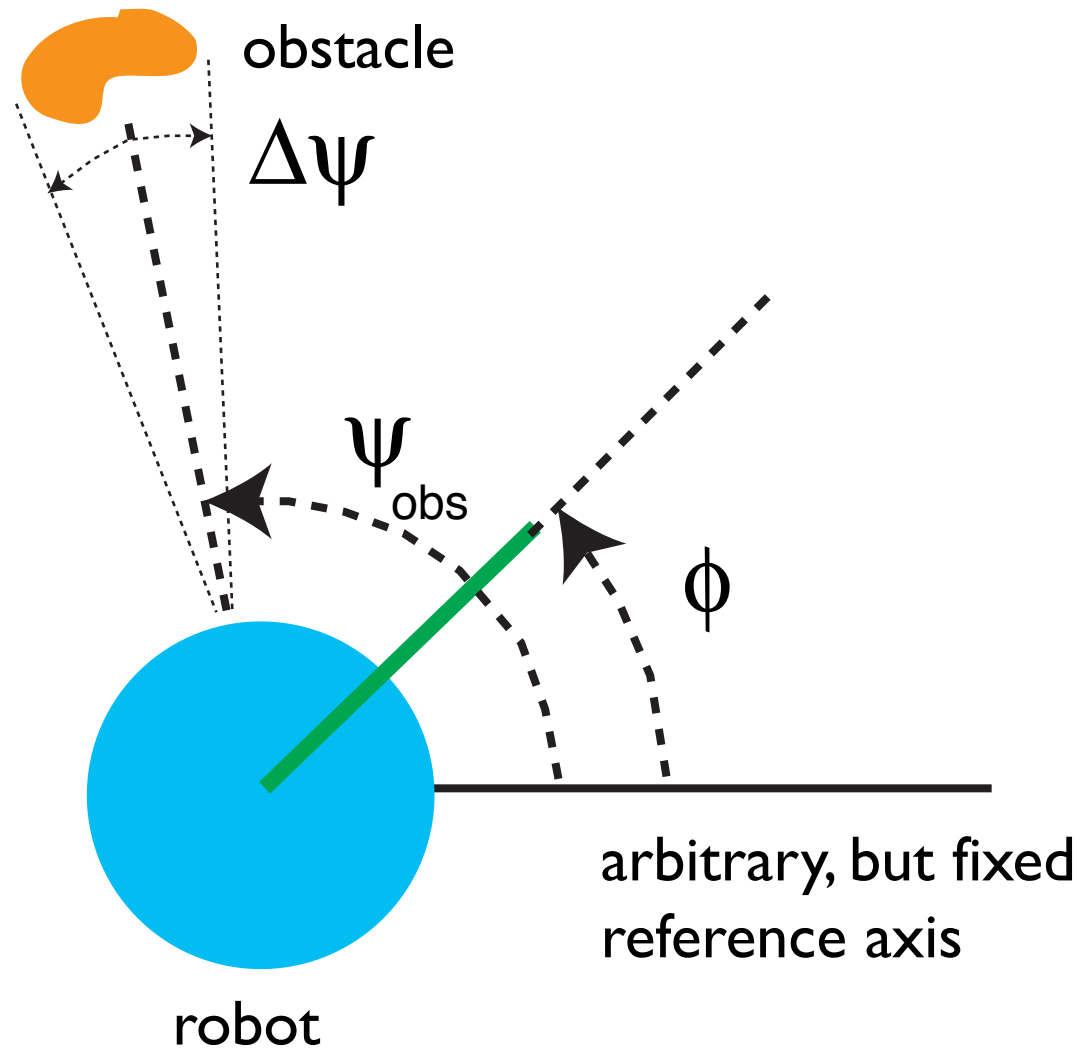


Attractor dynamics approach to behavior generation: vehicle motion Part 2: sub-symbolic approach

Gregor Schöner
Institute for Neural Computation, RUB

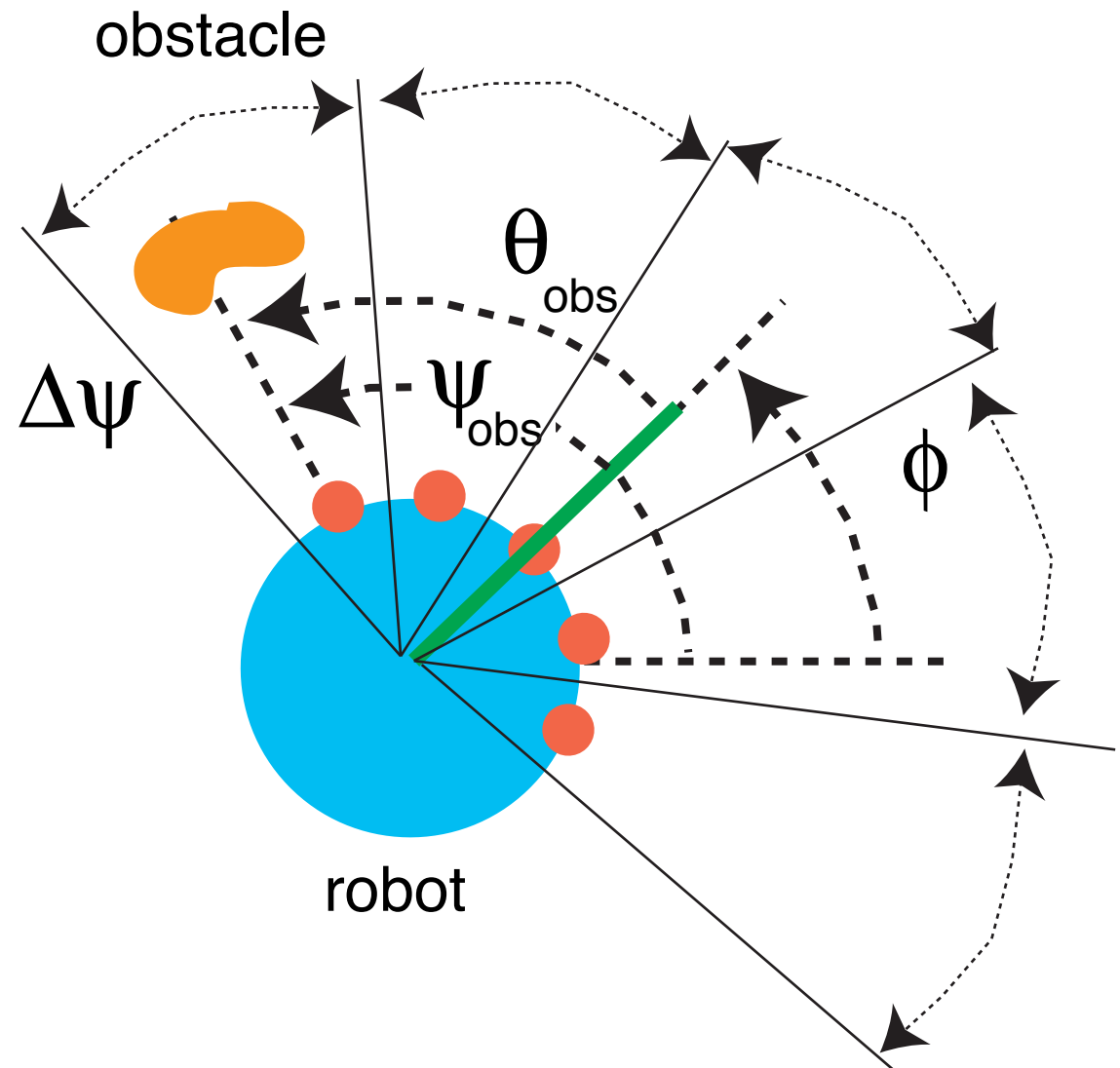
So far: “symbolic” approach

- high-level implementation: knowledge about objects in the world (“obstacles”, “targets”, etc)



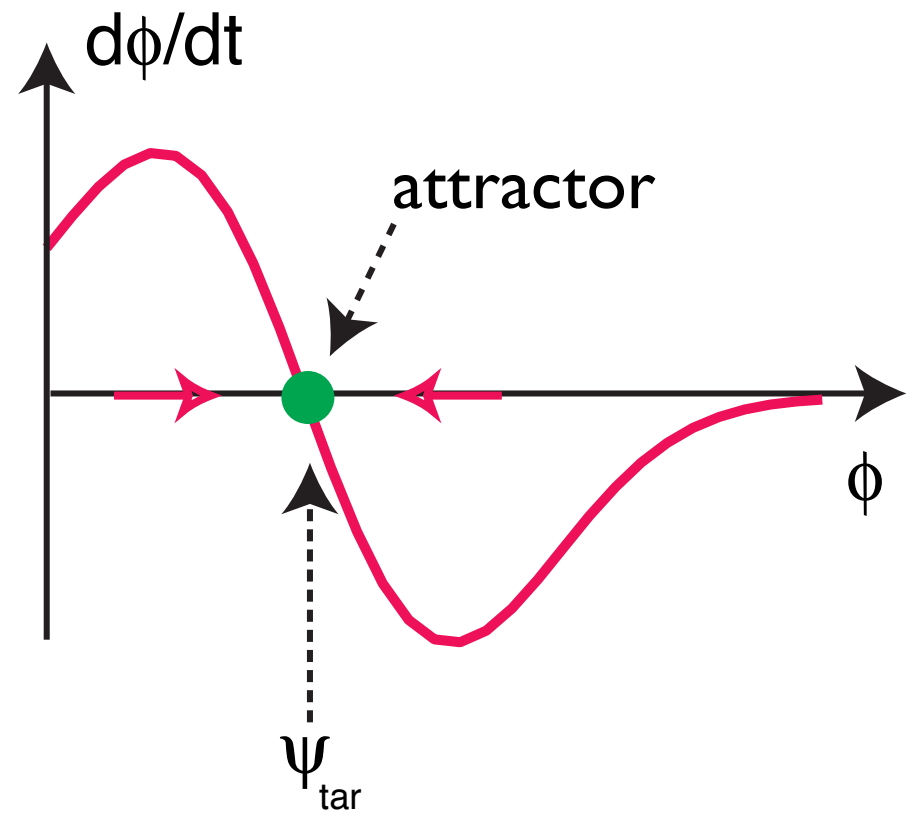
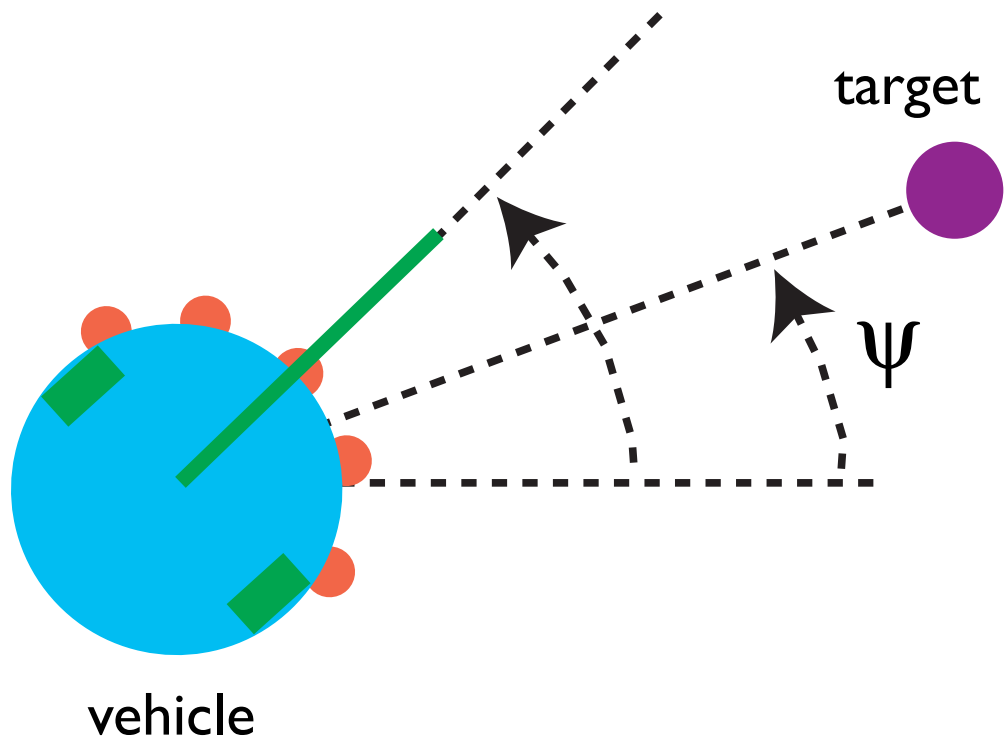
Now: “sub-symbolic” approach

