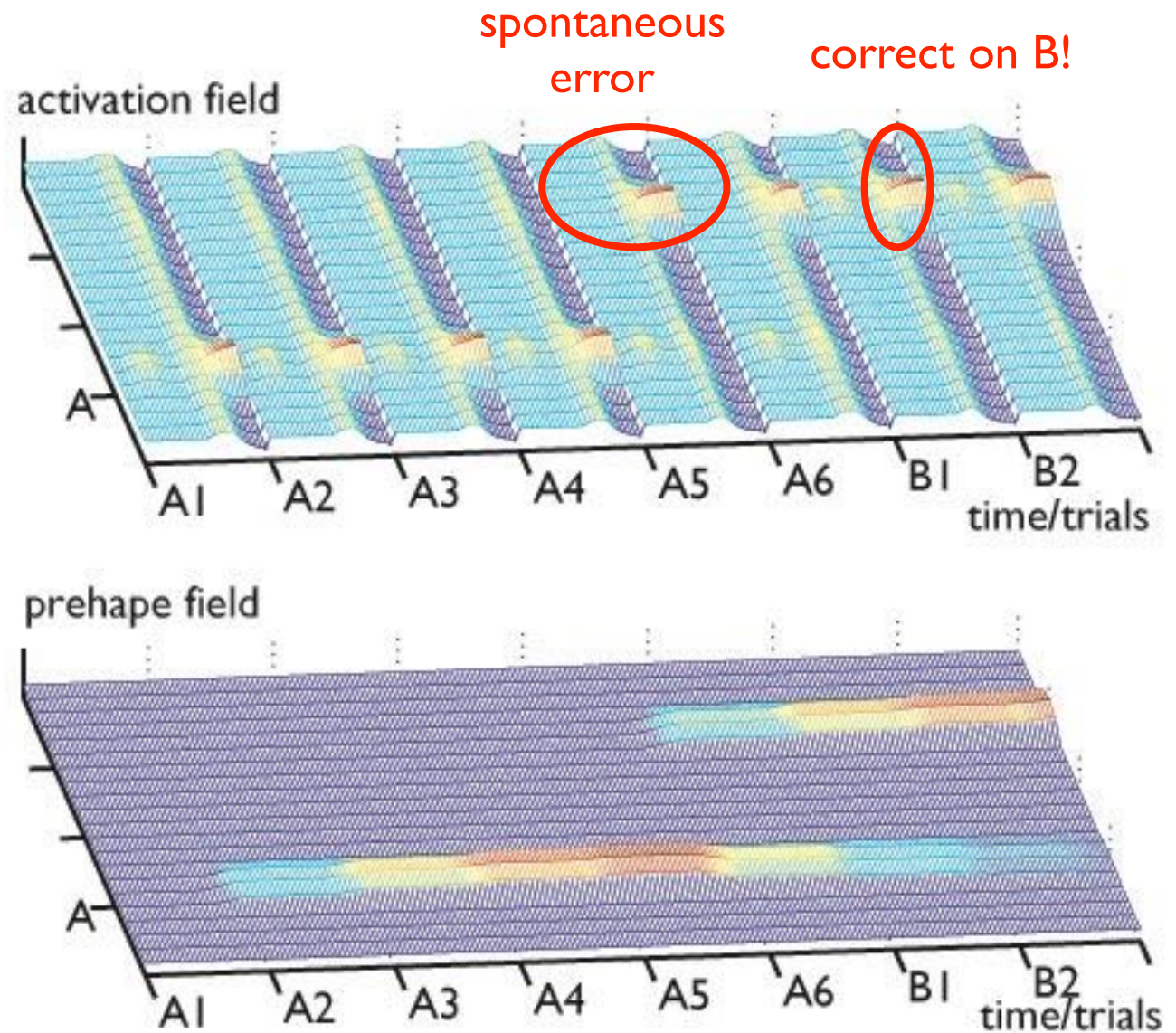
■ which leads to correct reaching on B trial





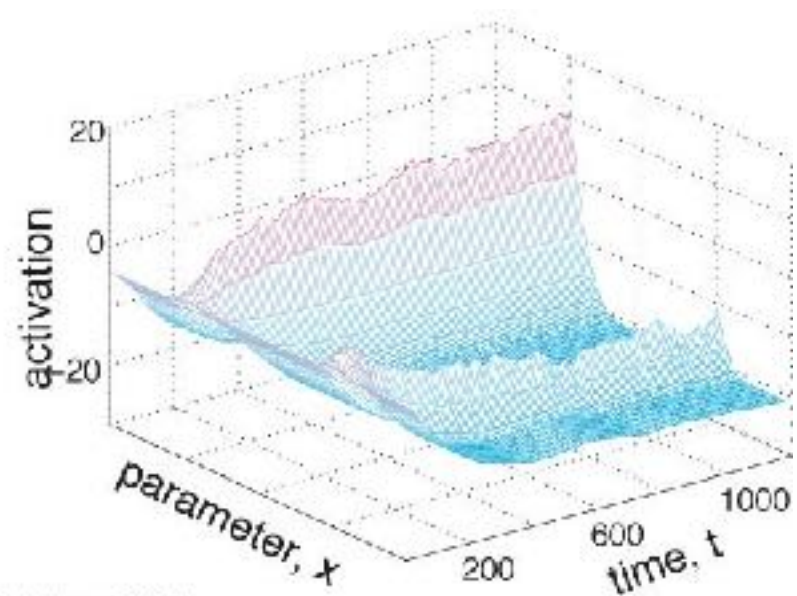
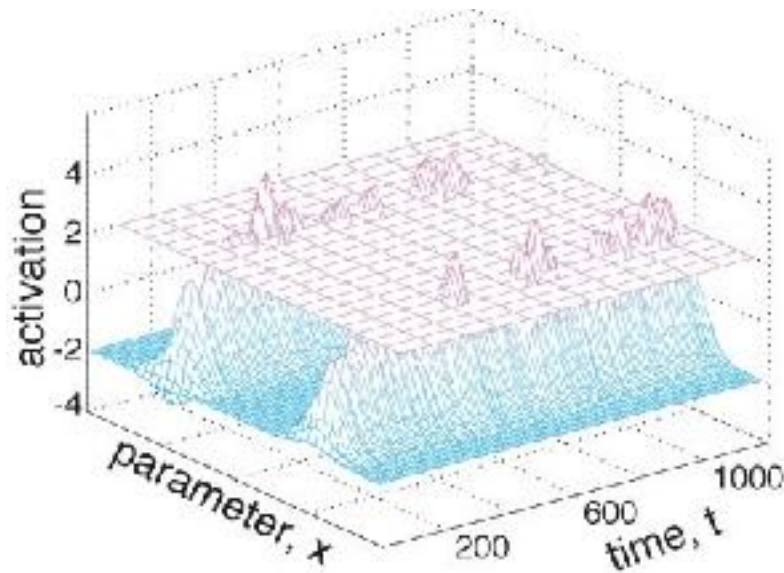
# DFT of infant perseverative reaching

- that is because reaches to B on A trials leave memory trace at B



# DFT is a neural process model

- that makes the decisions in each individual trial, by amplifying small differences into a macroscopic stable state
- and that's how decisions leave traces, have consequences

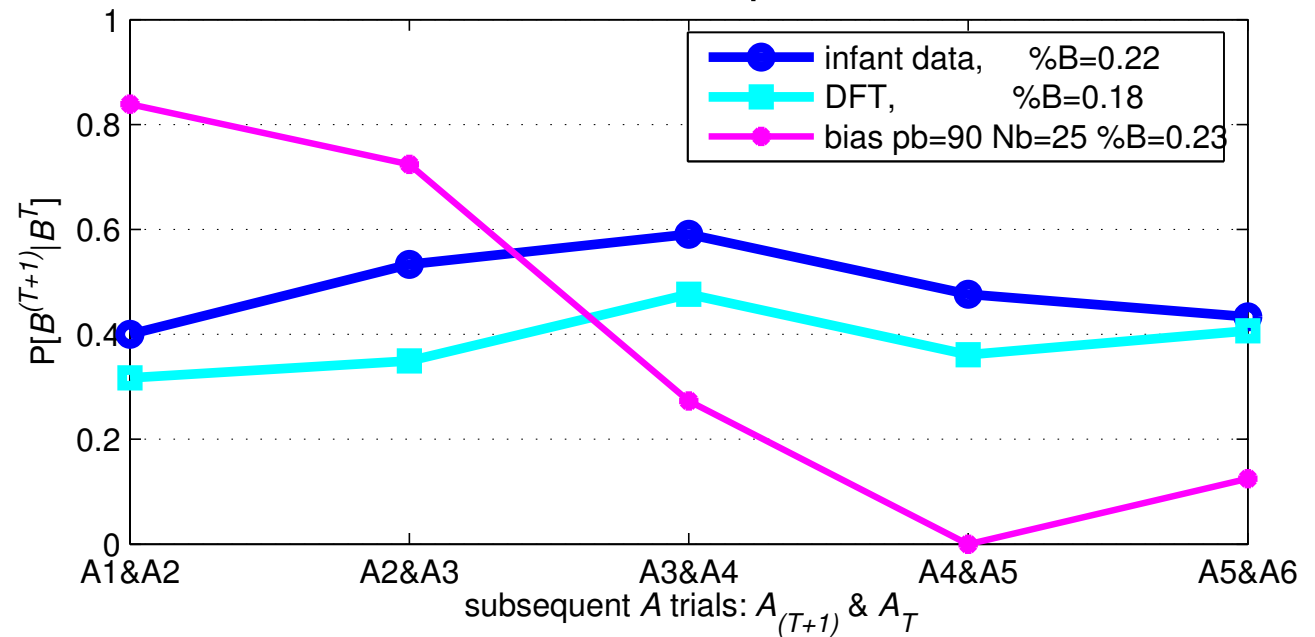


[Wilmzig, Schöner, 2006]