- low-level implementation: use sensory information directly, not via objects



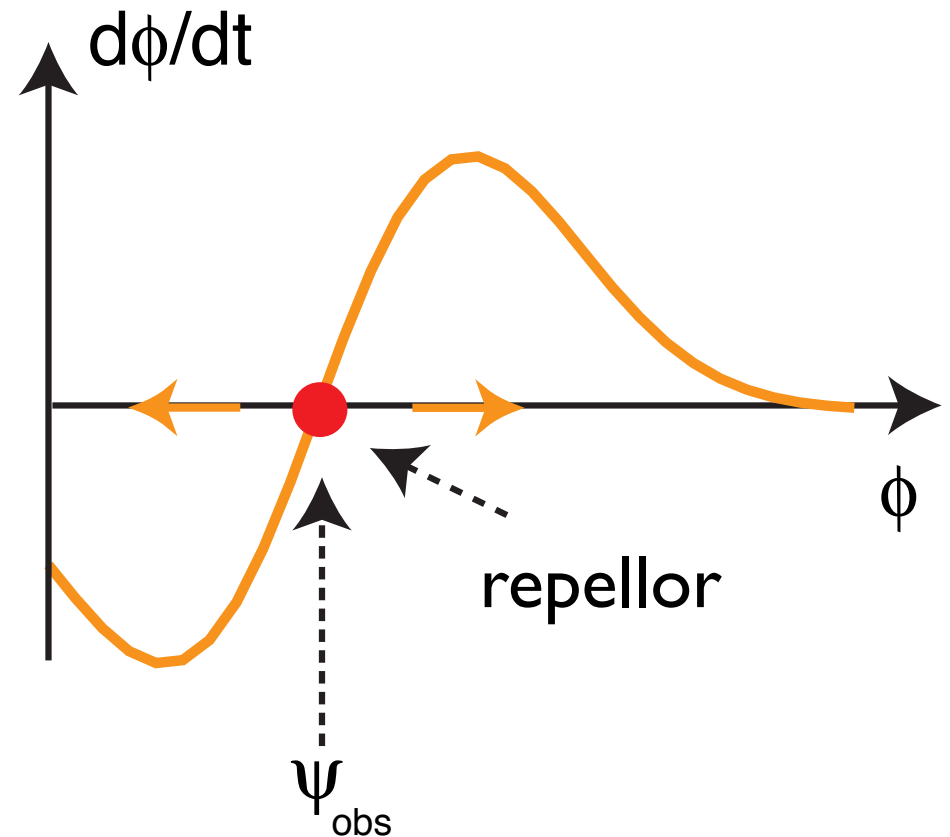
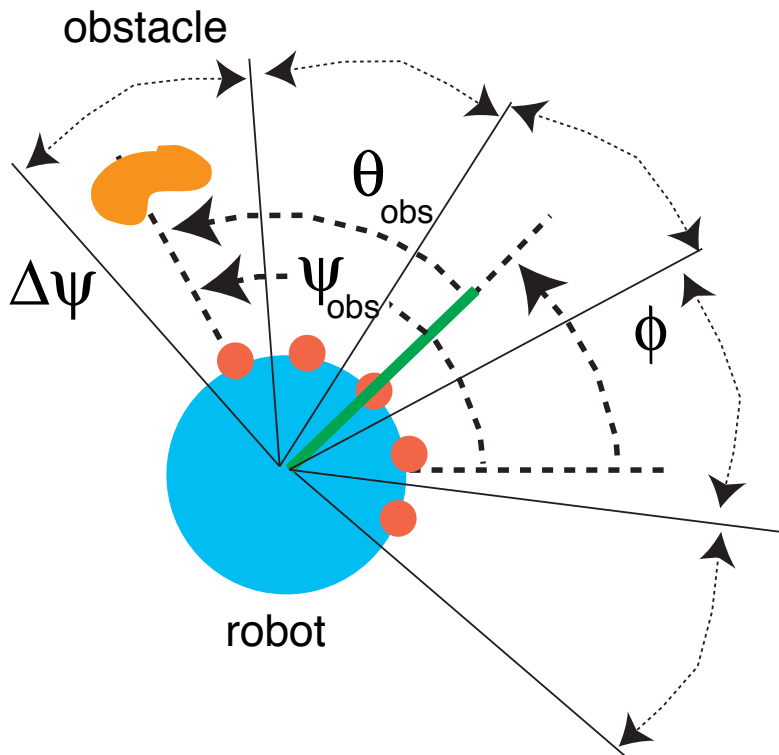
Target acquisition: still symbolic

- targets are segmented... in the foreground
- => need neural fields to perform this segmentation from low-level sensory information: Dynamic Field Theory ...



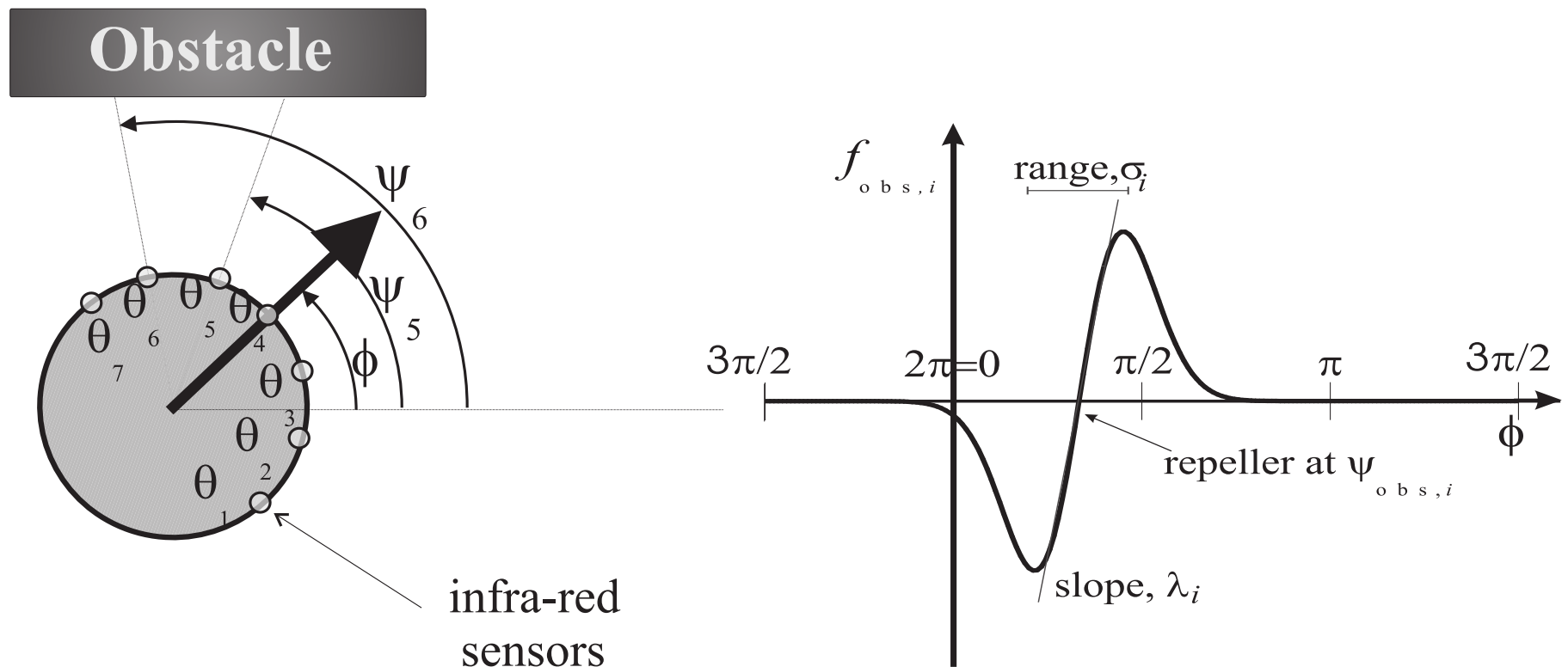
Obstacle avoidance: sub-symbolic

- obstacles need not be segmented
- do not care if obstacles are one or multiple: avoid them anyway...



Obstacle avoidance: sub-symbolic

- each sensor mounted at fixed angle θ
- that points in direction $\psi = \phi + \theta$ in the world
- erect a repeller at that angle



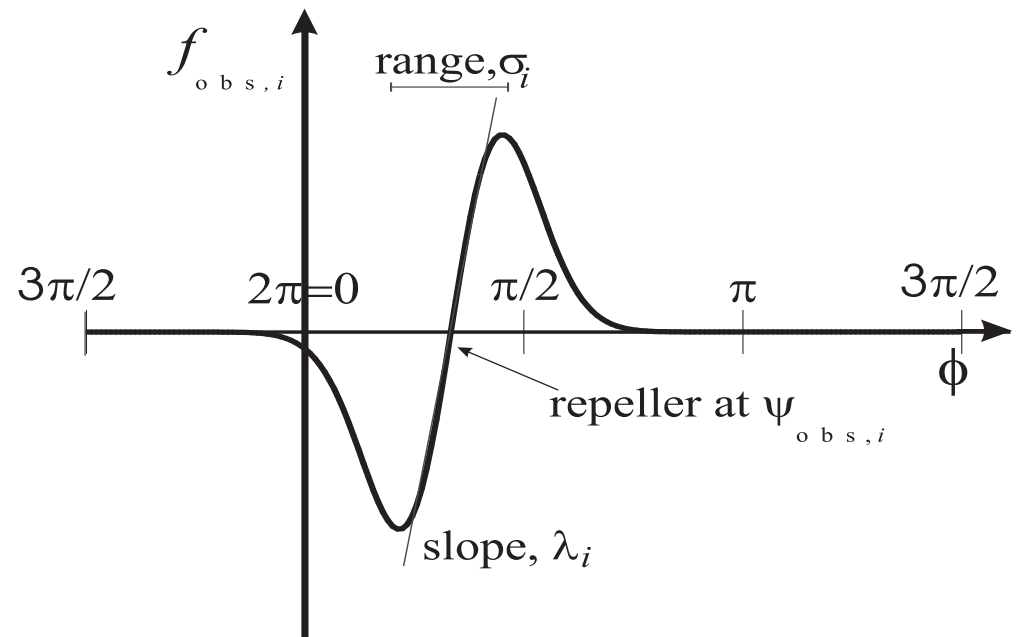
[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

$$f_{\text{obs},i}(\phi) = \lambda_i(\phi - \psi_i) \exp \left[-\frac{(\phi - \psi_i)^2}{2\sigma_i^2} \right] \quad i = 1, 2, \dots, 7$$

■ Note: only $\phi - \psi = -\theta$ shows up, which is constant!

■ \Rightarrow force-let does not depend on ϕ !



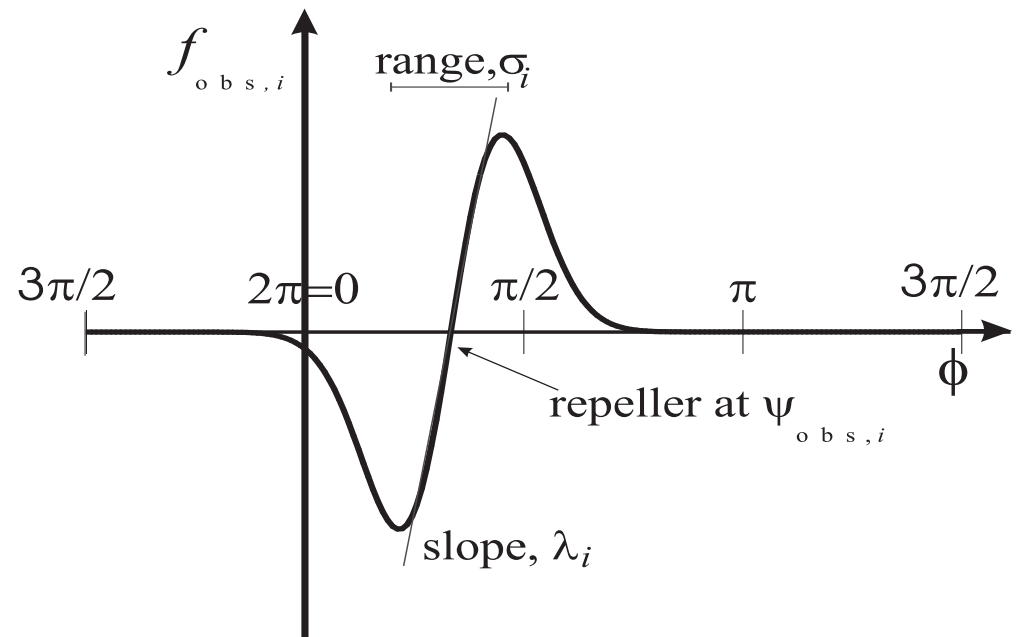
[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

$$f_{\text{obs},i}(\phi) = \lambda_i(\phi - \psi_i) \exp \left[-\frac{(\phi - \psi_i)^2}{2\sigma_i^2} \right] \quad i = 1, 2, \dots, 7$$

$$\lambda_i = \beta_1 \cdot \exp \left[-\frac{d_i}{\beta_2} \right]$$

- Repulsion strength decreases with distance, d_i
- \Rightarrow only close obstacles matter



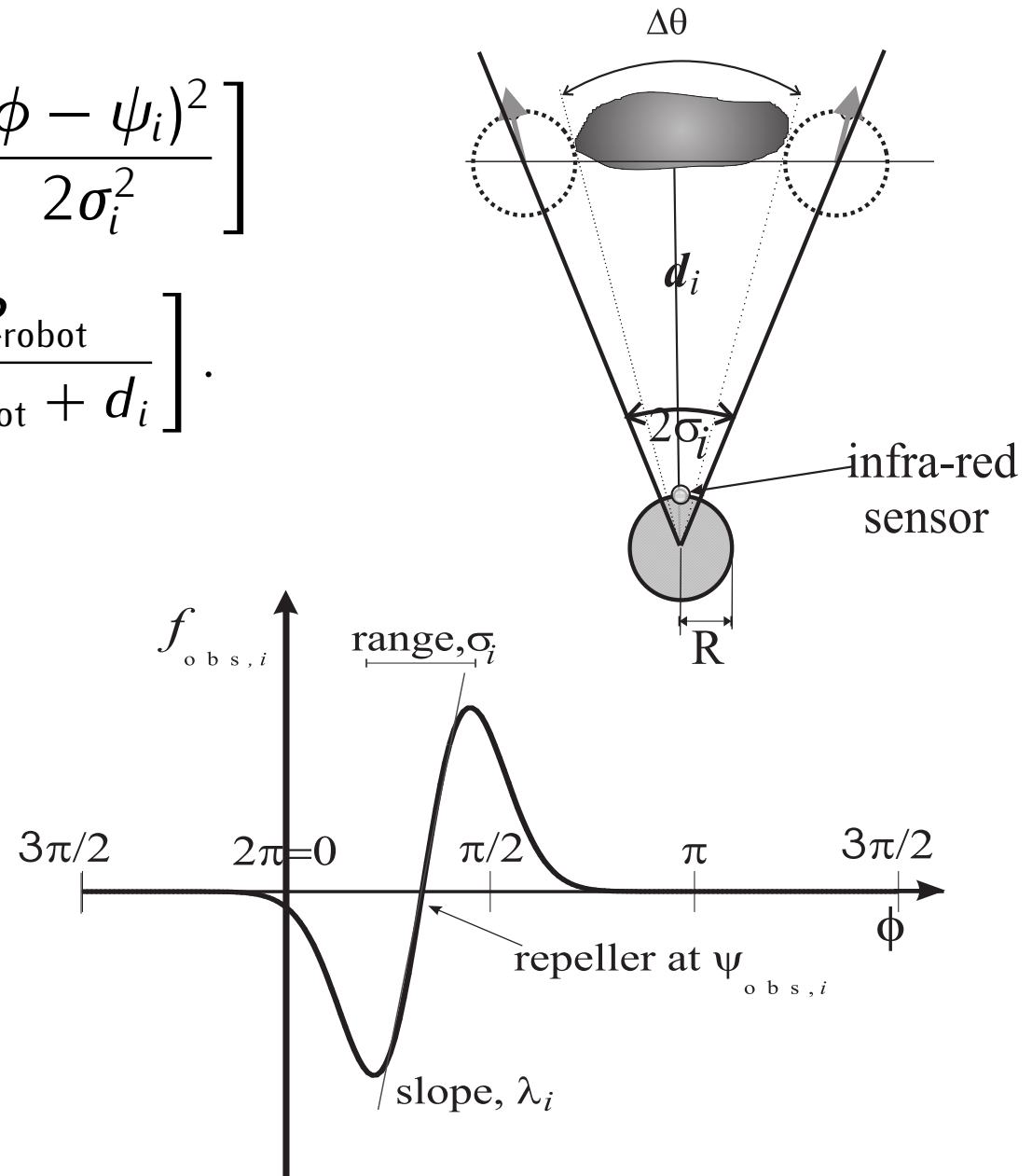
[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

$$f_{\text{obs},i}(\phi) = \lambda_i(\phi - \psi_i) \exp \left[-\frac{(\phi - \psi_i)^2}{2\sigma_i^2} \right]$$

$$\sigma_i = \arctan \left[\tan \left(\frac{\Delta\theta}{2} \right) + \frac{R_{\text{robot}}}{R_{\text{robot}} + d_i} \right].$$

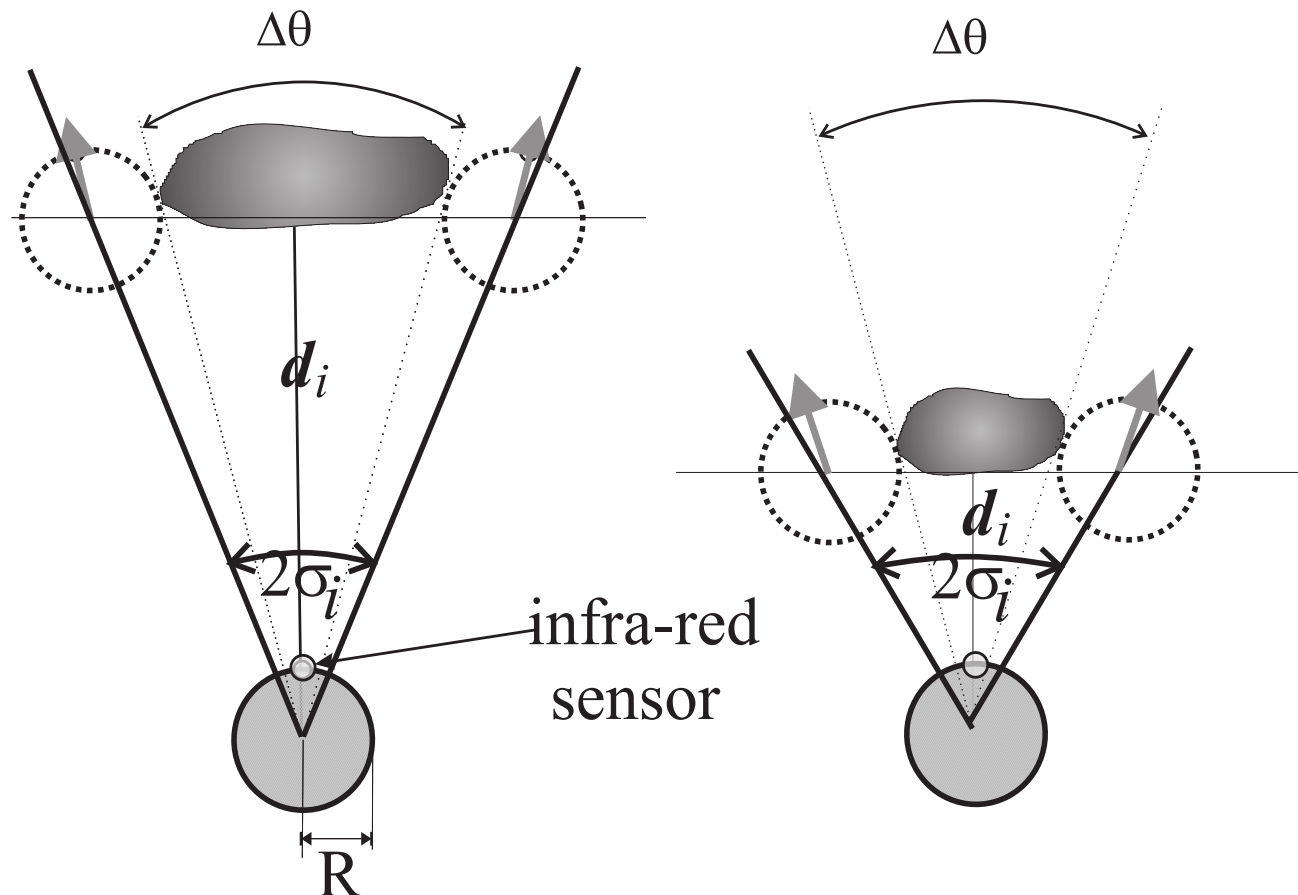
- angular range depends on sensor cone $\Delta\theta$ and size over distance



[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

■ \Rightarrow as a result, range becomes wider as obstacle moves closer

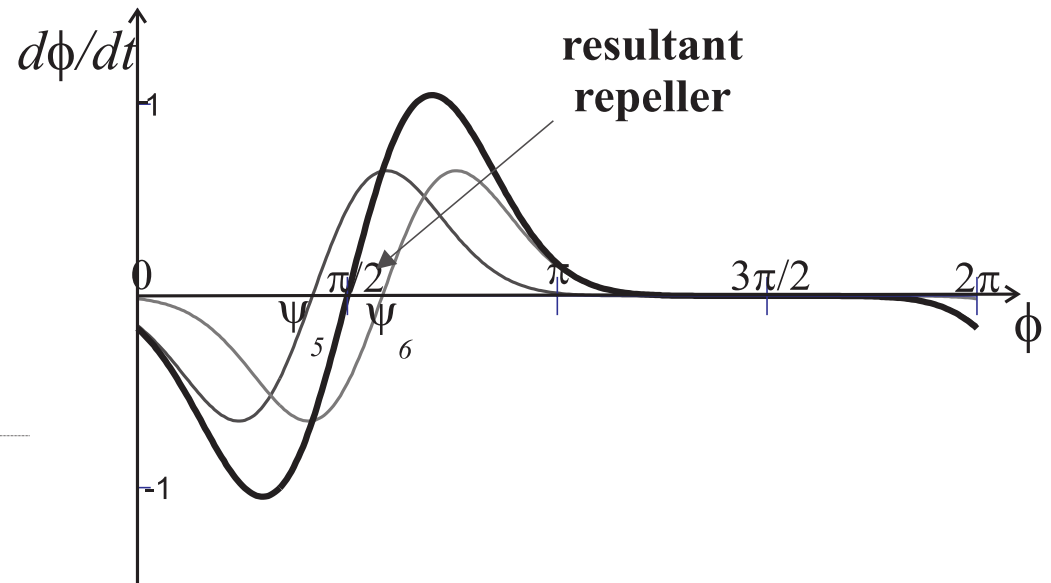
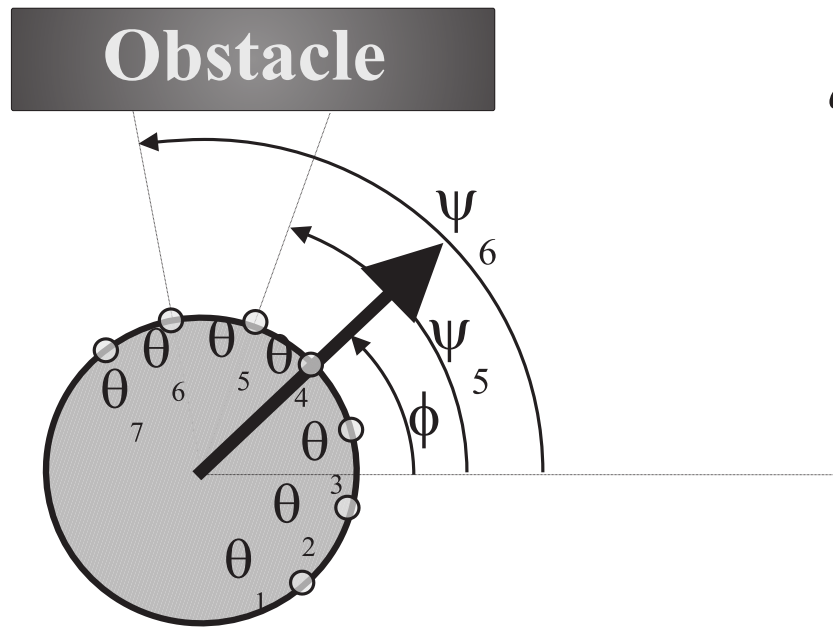


[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

- summing contributions from all sensors

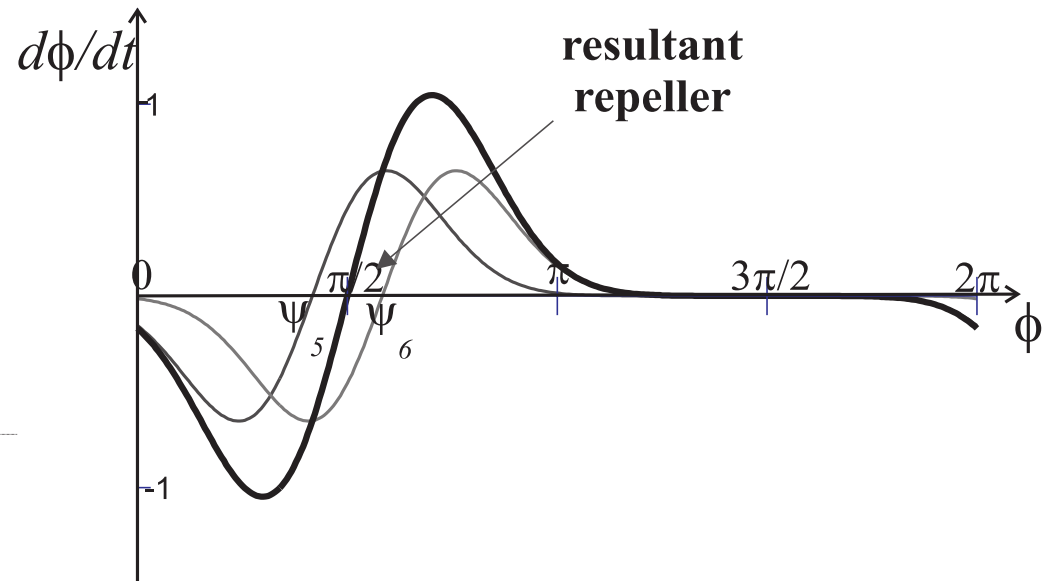
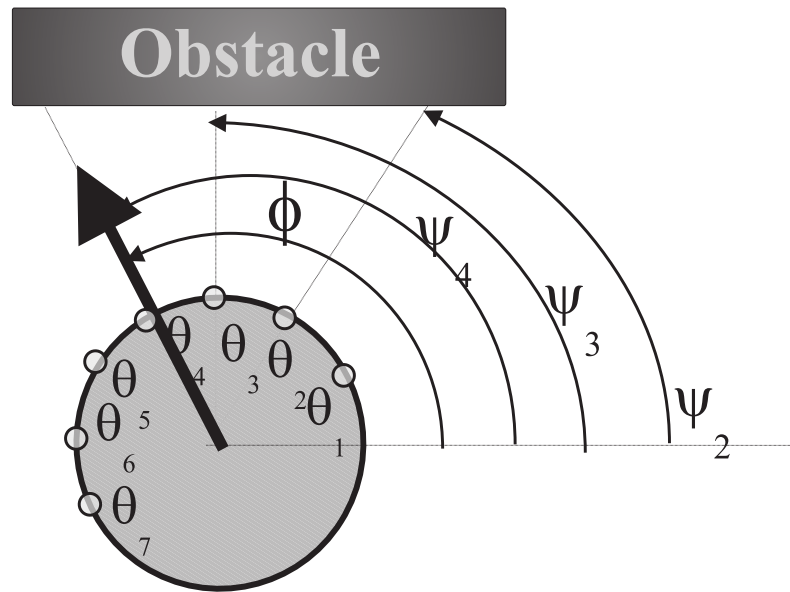
$$\frac{d\phi}{dt} = f_{\text{obs}}(\phi) = \sum_{i=1}^7 f_{\text{obs},i}(\phi)$$