# DFT of infant perseverative reaching

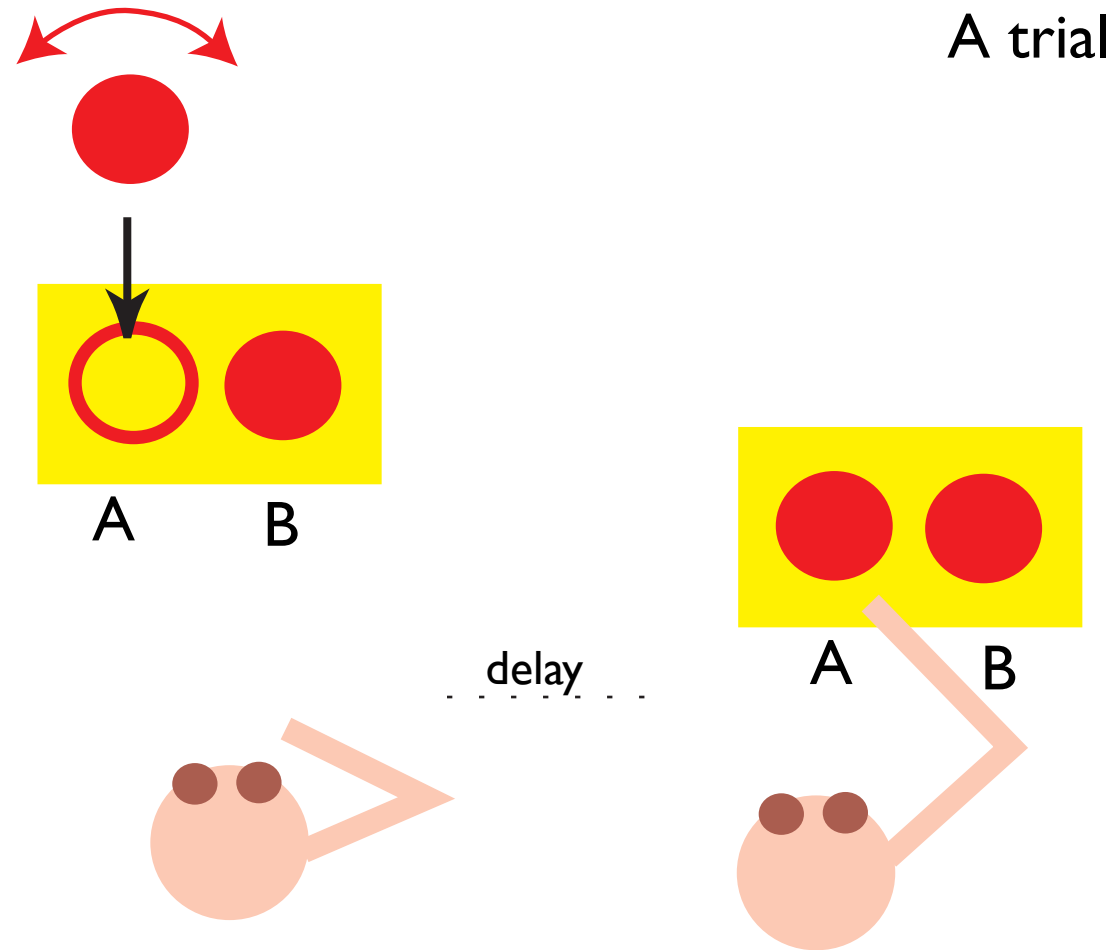
■ spontaneous errors promote spontaneous errors

first and second reaches to  $B$  are on two subsequent  $A$  trials



# summary: instabilities

- detection: forming and initiating a movement goal
- selection: making sensori-motor decisions
- boost-driven detection: initiating the the action
- learning: memory trace
- working memory: sustaining a delay

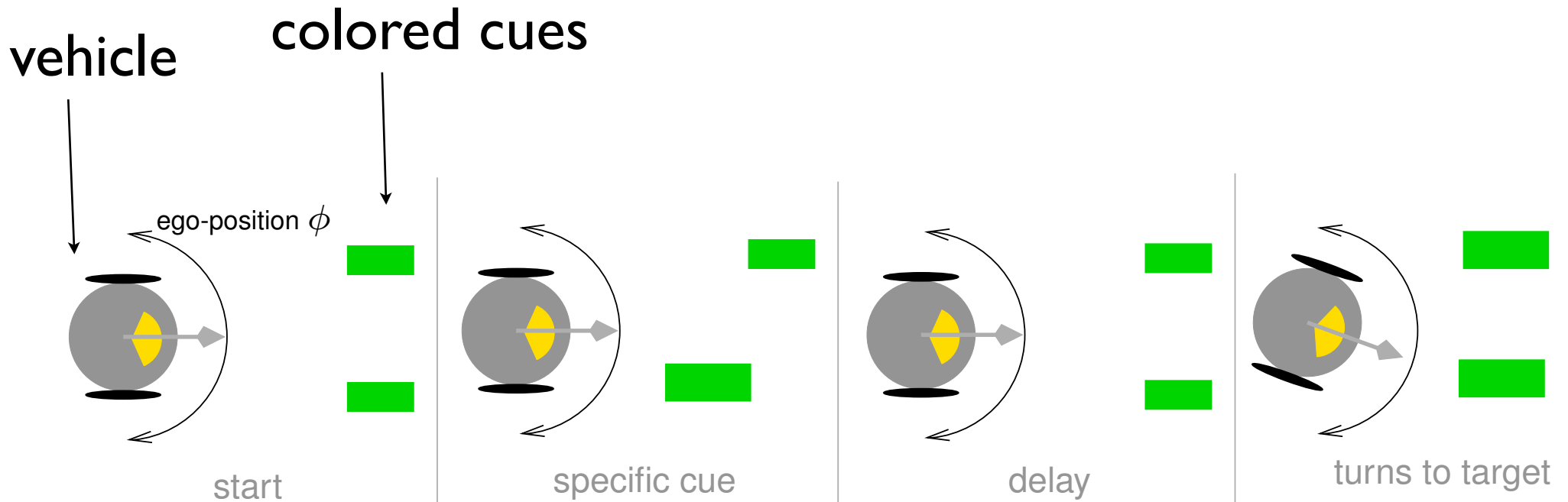


Toyless version of A not B  
(Smith, Thelen, et al., 1999)



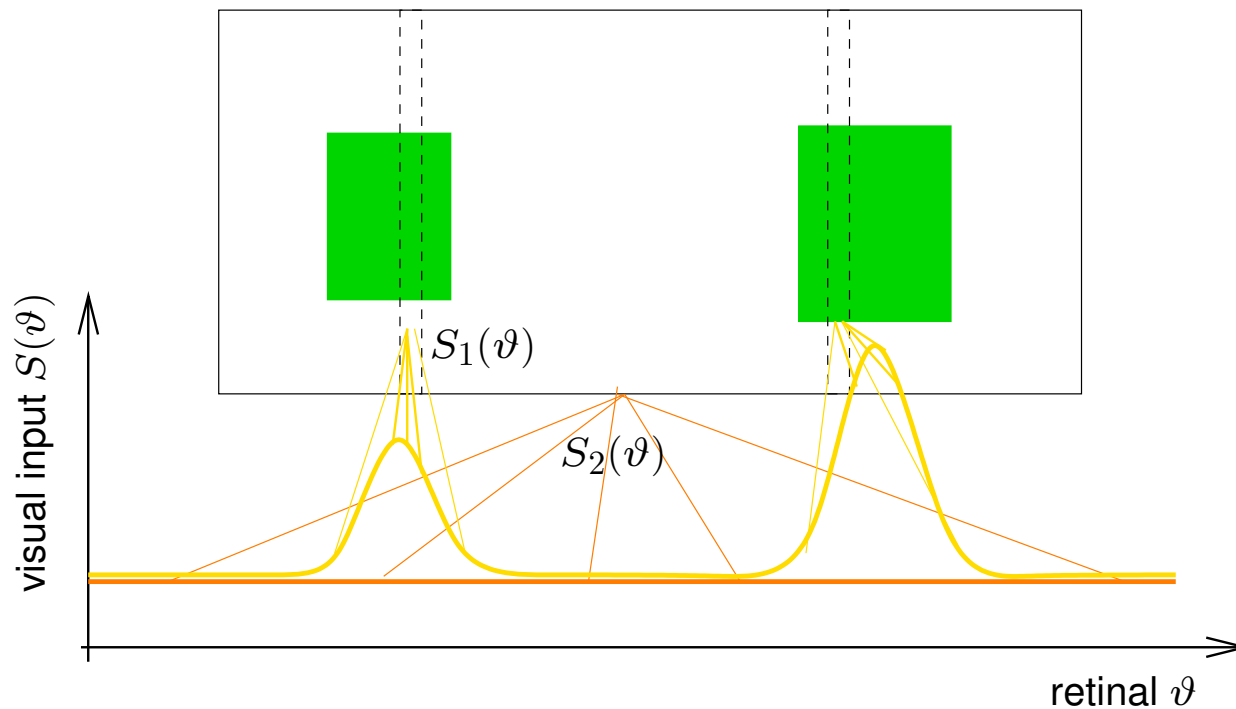
# Embodied A not B

- implementing the A not B model on a autonomous robot with continuous link to sensory and motor surfaces...