[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

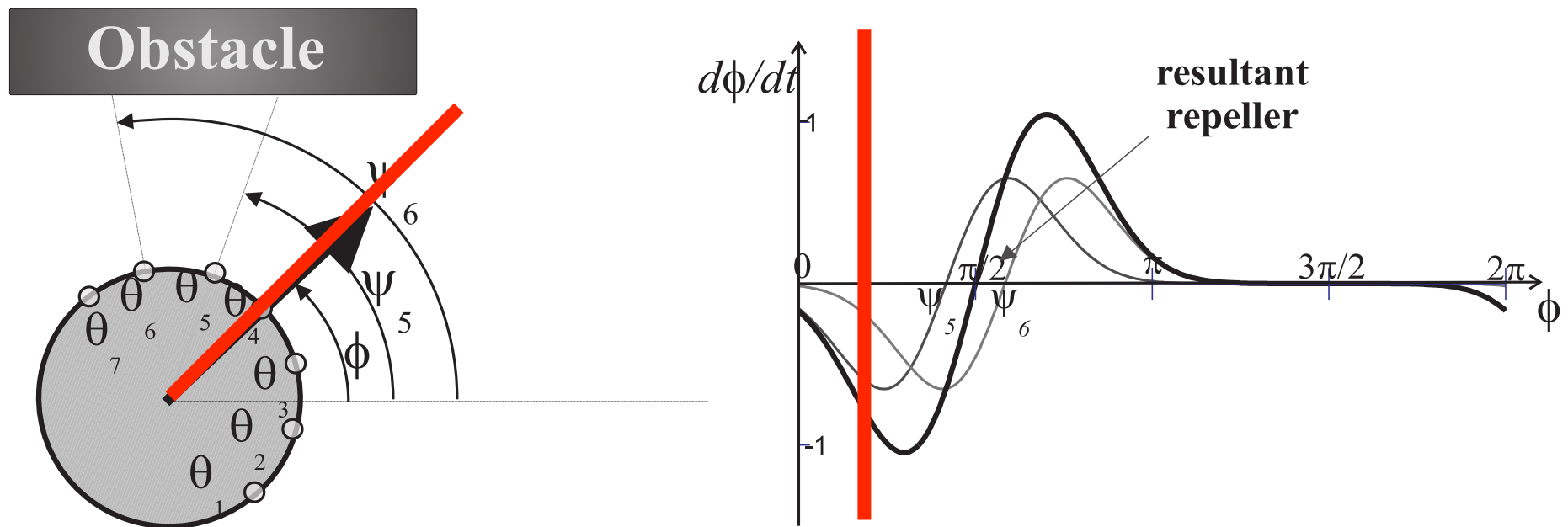
- but why does it work?
- shouldn't there be a problem when heading changes (e.g. from the dynamics itself)?



[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

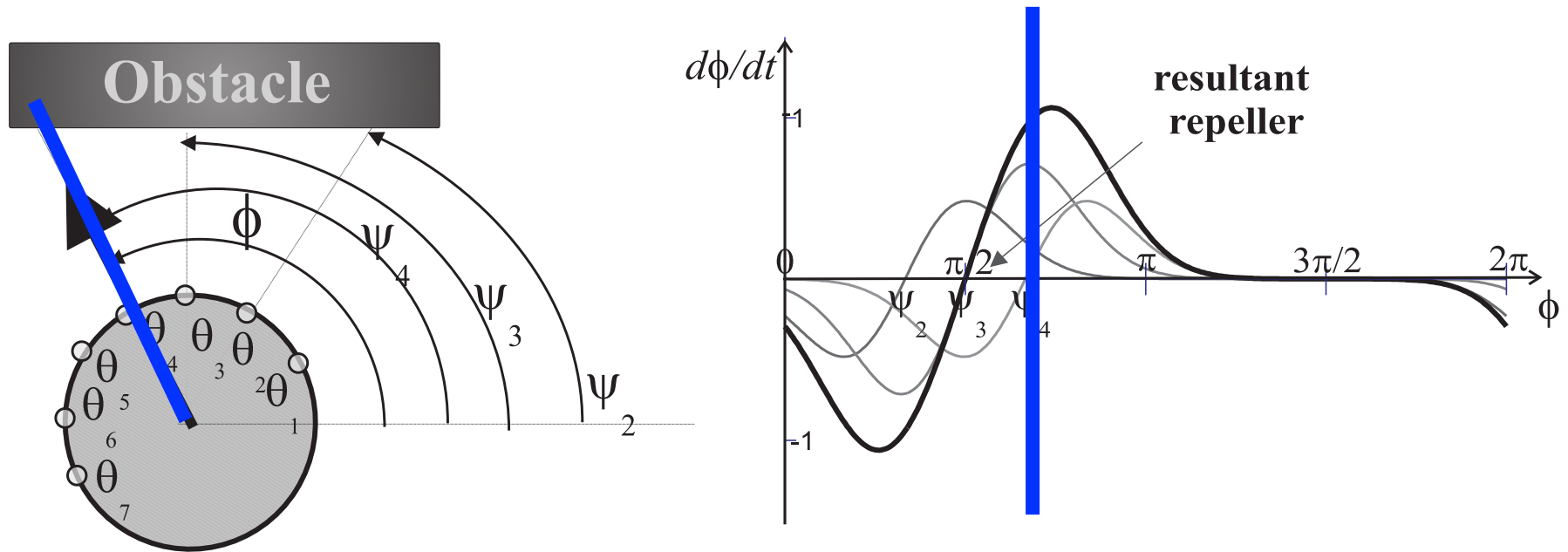
- but why does it work?
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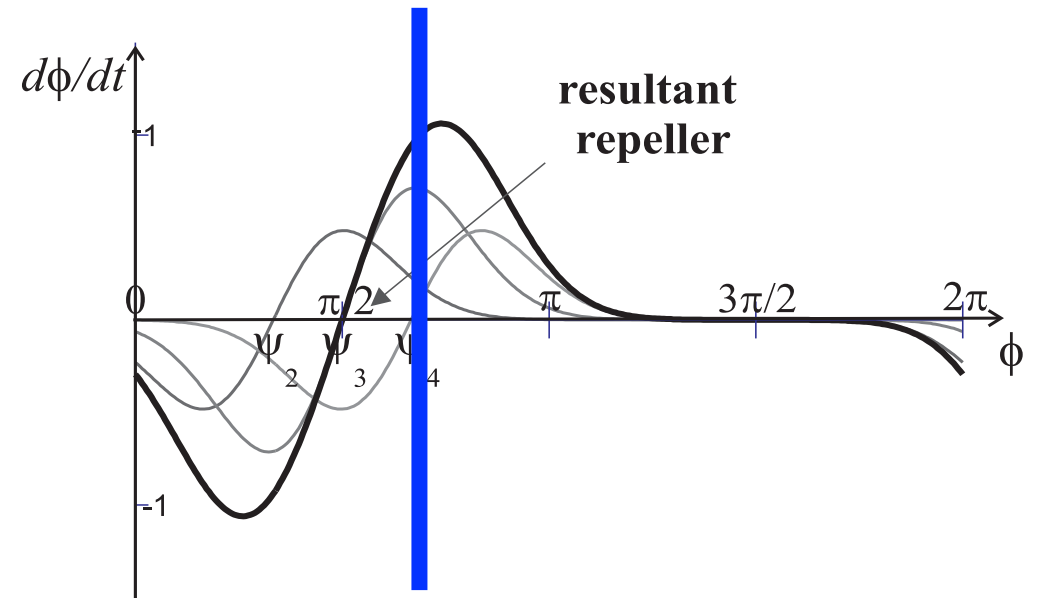
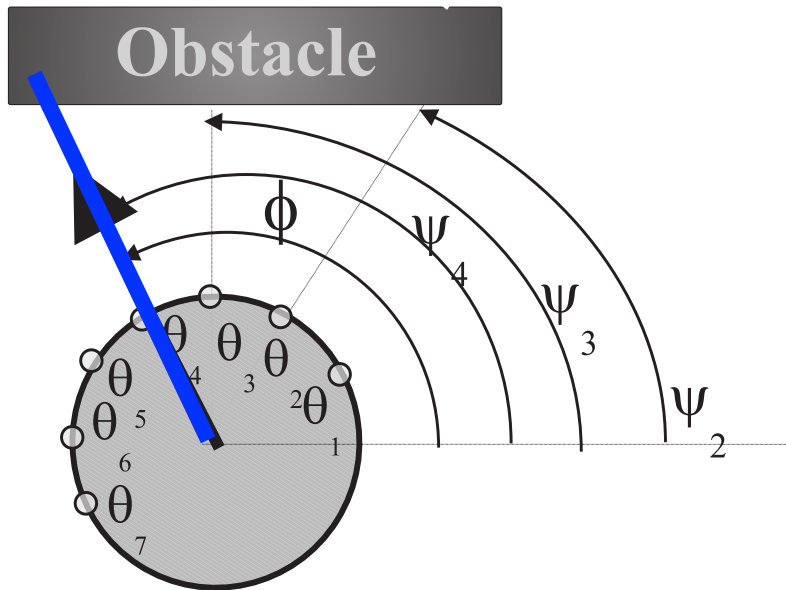
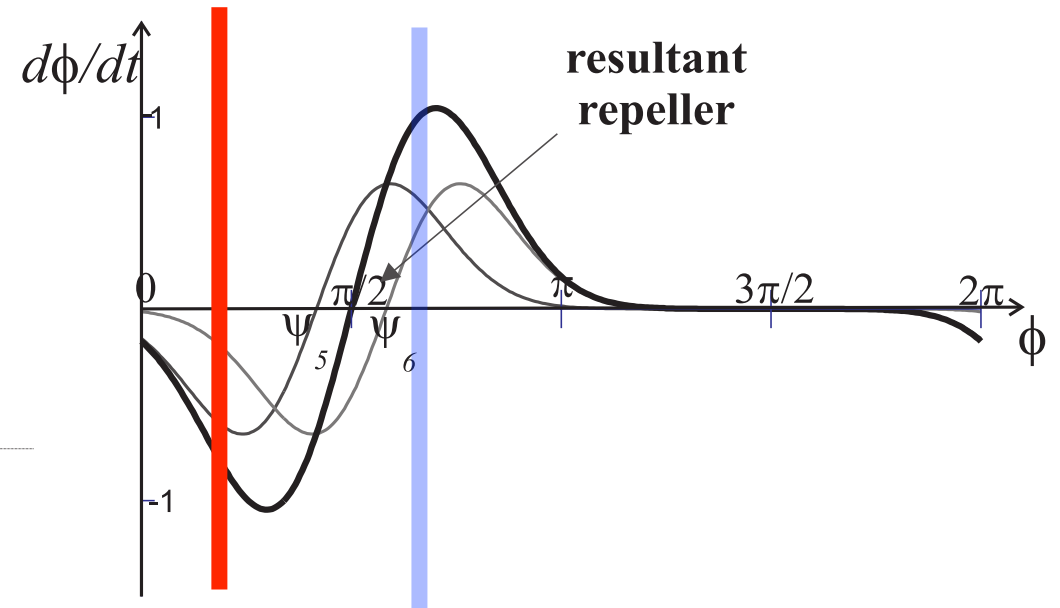
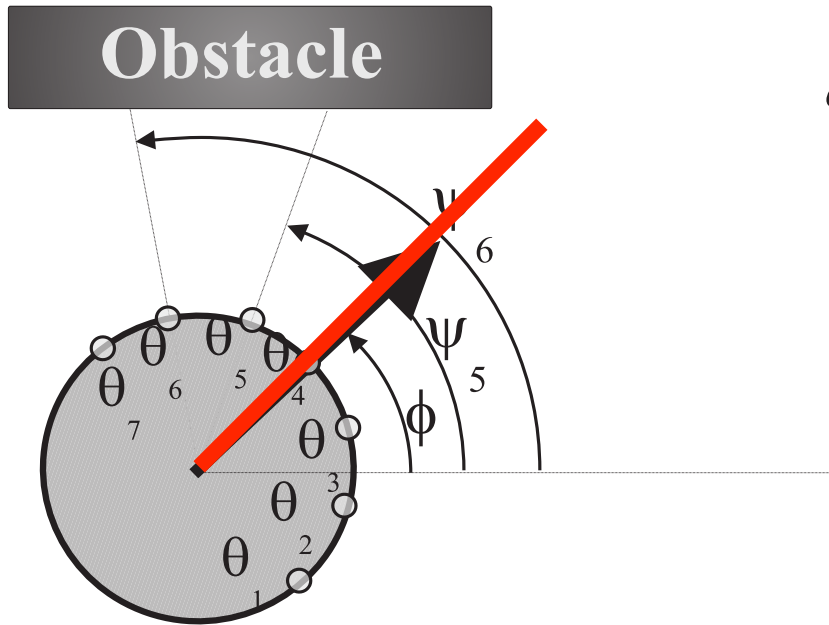
[from: Bicho, Jokeit, Schöner]

Obstacle avoidance: sub-symbolic

- but why does it work?
- shouldn't there be a problem when heading changes (e.g. from the dynamics itself)?