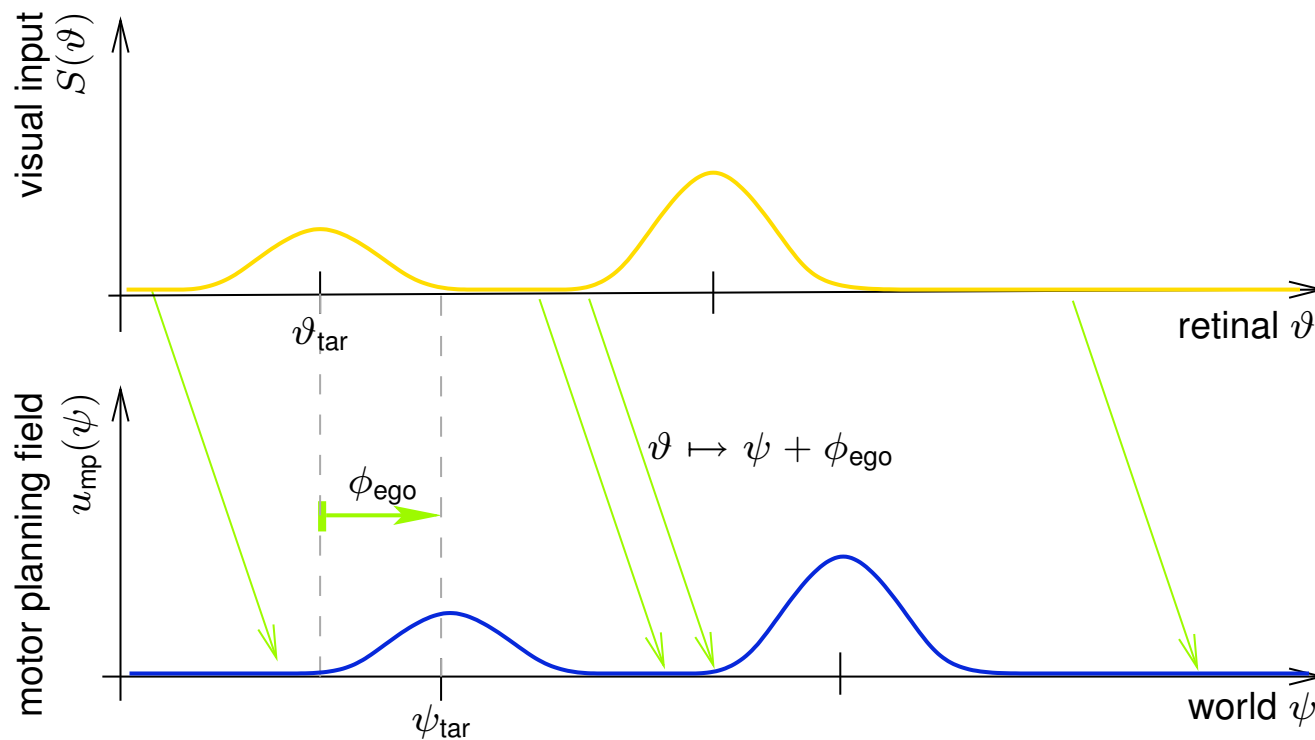
# Visual input

- color-based segmentation
- summing color pixels within color slot along the vertical
- spatially filter at two resolutions



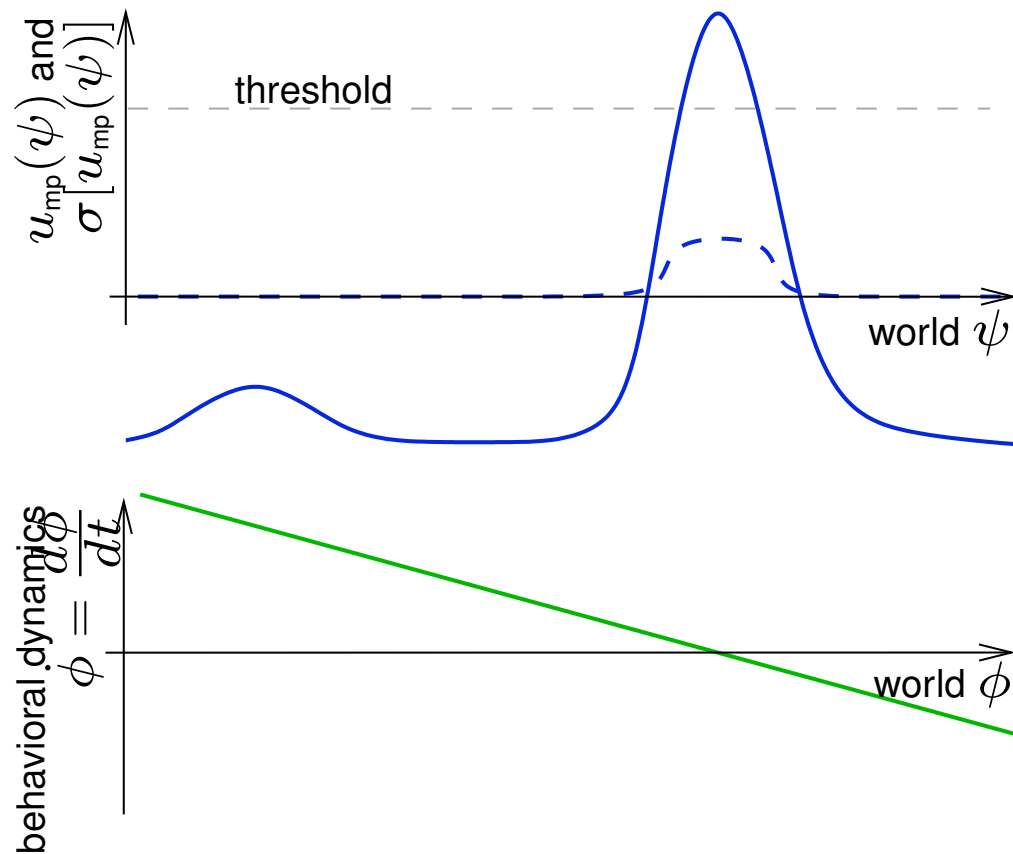
# Dynamic field

- defined over direction in the world
- (requires coordinate transform from retina based on dead-reckoning)



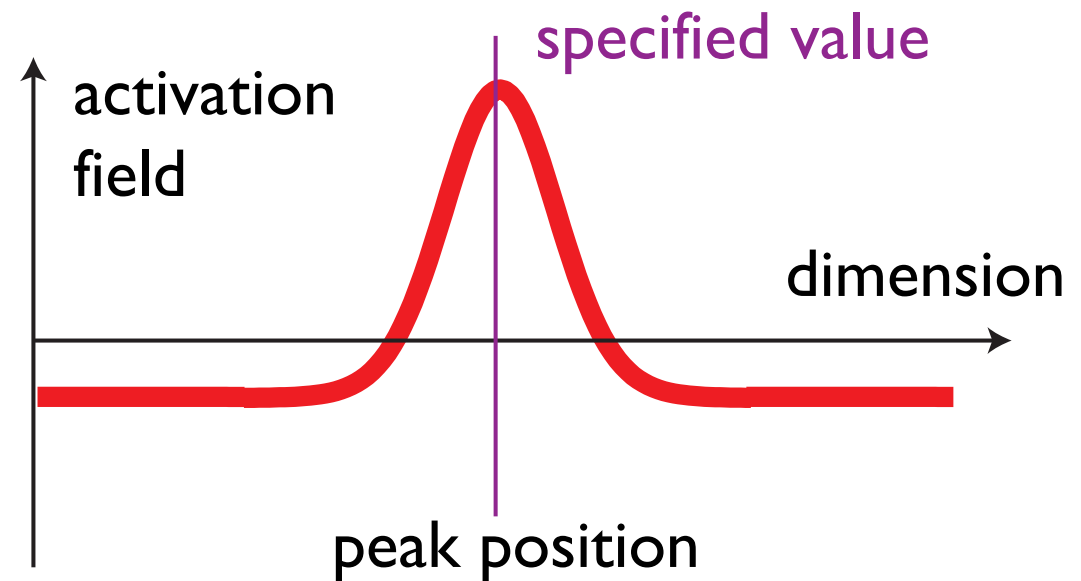
# Motor dynamics

- couple peak in direction field into dynamics of heading direction as an attractor



# “Read-out” by generating attractor dynamics for motor system

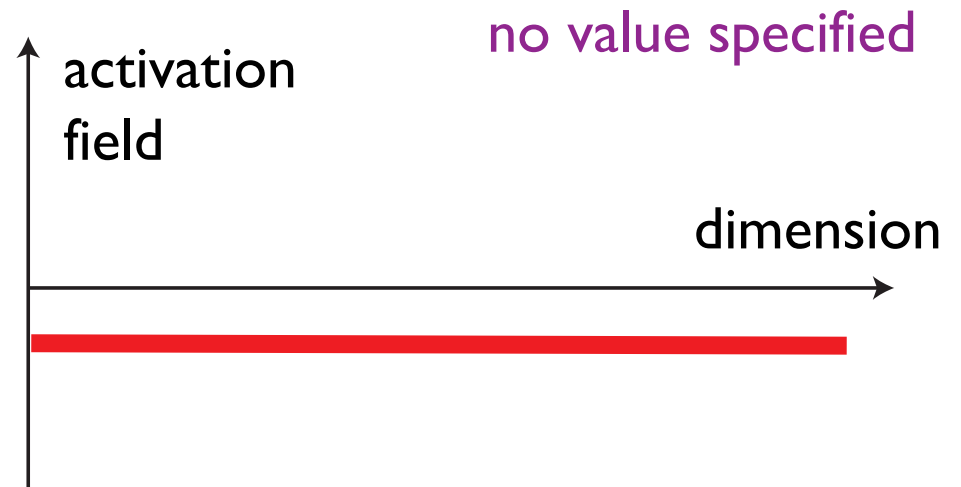
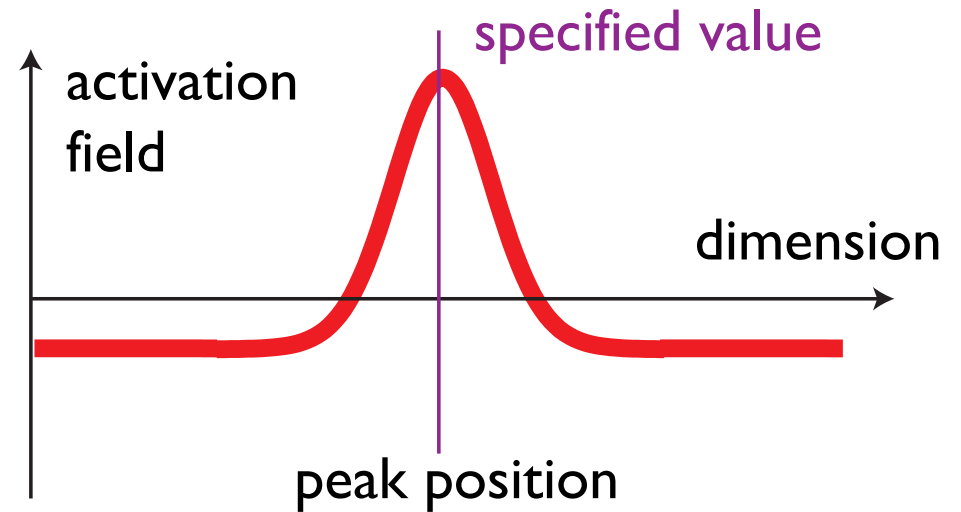
- peak specifies value for a dynamical variable that is congruent to the field dimension



■ treating sigmoided field as probability: need to normalize

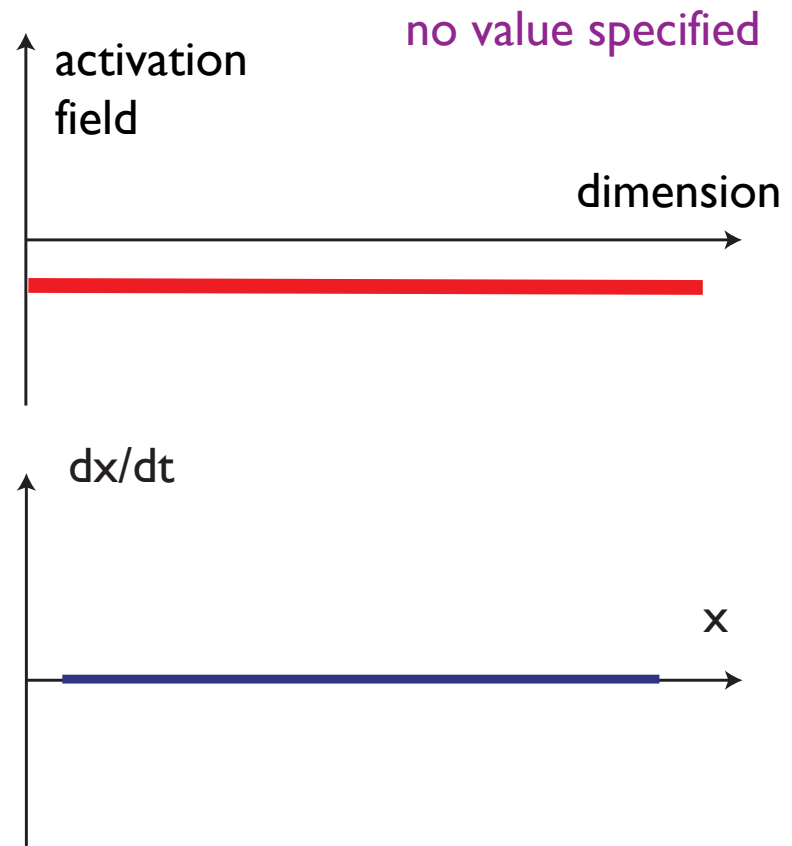
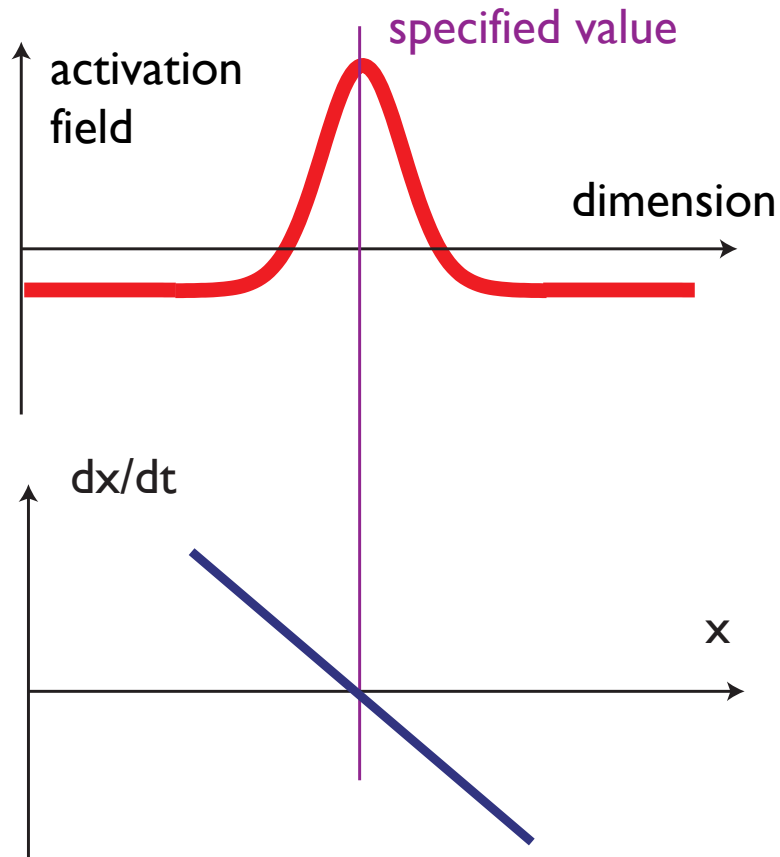
■ => problem when there is no peak: divide by zero!

$$x_{\text{peak}} = \frac{\int dx' \sigma(u(x', t)) x'}{\int dx' \sigma(u(x', t))}$$