[from: Bicho, Jokeit, Schöner]



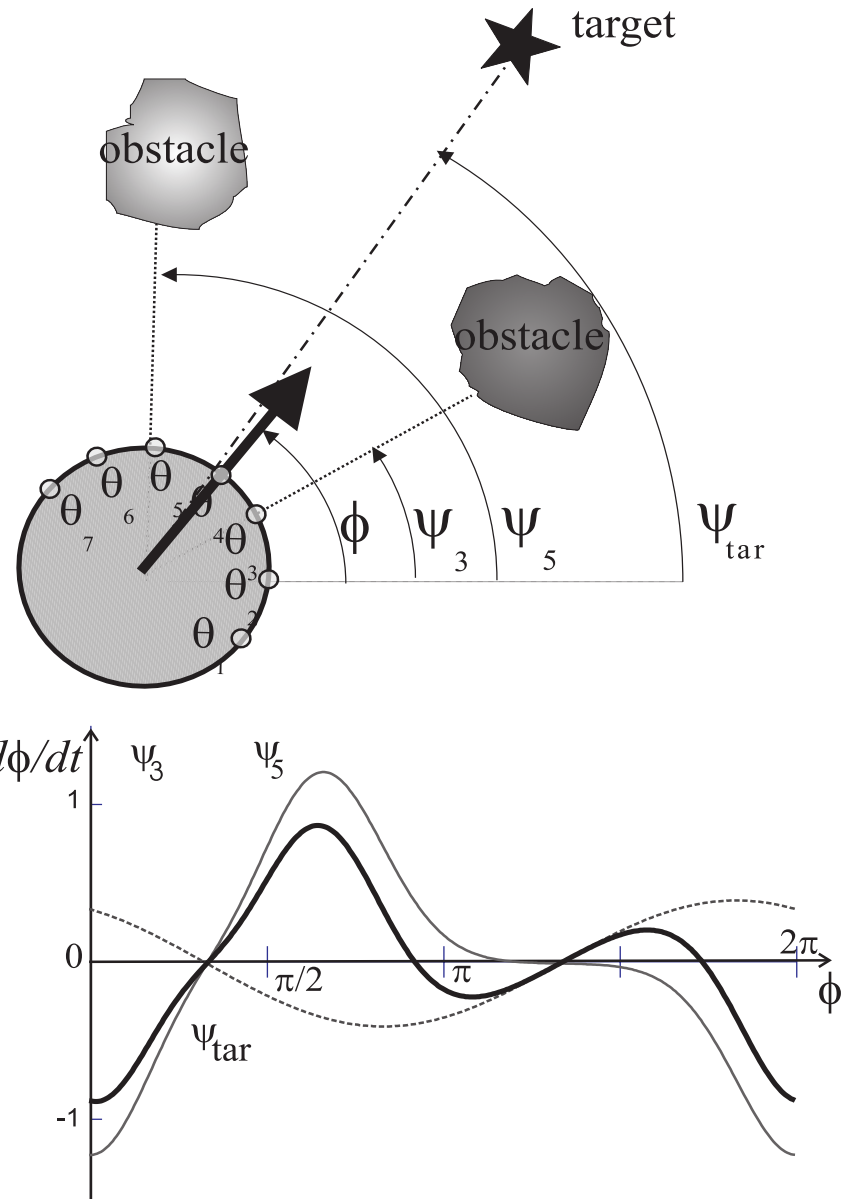
■ => dynamics invariant!

[from: Bicho, Jokeit, Schöner]

Behavioral Dynamics

- integrating the two behaviors

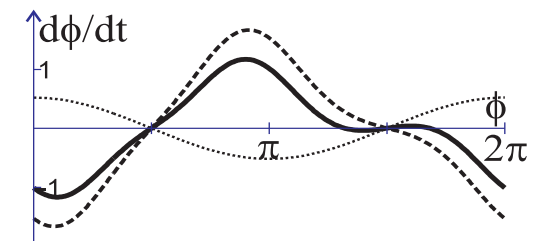
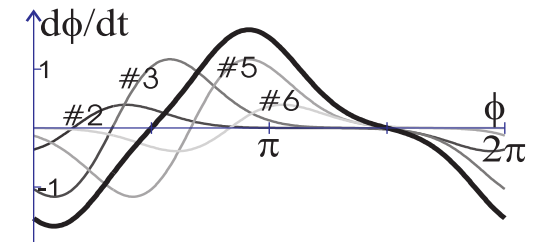
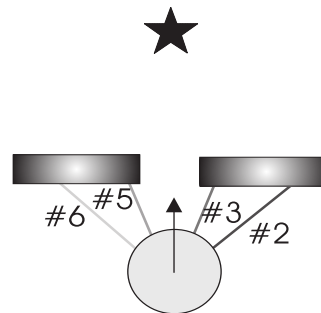
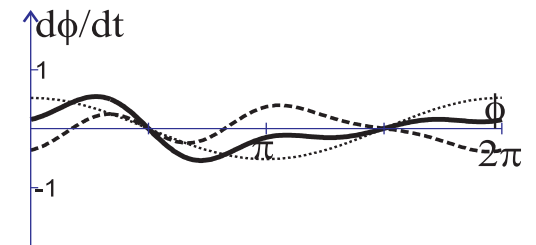
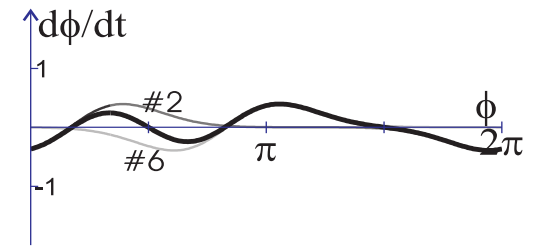
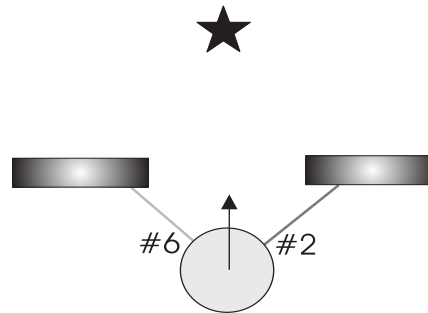
$$\frac{d\phi}{dt} = f_{\text{obs}}(\phi) + f_{\text{tar}}(\phi)$$



[from: Bicho, Jokeit, Schöner]

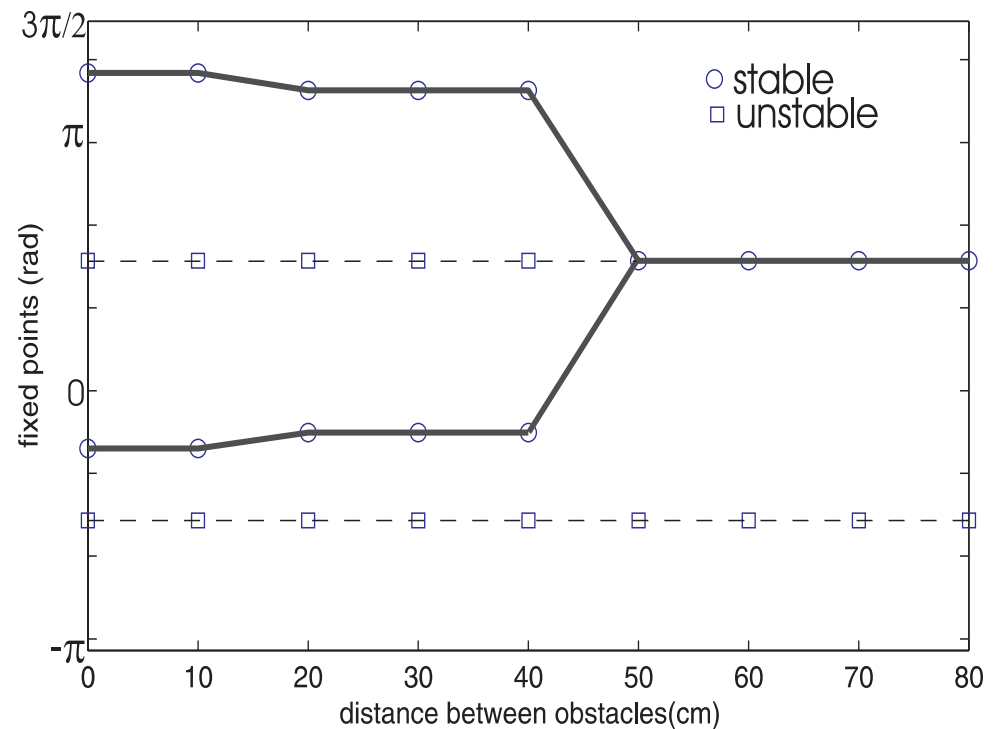
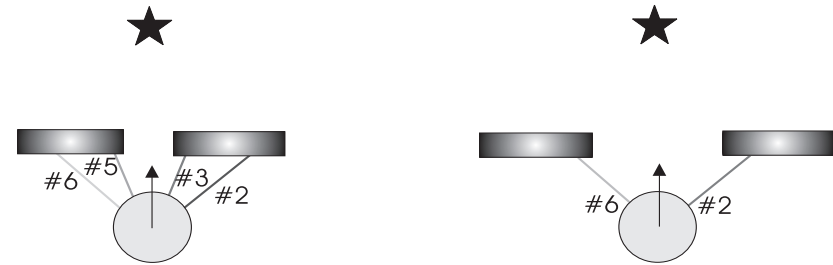
Bifurcations

■ bifurcation as a function of the size of the opening between obstacles

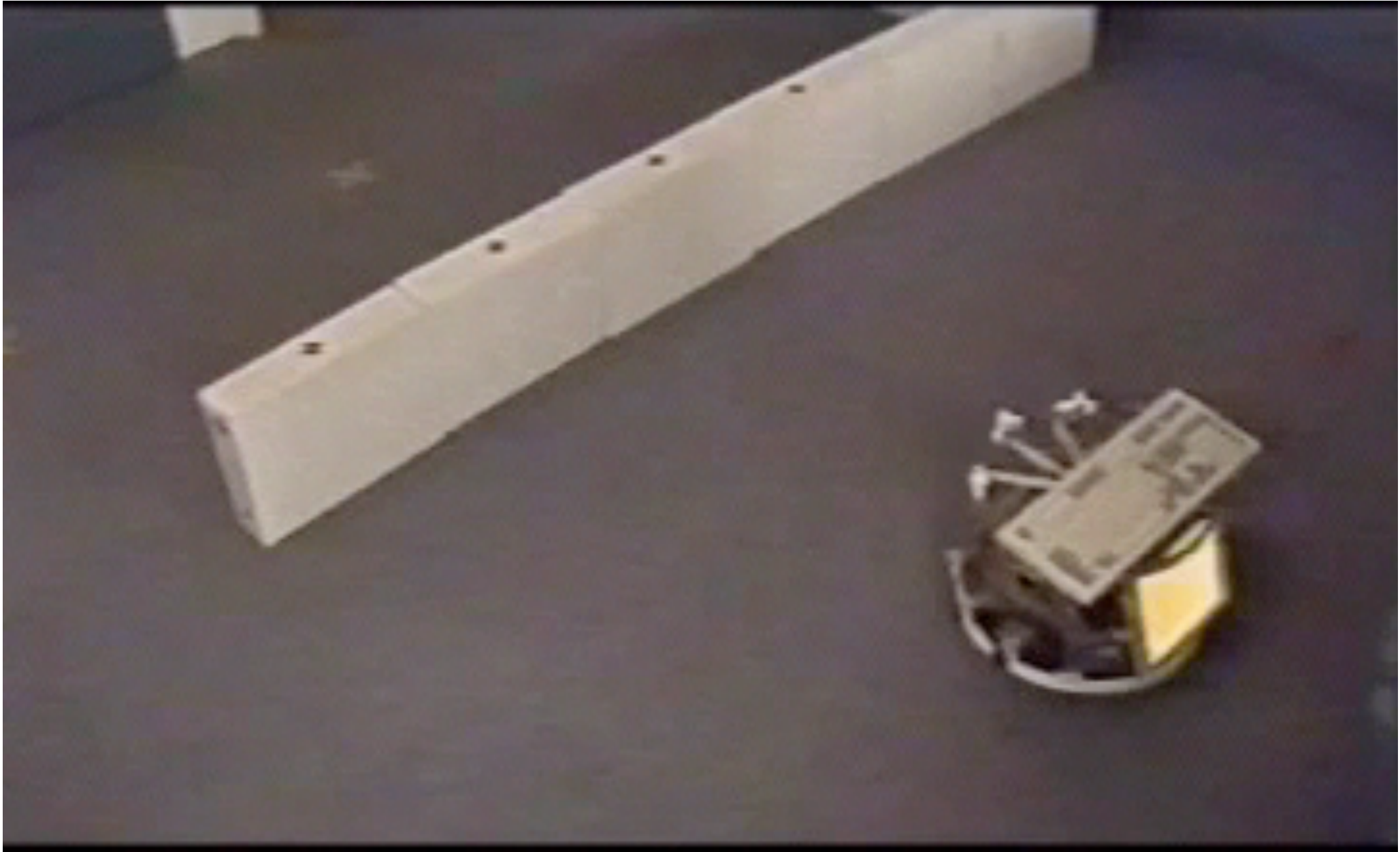


Bifurcations

- bifurcation as a function of the size of the opening between obstacles
- => tune distance dependence of repulsion so that bifurcation occurs at the right opening

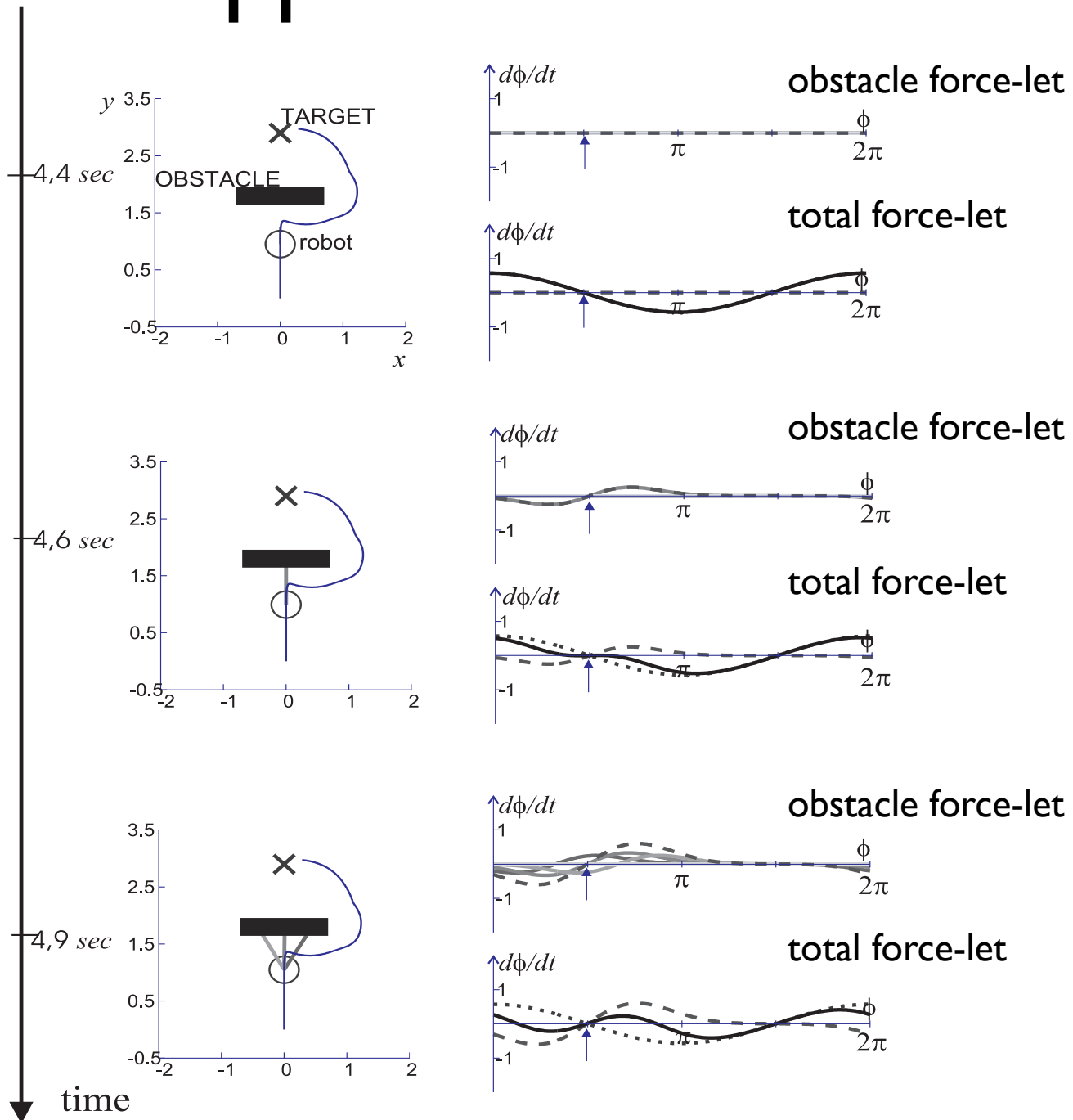


Bifurcations



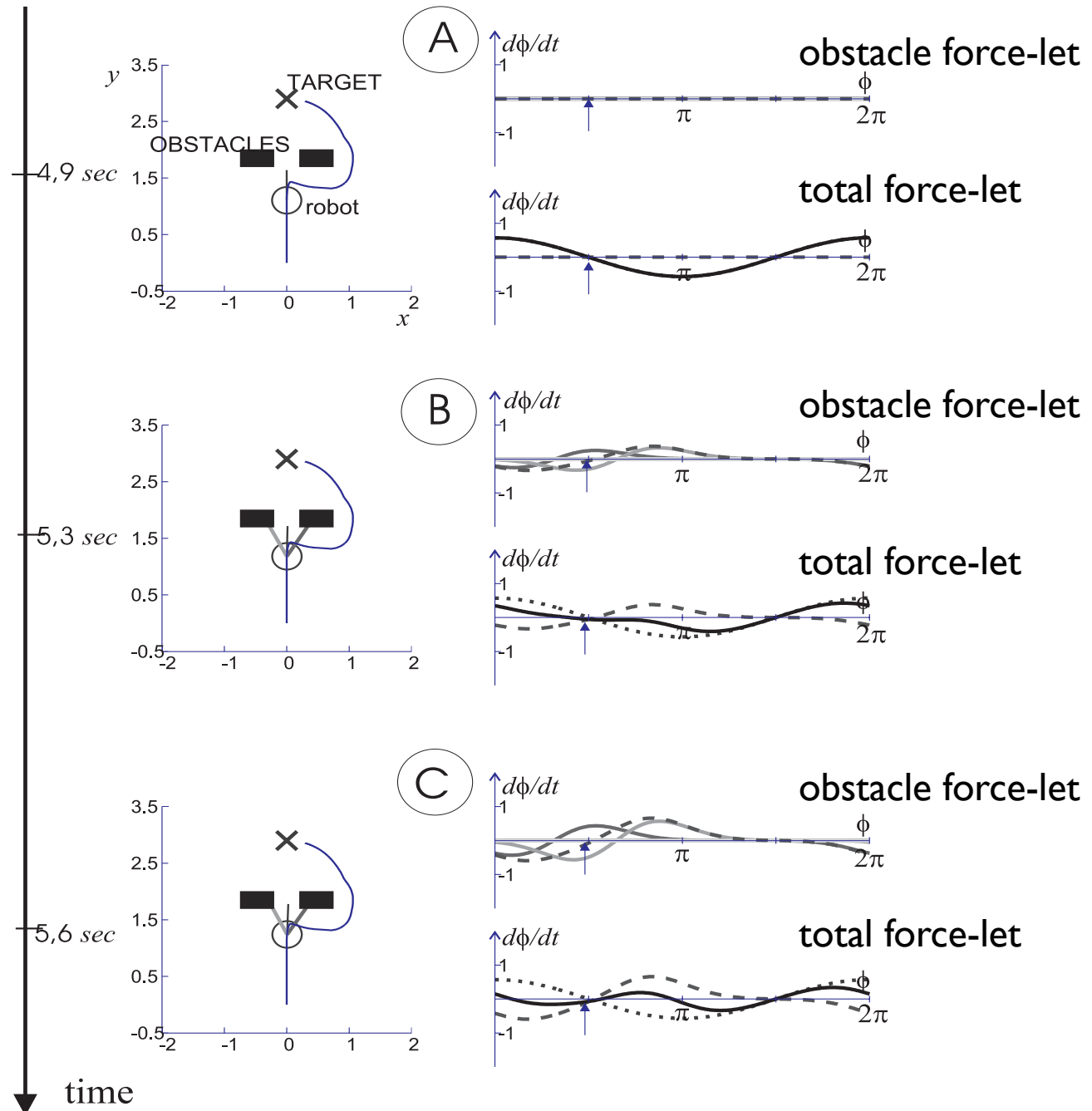
Bifurcation on approach to wall

- initially attractor dominates: weak repulsion
- bifurcation
- then obstacles dominate: strong repulsion and total repulsion



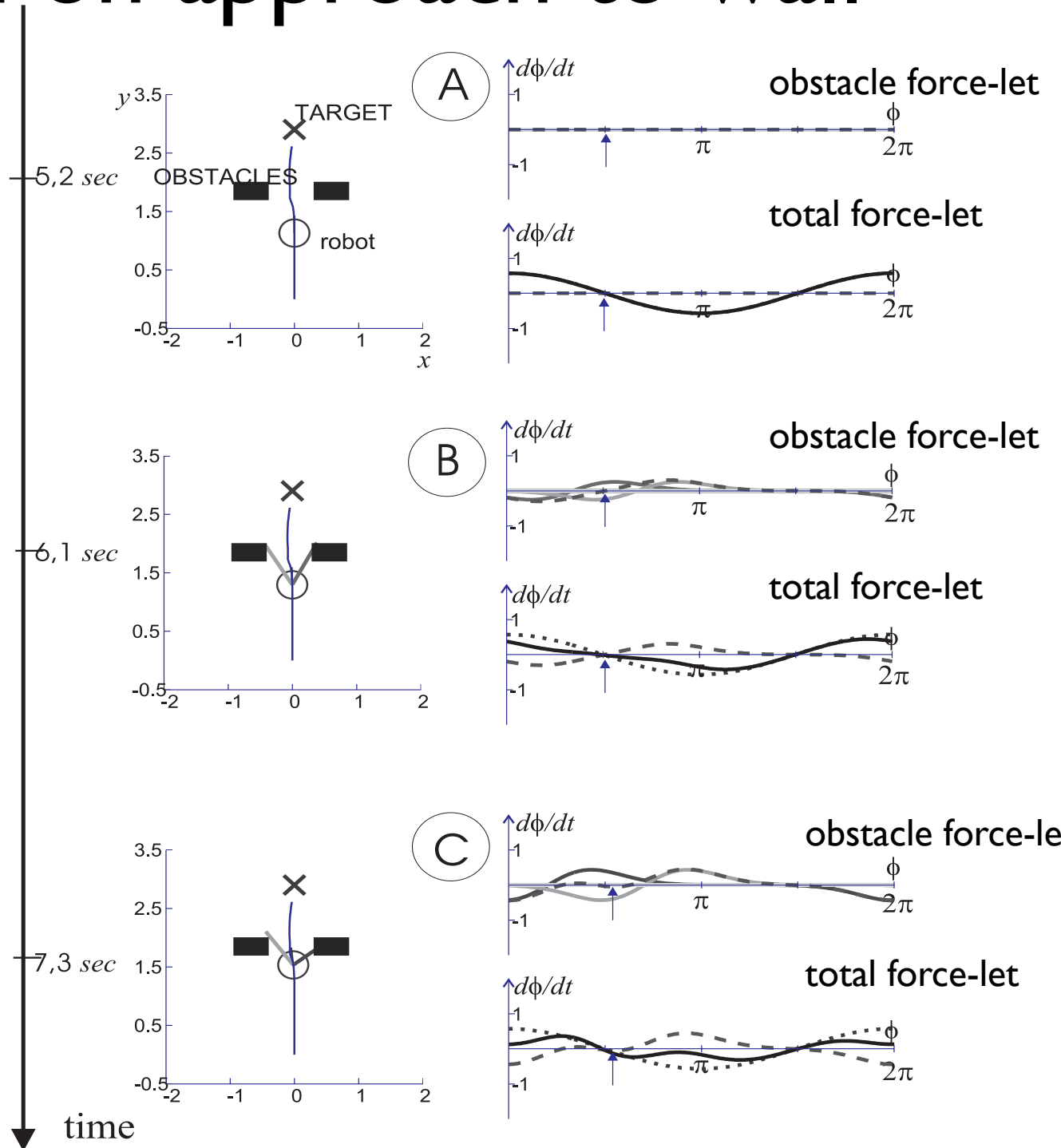
Bifurcation on approach to wall

■ same with small opening



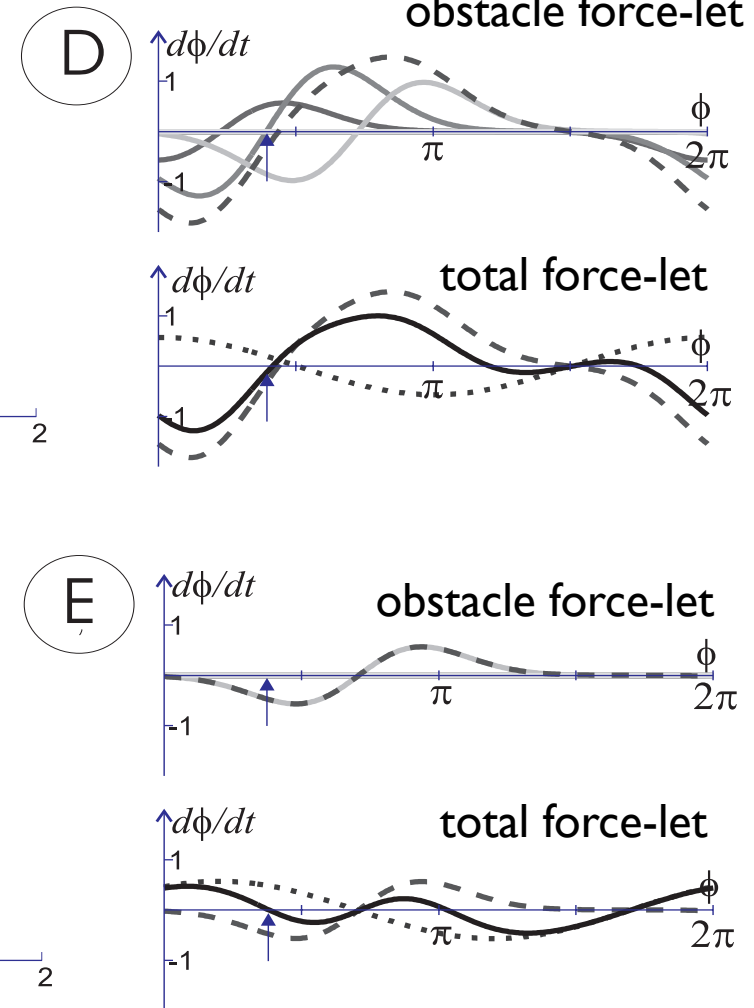
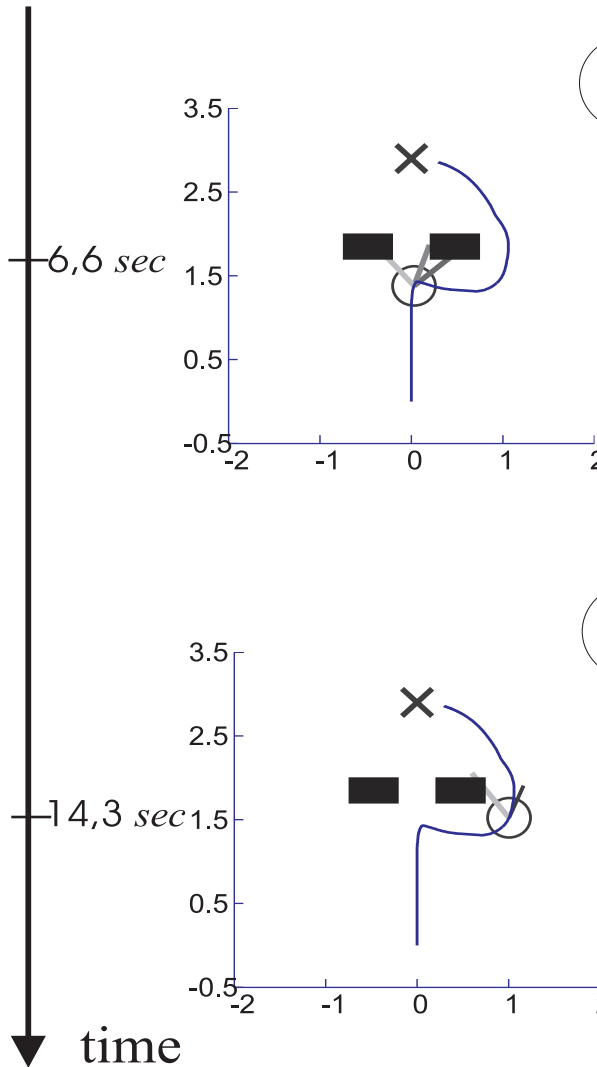
Bifurcation on approach to wall