# instead:

■ create attractor



## ■ solution: peak sets attractor

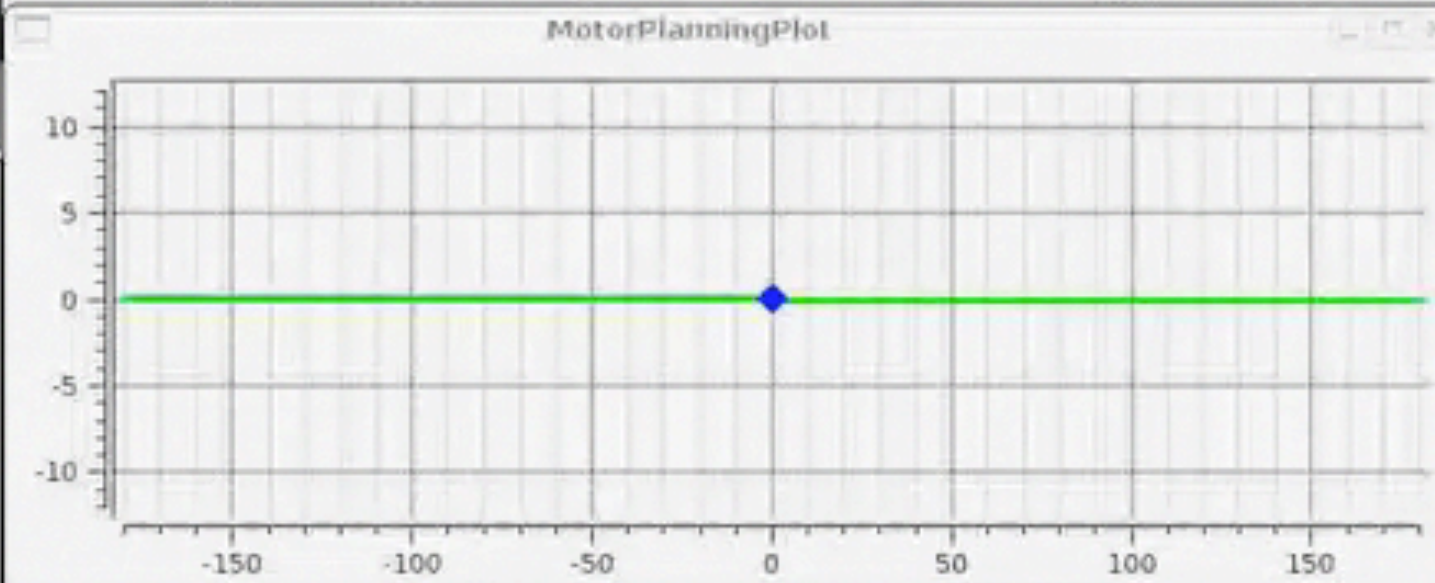
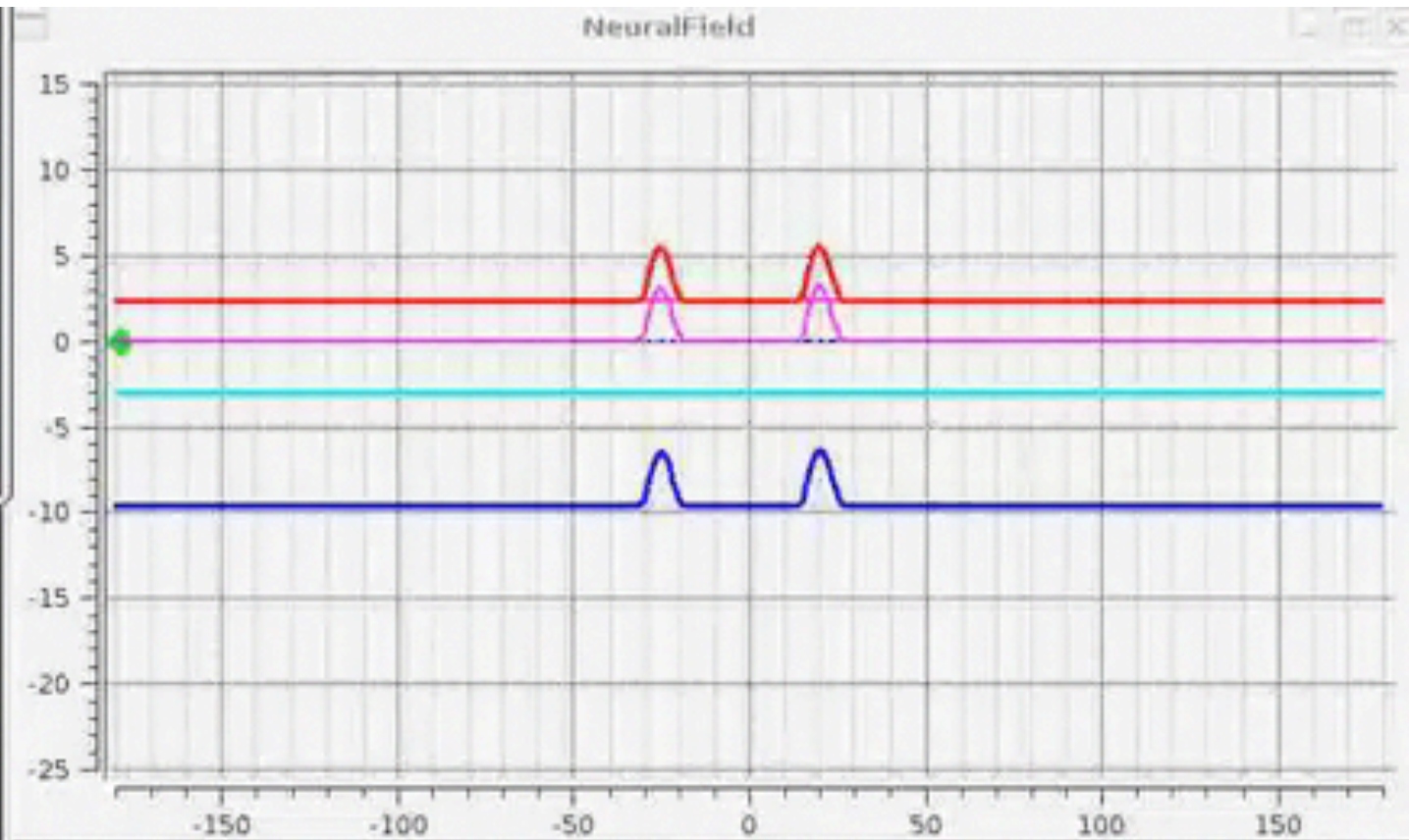
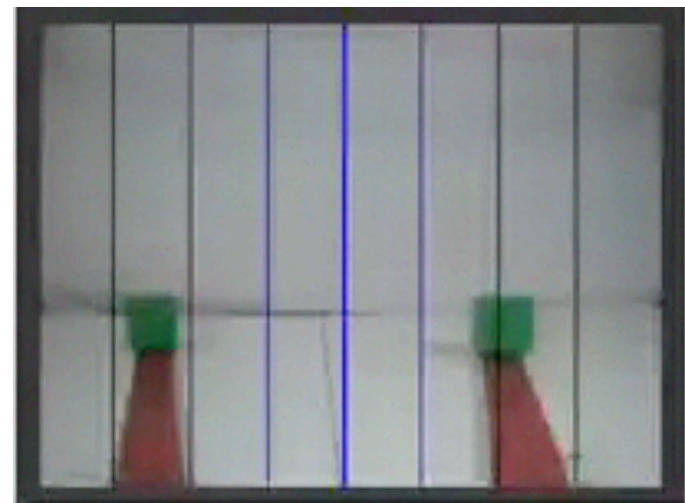
■ location of attractor: peak location

■ strength of attractor: summed supra-threshold activation

$$x_{\text{peak}} = \frac{\int dx' \sigma(u(x', t)) x'}{\int dx' \sigma(u(x', t))}$$

$$\begin{aligned} \dot{x} &= - \int dx' \sigma(u(x', t)) (x - x_{\text{peak}}) \\ &= - \left[ \int dx' \sigma(u(x', t)) x - \int dx' \sigma(u(x', t)) x_{\text{peak}} \right] \\ &= - \left[ \int dx' \sigma(u(x', t)) x - \int dx' \sigma(u(x', t)) x' \right] \\ &= - \int dx' \sigma(u(x', t)) (x - x') \end{aligned}$$