■ at larger opening:
 repulsion
 weak all the
 way through:
 attractor
 remains stable



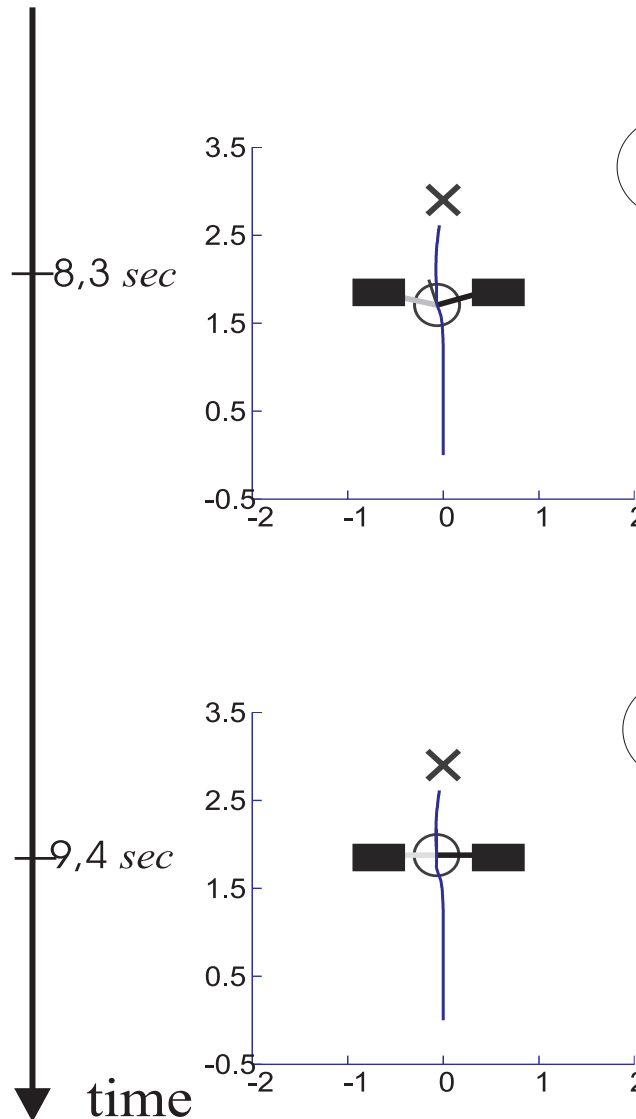
Tracking attractor

as robot moves around obstacles, tracks the moving attractor

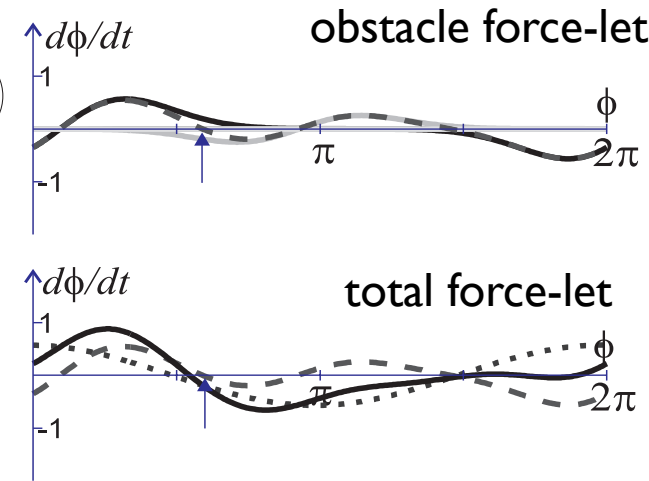


Tracking attractor

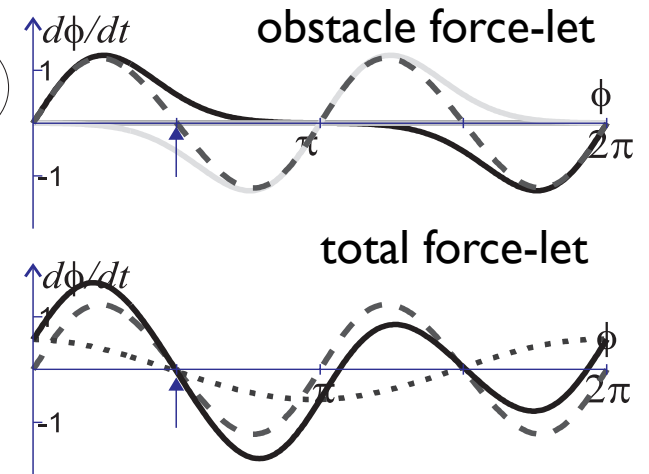
as robot moves in between obstacles, the dynamics changes but not the attractor



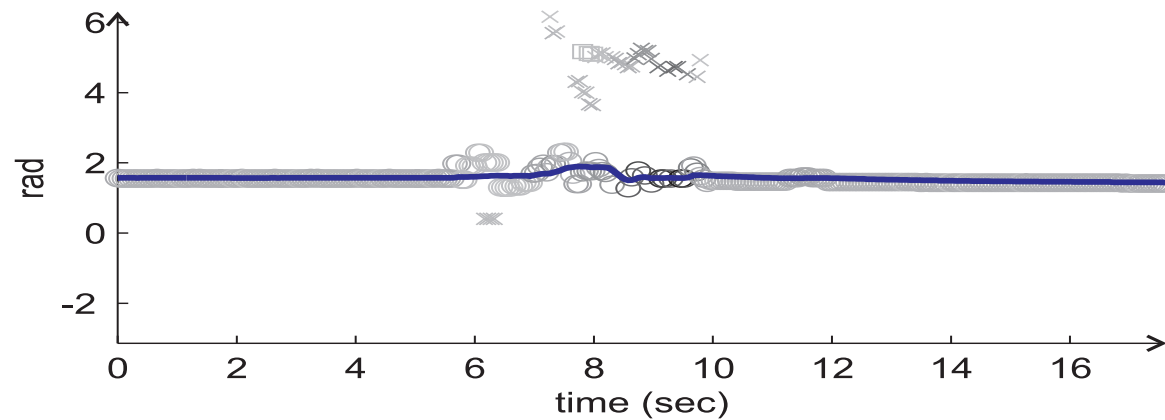
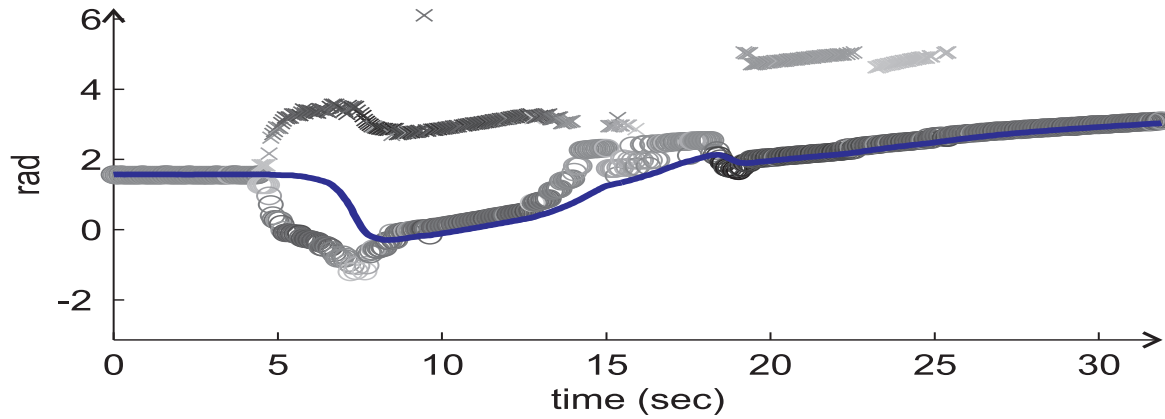
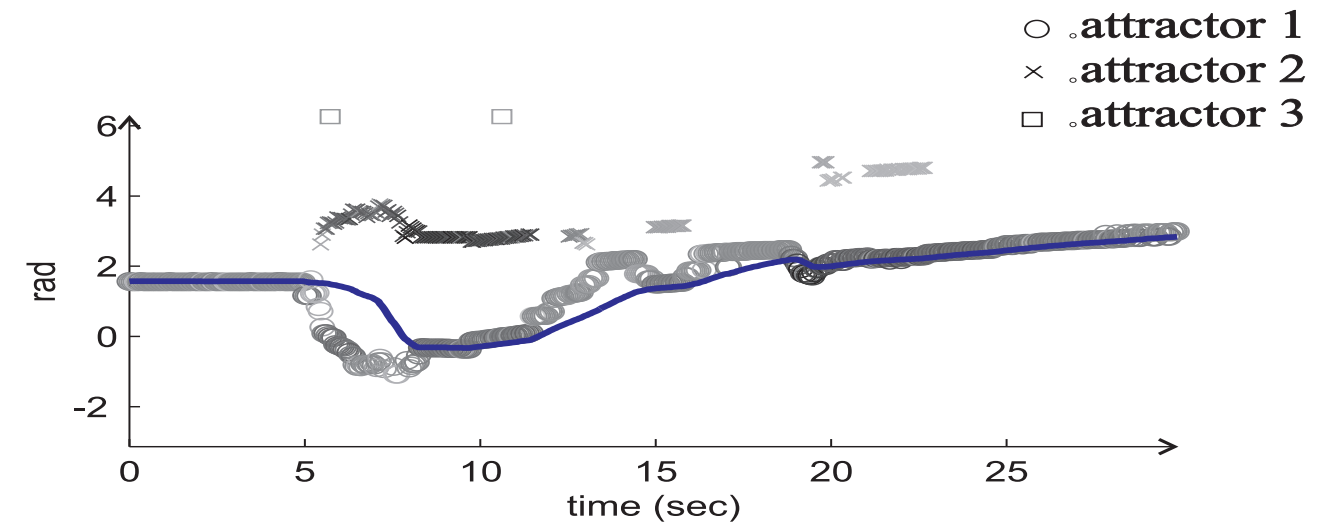
D



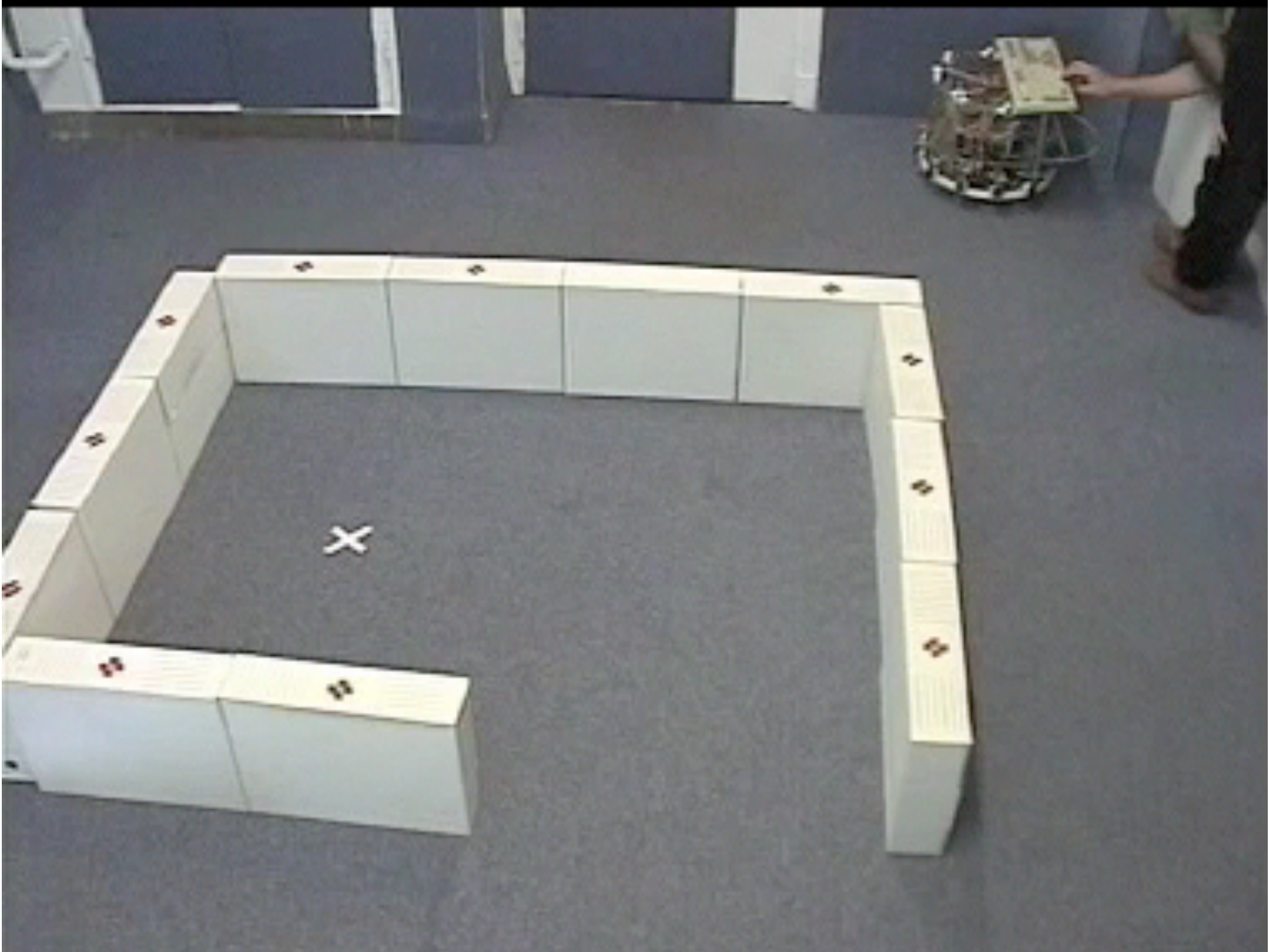
E

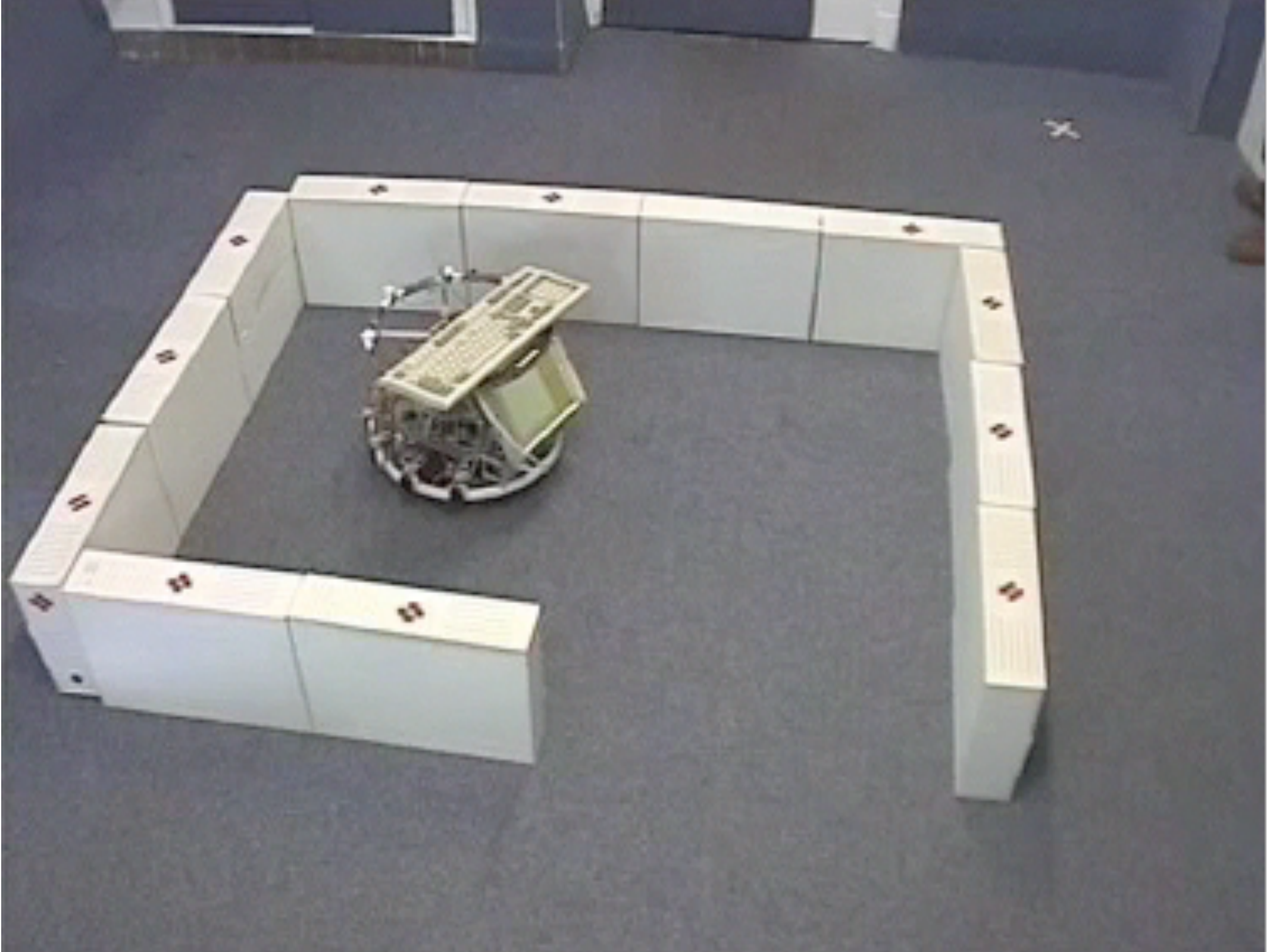


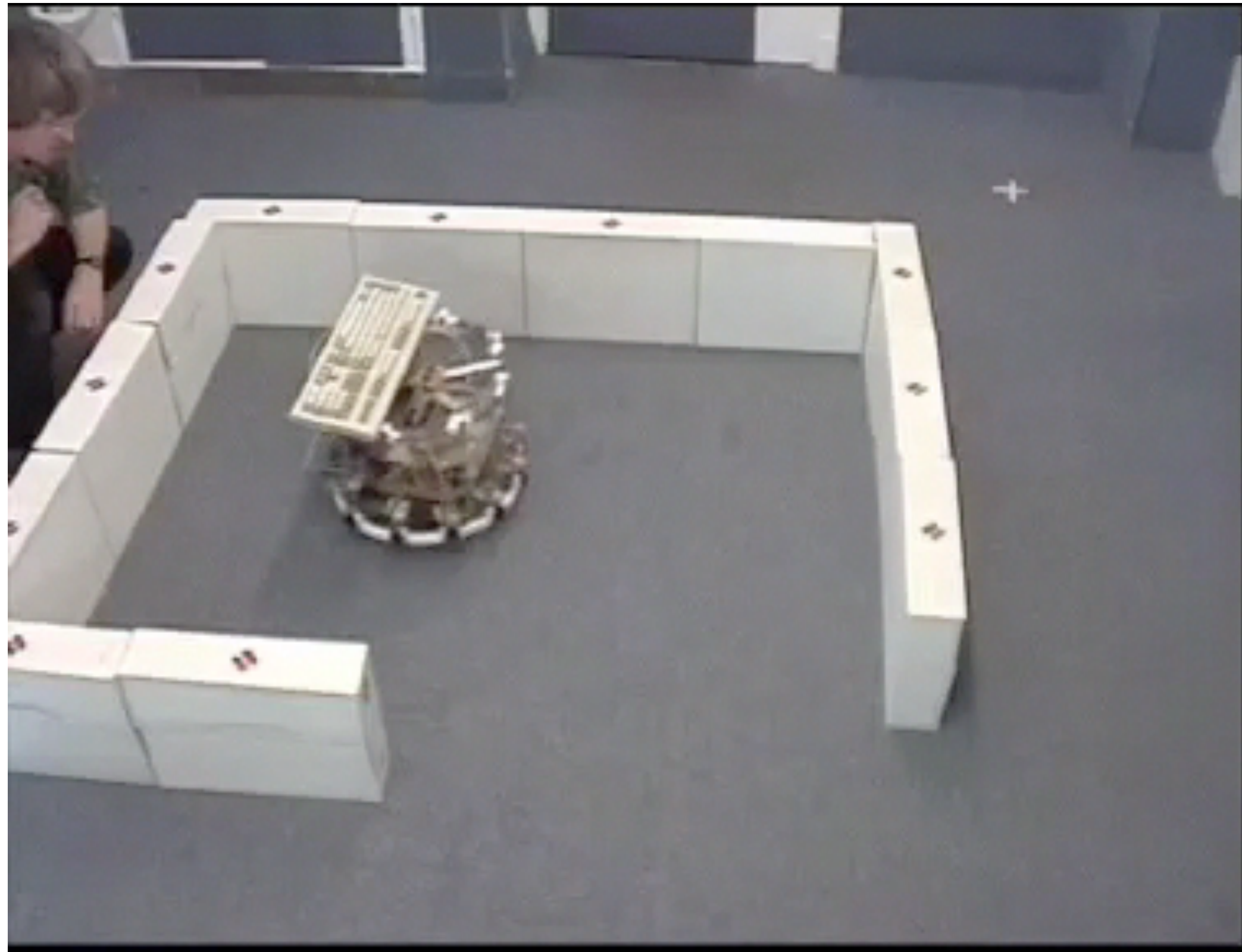
Tracking attractors

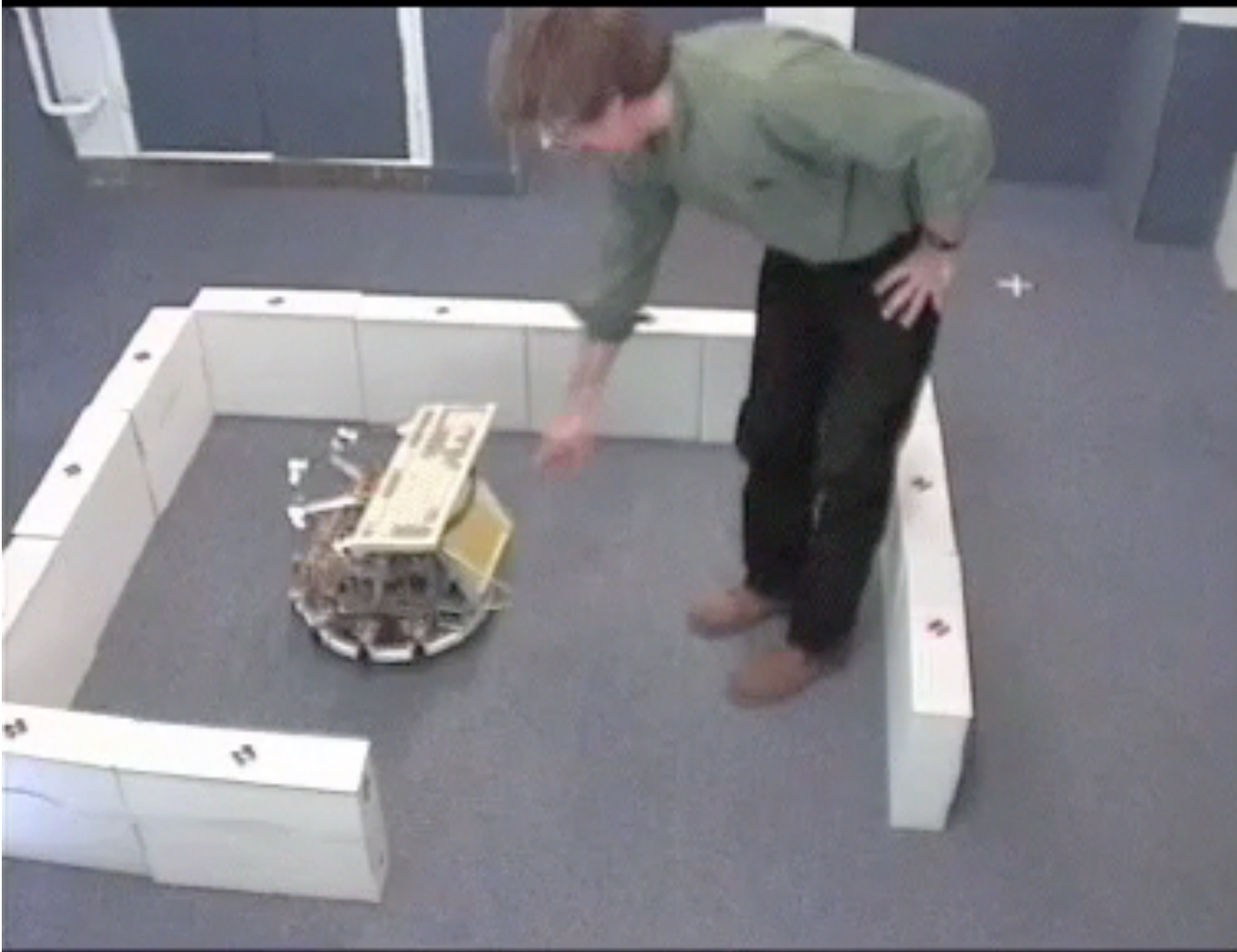












Observation:

- even though the approach is purely local, it does achieve global tasks
- based on the structure of the environment!

Conclusion

- attractor dynamics works on the basis low-level sensors information
- as long as the force-lets model the sensor-characteristics well enough to create approximate invariance of the dynamics under transformations of the coordinate frames

Summary

- behavioral variables
- attractor states for behavior
- attractive force-let: target acquisition
- repulsive force-let: obstacle avoidance
- bistability/bifurcations: decisions
- can be implemented with minimal requirements for perception