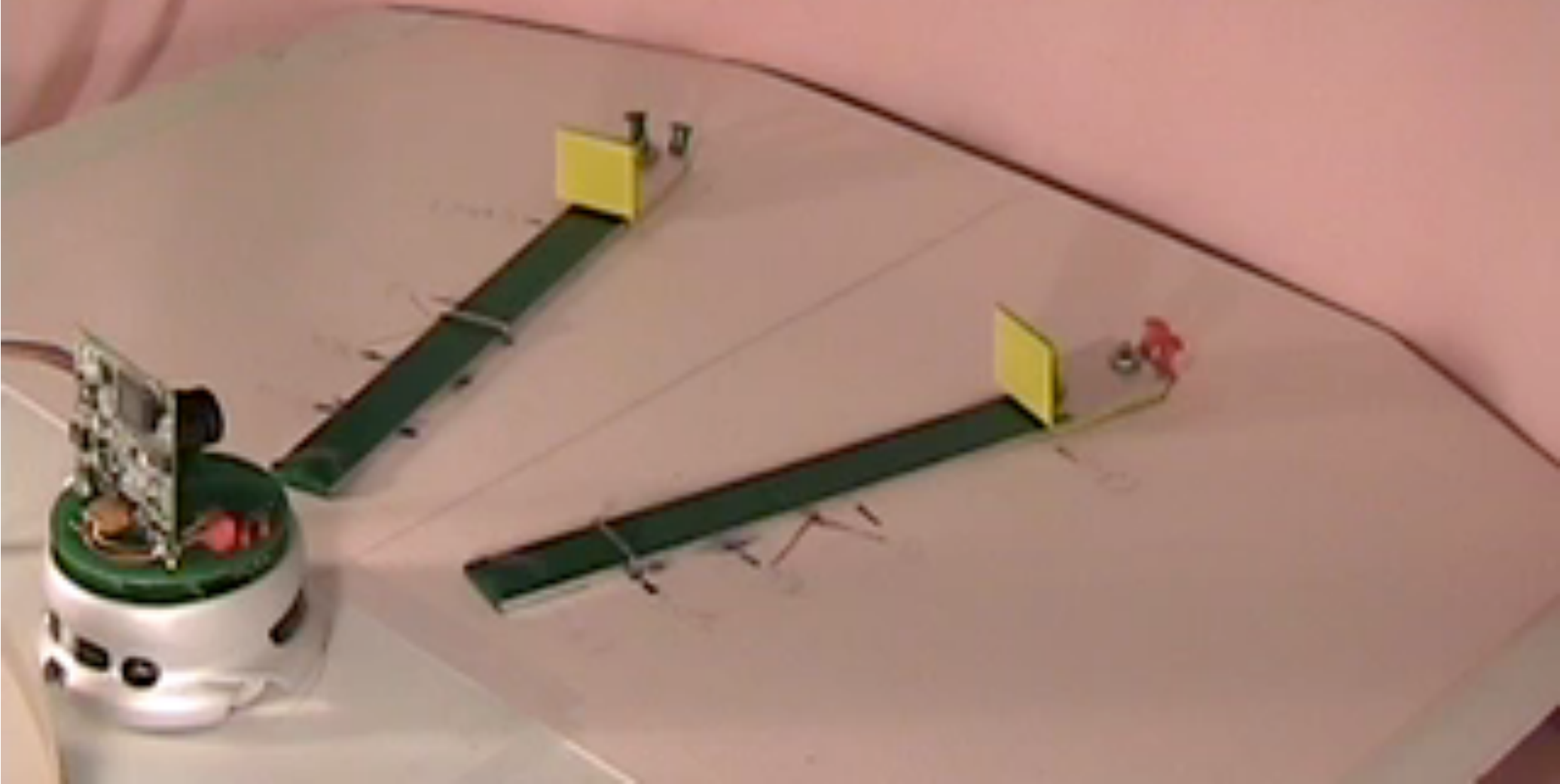


Exp #3

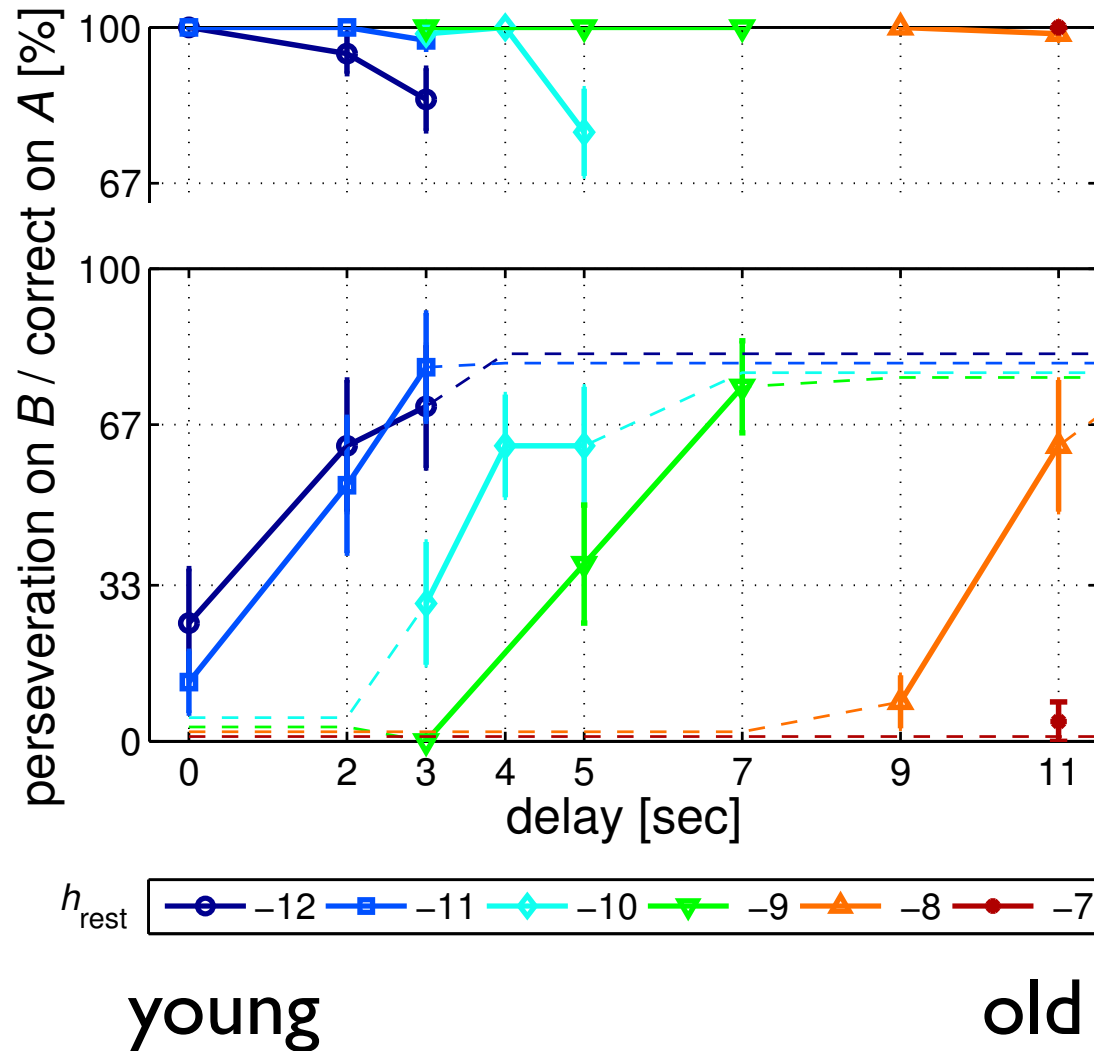
365  
h120  
-1  
PC-6

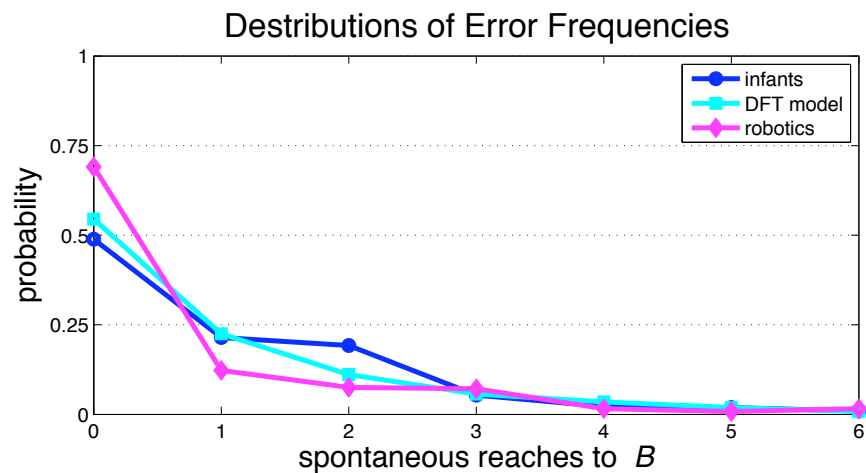
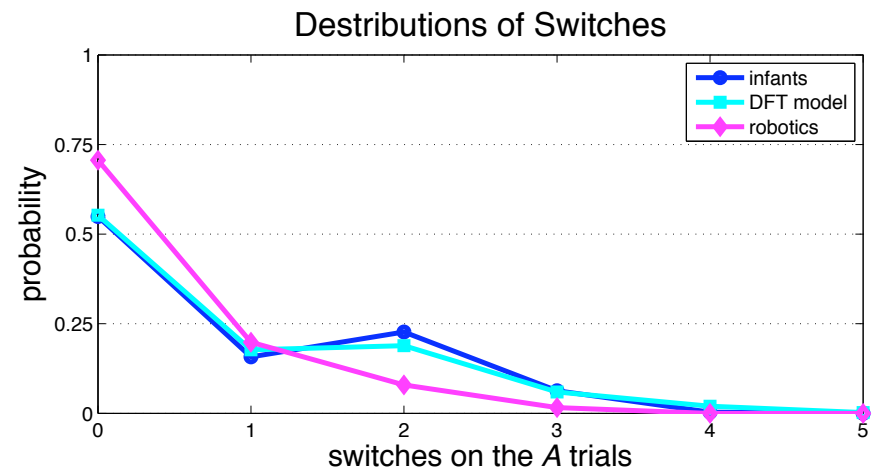
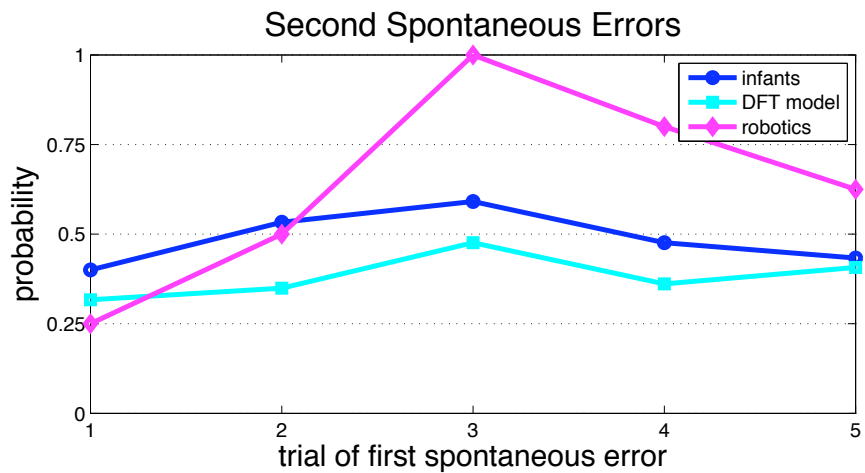
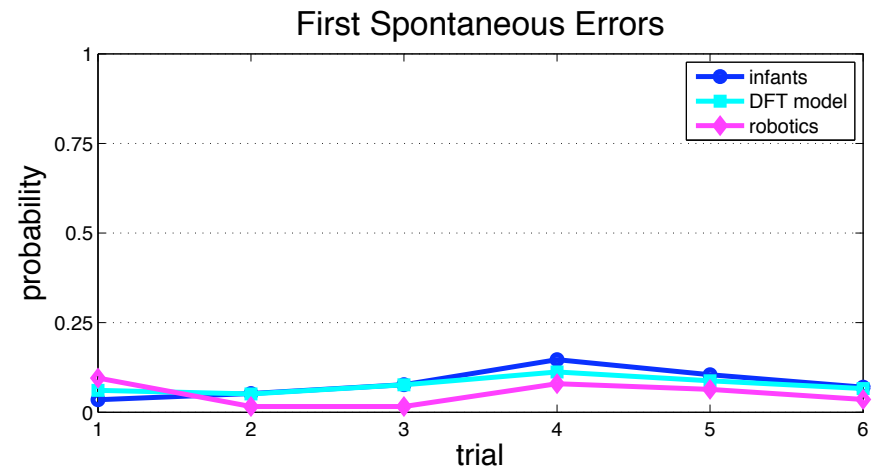
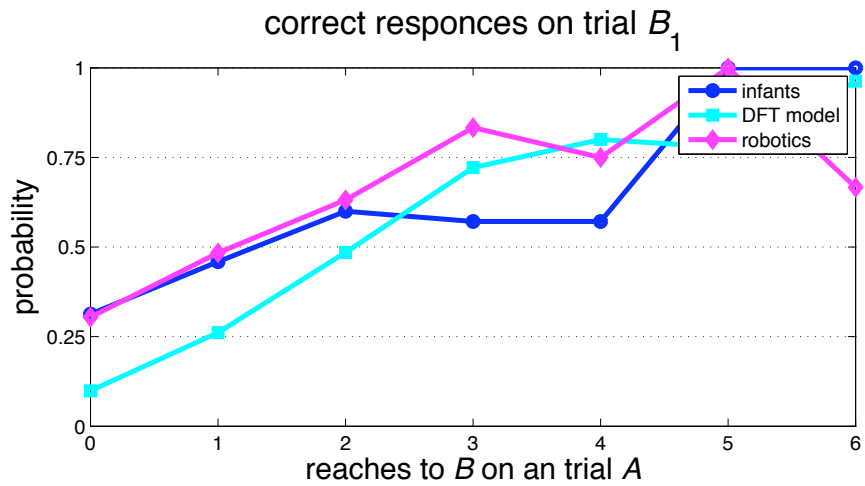
[1]

[R]



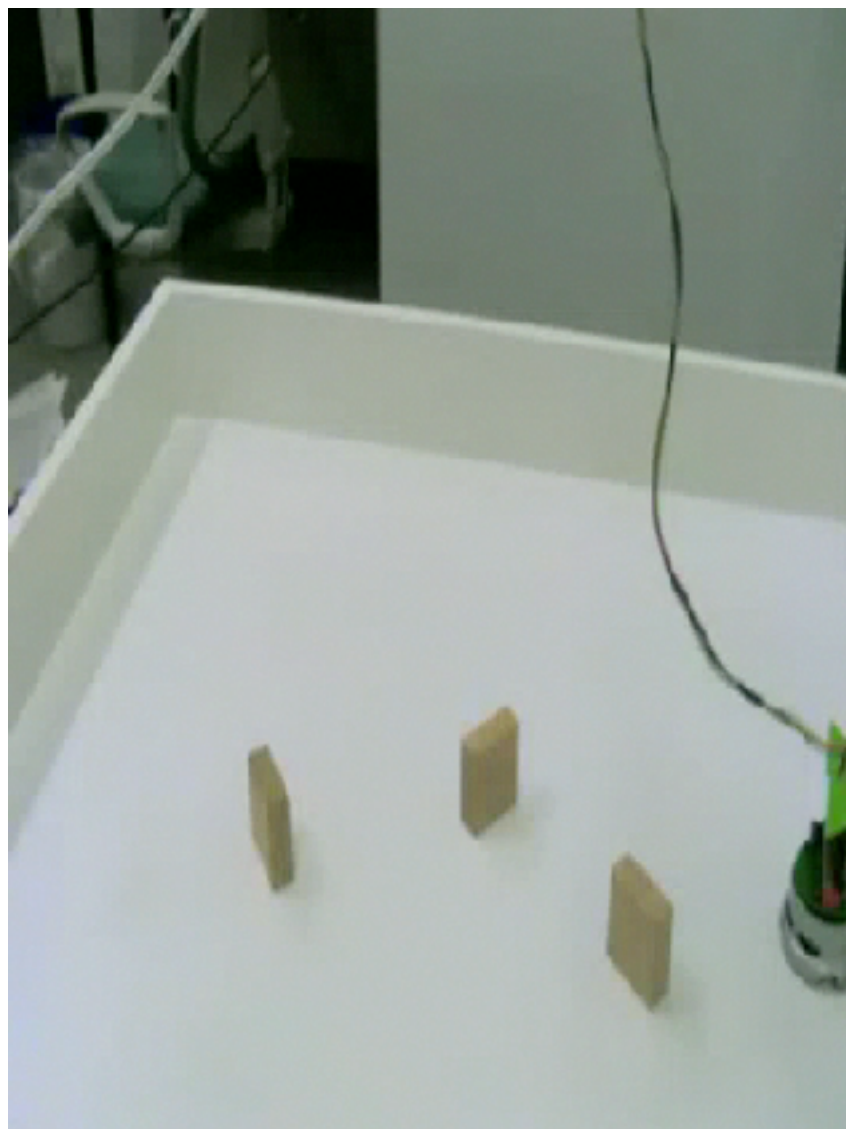
# result: reproduce fundamental age-delay trade-off in A not B



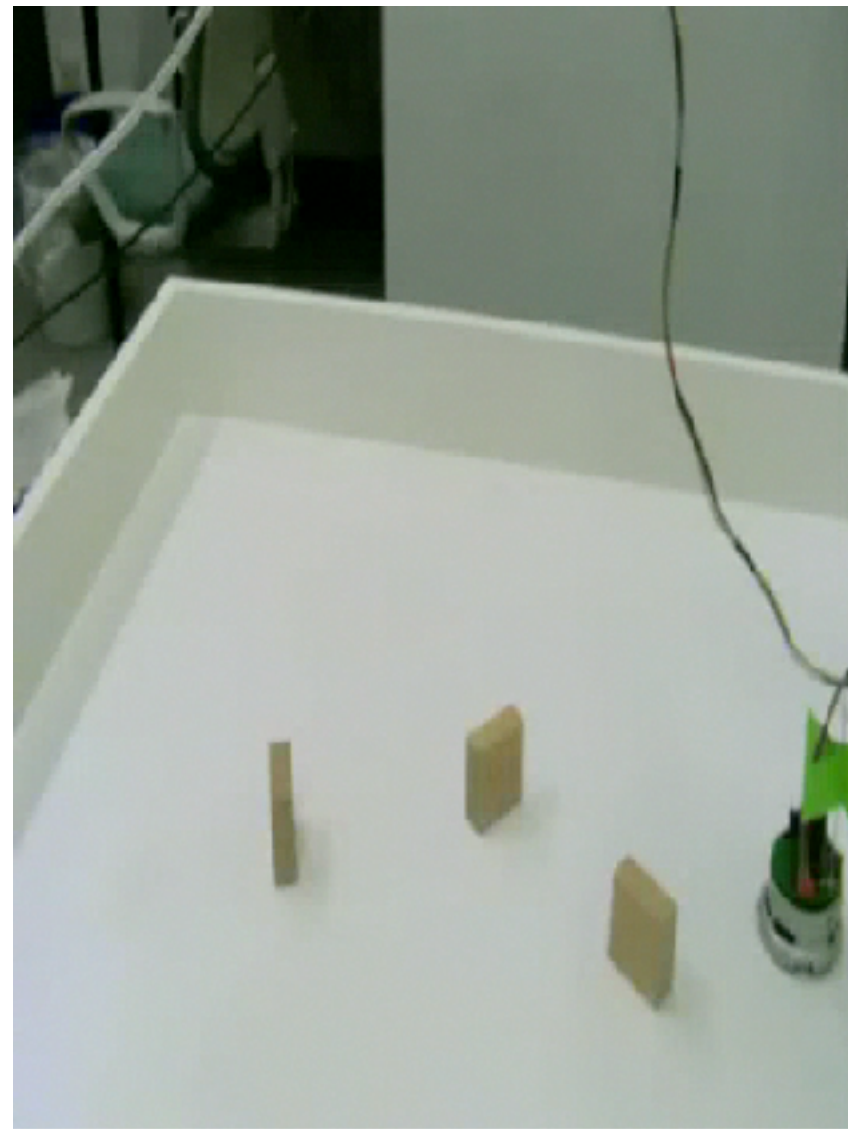




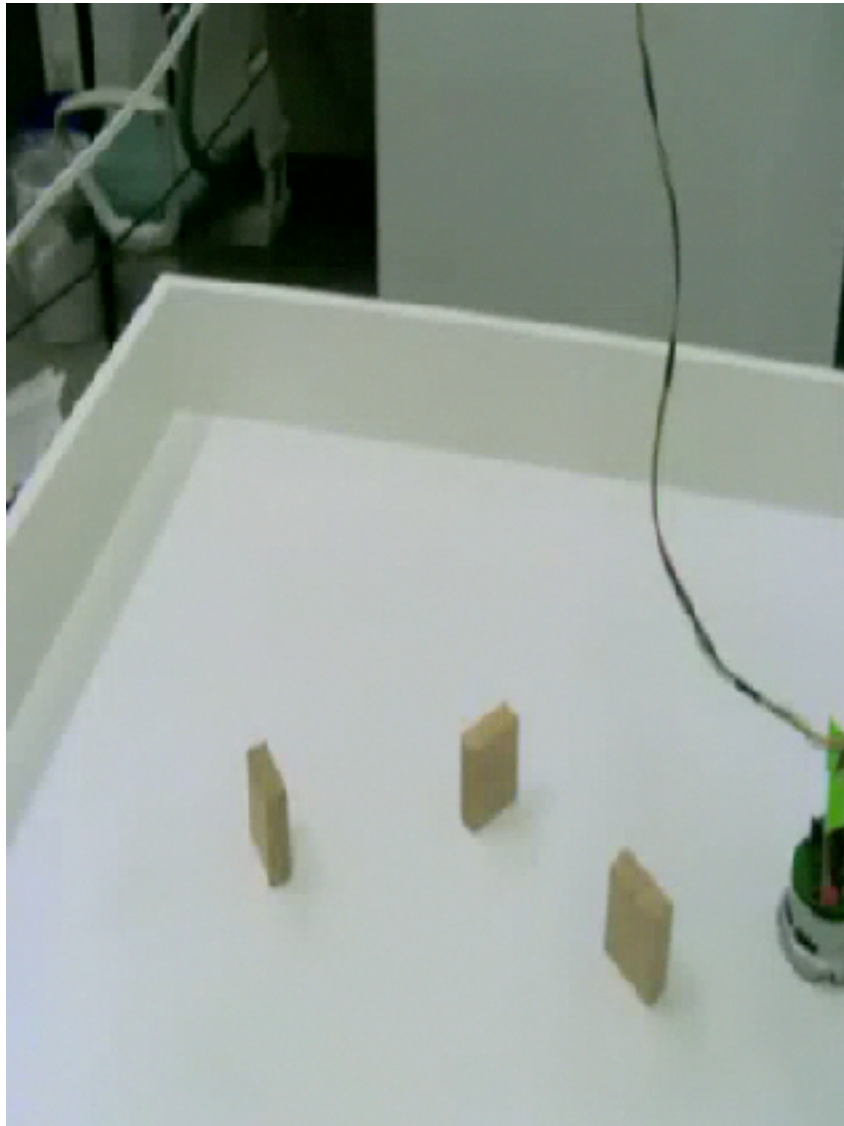
“young” robot



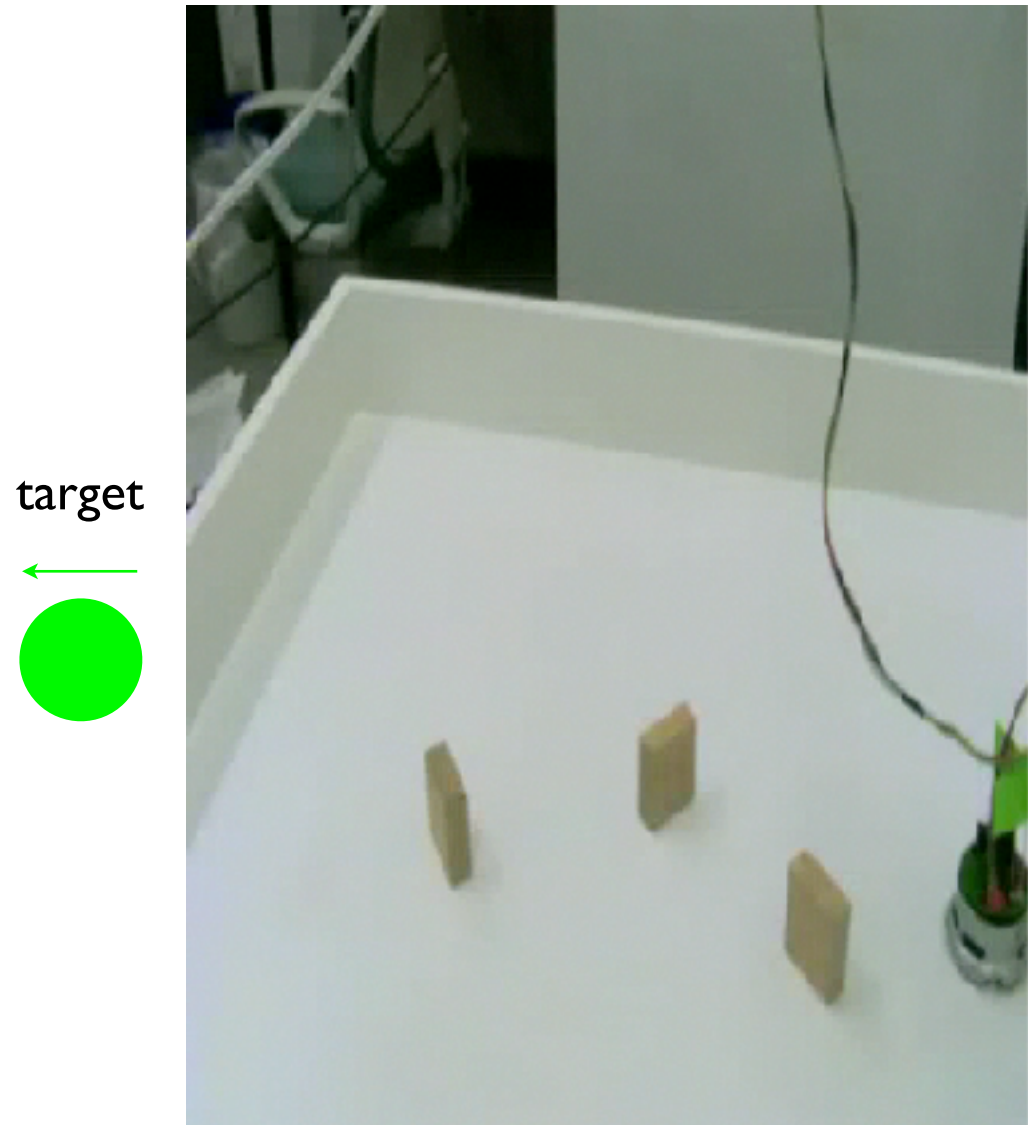
“old” robot



“young” robot



“young” robot with  
memory trace



# DFT models can be embodied

- stabilization of decisions is critical
- (when we failed to do so, by just “reading out” the location with maximal activation after the delay, that location fluctuate from moment to moment leading to meandering of the robot in an averaged direction)